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UMI®
Computational Studies on the Properties and Reactions of Biological Radicals

by

Fuqiang Ban

Submitted in partial fulfillment of the requirements for the degree of Doctor of Philosophy

at

Dalhousie University
Halifax, Nova Scotia
July, 2001

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To my family.
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Abstract

Numerous biological radical systems have been discovered that are fundamental to understanding the catalysis of enzymes, the oxidative damage to DNA and proteins, and the mechanisms of anticancer drugs. Spectroscopic techniques are powerful tools for monitoring radicals. However, highly reactive and short-lived radical species are extremely difficult to characterize in experiments. Fortunately, recent advancements in density functional theory offer a complementary approach to solving chemical problems for biological systems of reasonable sizes.

This thesis describes the application of density functional theory to predicting properties and reaction mechanisms of several biological radical systems. In the first part of the thesis, the structures and hyperfine coupling constants of a number of amino acid-derived radicals generated upon irradiation are investigated systematically. A valid computational scheme for obtaining the zwitterionic form of amino acid radicals is provided. The second part of the thesis concentrates on selected reaction mechanisms for the radical systems of DNA. In particular, the cross-linking mechanisms of a DNA base and an amino acid residue in a nucleohistone and the actions of an antitumor drug that leads to cleavage of DNA strands are investigated. The preferred mechanisms are identified on the basis of computed potential energy surfaces for possible reaction pathways, providing great insight into the radical-mediated oxidative damage to DNA and into the chemistry of tumor-selective drugs. The observations from the amino acid-derived and DNA-based radicals provide a fundamental basis for future work on biological radical systems.
List of Symbols

\( \Psi \) wave function
\( \hat{H} \) total Hamiltonian
\( E \) energy
\( \hat{T} \) kinetic energy operator
\( \hat{V} \) potential energy operator
\( r_{ij} \) the distance between two particles
\( q_i \) electric charge
\( M_A \) the mass of the \( A^{th} \) nucleus
\( R_{AB} \) the distance between nuclei A and B
\( \chi_i \) spin orbital
\( \hat{F} \) Fock operator
\( \psi_i \) \( i^{th} \) molecular orbital
\( \epsilon_i \) \( i^{th} \) orbital energy
\( \hat{j}_j \) Coulomb operator
\( \hat{K}_j \) exchange operator
\( \phi_{\mu} \) \( \mu^{th} \) atomic orbital
\( F_{\mu\nu} \) element of the Fock matrix
\( P_{\mu\nu} \) element of the density matrix
\( S_{\mu\nu} \) element of the overlap matrix
\( C_{\mu\nu} \) expansion coefficient
\( (\mu\nu|\lambda\sigma) \) two-electron integral
\( \Phi_0 \) exact total molecular function
\( \nu_i \) \( i^{th} \) vibrational frequency
\( a_0 \) radius of a fixed spherical cavity
\( \rho \) electron density
\( E_{xc} \) exchange-correlation functional
\( T[\rho] \) kinetic energy functional
\( J[\rho] \) Coulomb repulsion energy functional
\( V_{\text{ee}}[\rho] \) interelectronic potential energy functional
\( E_x \) exchange functional
\( E_c \) correlation functional
\( v_{\text{eff}} \) effective potential
\( \hbar \) Planck's constant
\( \varepsilon \) dielectric constant
\( g_e \) electronic g-factor
\( \beta_e \) electronic magneton
\( g_N \) nuclear g-factor
\( \beta_N \) nuclear magneton
\( \rho^{a=\beta} \) spin density
\( B \) field strength
\( Z \) nuclear charge
\( \hat{S} \) electronic spin operator
\( S \) electronic spin
\( \hat{I} \) nuclear spin operator
\( I \) nuclear spin
\( A_{\text{iso}} \) isotropic hyperfine coupling constant
\( T_{ij} \) \( ij \)th component of the anisotropic hyperfine coupling tensor
\( \alpha \) alpha spin
\( \beta \) beta spin
### List of Abbreviations

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<thead>
<tr>
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<tbody>
<tr>
<td>HF</td>
<td>Hartree-Fock</td>
</tr>
<tr>
<td>UHF</td>
<td>Unrestricted Hartree-Fock</td>
</tr>
<tr>
<td>ROHF</td>
<td>Restricted open-shell Hartree-Fock</td>
</tr>
<tr>
<td>STO</td>
<td>Slater-type orbital</td>
</tr>
<tr>
<td>GTO</td>
<td>Gaussian-type orbital</td>
</tr>
<tr>
<td>CI</td>
<td>Configuration interaction</td>
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<td>Multi-reference configuration interaction</td>
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<td>DFT</td>
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<td>LDA, LSDA</td>
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<td>GGA</td>
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<tr>
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<td>Perdew's correlation functional</td>
</tr>
<tr>
<td>PW91</td>
<td>Perdew and Wang's 1991 correlation functional</td>
</tr>
<tr>
<td>SCRF</td>
<td>Self-consistent reaction field</td>
</tr>
<tr>
<td>PCM</td>
<td>Polarized continuum model</td>
</tr>
<tr>
<td>HFCC</td>
<td>Hyperfine coupling constant</td>
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<tr>
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<td>Electron spin resonance</td>
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Introduction

Biological radicals, species existing in living cells that contain one or more unpaired electrons, have become one of the most exciting topics in molecular biology.\textsuperscript{1-3} The increasing interest in biological radicals is due in part to the realization of the importance of many radical reactions in normal cellular chemistry and to their role in the mechanisms of many toxins.\textsuperscript{4} In particular, the discoveries of hypoxia-selective drugs that induce damage to tumors are noteworthy.\textsuperscript{5-7}

Due to their central roles in cellular chemistry, DNA\textsuperscript{8} and protein-derived\textsuperscript{9} radicals are of particular interest for understanding the functionality of biological radicals. In general, except for situations in which radicals act as catalytic centres of an enzyme, biological radicals in high concentration can seriously damage living organisms. The accumulation of damage in both DNA and proteins potentially induces various pathological conditions, for which cancer, Alzheimer's and many other diseases are of particular concern for human health. Hence, extensive experimental\textsuperscript{10} and theoretical\textsuperscript{11,12} studies have been performed on various biological radical systems.

In general, DNA and protein radicals originate by the attack of reactive oxygen species (ROS) of which the more common ones are the superoxide anion (O$_2^-$), hydroperoxyl (HOO$^*$) and hydroxyl (OH$^*$) radicals and hydrogen peroxide (H$_2$O$_2$). The
primary free radical in most oxygenated biological systems is $O_2^- \cdot$, generated from the
electron transport chains of mitochondria, chloroplastic and endoplasmic reticulum.
Furthermore, biological systems may convert $O_2^- \cdot$ to other reactive species such as
peroxyl (ROO$^\cdot$), alkoxy (RO$^\cdot$) and *OH radicals. The hydroxyl radical is the most
reactive and damaging of the ROS to both DNA and proteins. Hydroxyl radicals can be
generated by the Fenton reaction (I), UV radiation (II) or ionizing radiation (III)

I. $\text{Fe}^{2+} + \text{H}_2\text{O}_2 \rightarrow \text{Fe}^{3+} + \cdot\text{OH} + \text{OH}^-$

II. $\text{H}_2\text{O}_2 \xrightarrow{\text{UV}} 2 \cdot\text{OH}$

III. $\text{H}_2\text{O} \xrightarrow{\text{Ionizing radiation}} \text{H}^+ + \cdot\text{OH}$

The attack of *OH on DNA and proteins generates amino acid-, DNA base-, and
sugar-derived radical species. When the efficiency of repair enzymes decreases with age,
the reaction of these radicals with each other often leads to permanent alterations of DNA
or modifications of proteins.

While oxidative damage to DNA and proteins is recognized to be toxic towards
living cells, techniques have been developed that utilize the toxicity of biological radicals
for medical purposes. Radiation therapy is one of the first and most effective treatments
for many cancers. The high energy of radiation initially produces significant amounts of
*OH radicals. When focused on tumors, further propagation of radical reactions can lead
to DNA strand breaks, thus destroying the tumor cells. Sugar radicals have been found to
be the crucial intermediates for DNA strand breaks, as illustrated below.
Figure 1.1 Single strand DNA break via a sugar radical.

The above mechanism depends on molecular oxygen. Unfortunately, many regions of solid tumors are found to be hypoxic, having a lower oxygen level than normal cells. Thus, radiation would more easily kill normal cells than hypoxic tumor cells. Hence, the development of hypoxia-selective antitumor drugs has attracted great attention. In particular, the combination of radiation with such drugs has shown high efficacy in experiments.5–7

A general feature of radical species is their high reactivity and short life-times. Thus, radical species are often extremely difficult to characterize experimentally. For computational chemistry, however, the study of such species is generally as straightforward as the study of conventional long-lived stable species.
The development of efficient density functional theory methods\textsuperscript{13,14} and the emergence of faster computers have stimulated an increase in the application of the methods of computational chemistry in all branches of chemistry and biochemistry. The state-of-the-art of computational chemistry is the quantitative prediction of the properties and reaction mechanisms of important chemical systems. The work presented in this thesis focuses on computational studies of the properties and chemistry of biological radicals, in particular, oxidative damage or radiation induced DNA- and protein-derived radicals.

1.1 Thesis Summary

A brief overview of theoretical chemistry and of the methods employed in this thesis is presented in Chapter 2.

In Chapter 3, the radicals which have been proposed to be formed upon irradiation of glycine crystals are investigated. The results suggest that the radicals are R1: $^{\text{\textsuperscript{15}}}\text{NH}_3\text{C}^*\text{HCOO}$; R2: $^{\text{\textsuperscript{16}}}\text{CH}_2\text{COOH}$; R3: $^{\text{\textsuperscript{17}}}\text{NH}_2\text{C}^*\text{HCOOH}$ and R4: $^{\text{\textsuperscript{18}}}\text{NH}_2\text{CH}_2\text{COC}^*\text{HCOOH}$. A $C_s$ structure for R1, obtained using the Onsager model, gives hyperfine coupling constants in agreement with experiment. Hyperfine coupling constants computed for R2 are in agreement with unassigned experimental data. The computed hyperfine coupling constants for R4 are in good agreement with the experimental data previously assigned to the zwitterionic form $^{\text{\textsuperscript{19}}}\text{NH}_3\text{CH}_2\text{COC}^*\text{HCOO}$. It is shown that the structure of R3 is influenced significantly by the glycine crystal environment. Protonation of R3 gives rise
to hyperfine couplings similar to the experimental values assigned to one conformer of R3.

In Chapter 4, the radiation products (radicals R1: $^\cdot$CH(CH$_3$)COOH, R2: H$_3$N$^+$C$^\cdot$(CH$_3$)COO$^-$ and R3: H$_2$NC$^\cdot$(CH$_3$)COOH) of L-$\alpha$-alanine are investigated. Four conformers were found for R1 and R3. The zwitterionic form of radical R2 was obtained using the Onsager model. The relative energies of each of the four conformers of R1 and R3 show that structures with intramolecular hydrogen bonding are more stable. The computed hyperfine couplings are shown to be in good agreement with the results obtained from electron spin resonance spectroscopy. The effects of rotation about the N—C bond on the hyperfine coupling constants (HFCCs) of the amino protons in R2 support the previous suggestion that the amino protons are fixed by intermolecular hydrogen bonding in L-$\alpha$-alanine crystals. Moreover, a good correlation between the structure of the amino group and HFCCs in the four conformers of R3 was found.

The radiation products of hydroxyproline have been investigated in Chapter 5. In the resulting radicals, the choice of the apical ring atom was found to be dependent on the nature and strength of the intramolecular hydrogen bonding. The observed hyperfine couplings previously assigned to two zwitterionic conformers of the hydroxyproline primary radical anion are found to be better described by its non-zwitterionic isomers and corresponding neutral protonated isomers. Similarly, the observed hyperfine couplings for radicals formed by cleavage of the C$_\alpha$—N bond (deamination) are in closest agreement with those calculated for their neutral forms. Theoretical proton hyperfine couplings support the experimental assignment of the radical cation formed by
decarboxylation and the radicals resulting from hydrogen abstraction from the $C_2$ and $C_3$ positions. The proton hyperfine couplings are sensitive to the conformations of the radicals, which in turn are highly dependent upon the extent of intramolecular hydrogen bonding.

The mechanisms for the formation of a cytosine-tyrosine cross-link in a nucleohistone are investigated in Chapter 6. The reactions are modelled by use of smaller systems of cytosine, phenol and the major radicals derived from their reactions with hydroxyl radicals. The calculated reaction potential energy surfaces suggest that the direct radical combination mechanism of the $C_5$-hydroxylated cytosine radical and tyrosyl radical is preferred over the radical addition mechanisms of both tyrosyl radical to cytosine and the $C_5$-hydroxylated cytosine radical to tyrosine. Water and hydrogen bonding interactions are suggested to play a key role in catalyzing the subsequent hydrogen transfer step of the reaction.

In Chapter 7, the experimentally proposed mechanisms by which the antitumor drug tirapazamine may react with a DNA sugar-$C_1'$ radical to give the sugar derivative deoxyribonolactone, with concomitant DNA strand cleavage are investigated. For the previously proposed minor pathway, ionization of the sugar-$C_1'$ radical by tirapazamine, the calculated ionization energy and the electron affinity of the models of the sugar-$C_1'$ radical of DNA and tirapazamine suggest that tirapazamine must be protonated in order for it to be able to oxidize the sugar-$C_1'$ radical. The preferred mechanism for reaction of tirapazamine with a sugar-$C_1'$ radical, in agreement with experimental observations, is found to proceed by direct attack of an N-oxide oxygen of tirapazamine at the sugar-$C_1'$
position, followed by homolytic cleavage of the N—O bond of the drug moiety. Possible alternative mechanisms are also investigated.

Finally, global conclusions and possible directions for future research are provided in Chapter 8.

References


Theoretical Background

2.1 Introduction

Quantum chemistry is based on the laws of quantum mechanics and is being applied to an ever increasing range of chemical and biochemical problems. Theoretical chemistry, as it is often called, can provide an alternative independent approach to experiment for the chemist. It has opened great possibilities in describing the behaviour of electrons in atoms and molecules.

In principle, most chemical phenomena, if not all, can be predicted exactly. In practice, however, the fundamental equations of quantum chemistry cannot be solved exactly except for the simplest of systems, e.g., the hydrogen atom. However, this problem can be circumvented by application of various approximations, so that it is possible to obtain approximate, yet often highly accurate, results.

The development of density functional theory and the foundation of a hierarchy of well-calibrated computational methods are highlights of the progress in theoretical chemistry for the past several decades. In particular, the methods of theoretical chemistry can, in general, be applied as straightforwardly to reactive or transient species as they can to conventional long-lived species.
In this chapter, a brief overview of theoretical chemistry is given. In addition, some of the methods used in this thesis are described and their application in the investigation of various chemical properties is outlined.

2.2 The Schrödinger Equation

A fundamental postulate of quantum chemistry is that all information about a chemical system is described by some wave function $\Psi$. Essentially, most quantum chemical studies of chemical problems are concerned with the time-independent Schrödinger equation\(^1\)

$$\hat{H}\Psi(r, R) = E\Psi(r, R)$$  \hspace{1cm} (2.1)

where $\hat{H}$ is the Hamiltonian operator of the system. The Hamiltonian operator is the sum of kinetic energy ($\hat{T}$) and potential energy ($\hat{V}$) operators,

$$\hat{H} = \hat{T} + \hat{V}$$  \hspace{1cm} (2.2)

The terms $\hat{T}$ and $\hat{V}$ are given by the expressions:

$$\hat{T} = -\sum_i \frac{\hbar^2}{8\pi^2 m_i} \nabla_i^2$$  \hspace{1cm} (2.3)

$$\hat{V} = \sum_{i<j} \frac{q_i q_j}{r_{ij}}$$  \hspace{1cm} (2.4)

where the sum is over all particles $i$ (nuclei and electrons), $m_i$ is the mass of particle $i$, $\hbar$ is Planck’s constant, $r_{ij}$ is the distance between two particles, and $q_i$ and $q_j$ are the electric charges of particles $i$ and $j$, respectively. For electrons, $q_i = -e$ where $e$ is the fundamental unit of charge ($1.60210 \times 10^{-19}$ C), while for a nucleus with atomic number $Z_i$, $q_i = +Z_i e$. 
In atomic units the Hamiltonian operator for a system of \( n_E \) electrons and \( N_N \) nuclei is given by

\[
\hat{H} = -\sum_{\alpha=1}^{N_N} \frac{1}{2M_\alpha} \nabla_\alpha^2 - \sum_i \frac{1}{2} \nabla_i^2 - \sum_\alpha \frac{Z_\alpha^{}}{r_\alpha} + \sum_{i<j} \frac{1}{r_{ij}} + \sum_{\alpha<\beta} \frac{Z_\alpha^{}}{R_{\alpha\beta}}
\]  

(2.5)

where, \( A, B \) and \( i, j \) are the indices for the \( N_N \) nuclei and the \( n_E \) electrons, respectively. \( M_\alpha \) is the mass of the \( \alpha^{th} \) nucleus and \( R_{AB} \) is the distance between nuclei \( A \) and \( B \).

2.3 The Born-Oppenheimer Approximation and Electronic Problems

Because the Schrödinger equation (2.1) of molecular systems is generally too complicated to be solved exactly, approximations must be made to in order for it to be practically applicable.

The first common technique for simplifying the problem is to separate the nuclear and electronic motions based on the Born-Oppenheimer approximation.\(^2,3\) Since the nuclei are much heavier and move much more slowly than the electrons, the electrons can be treated as moving in a field of fixed nuclei. As a consequence, the energy terms depending on the nuclear coordinates can be separated; that is, the nuclear kinetic term can be neglected and the nuclear potential term can be treated as a constant. Hence, the electronic Hamiltonian is given by

\[
\hat{H}^{\text{el}} = -\frac{1}{2} \sum_i \nabla_i^2 - \sum_\alpha \frac{Z_\alpha^{}}{r_\alpha} + \sum_{ij} \frac{1}{r_{ij}}
\]  

(2.6)

and the electronic form of the Schrödinger equation can be written as

\[
\hat{H}^{\text{el}} \Psi(r) = E^{\text{el}} \Psi(r)
\]  

(2.7)
where \( E^{\text{ele}} \) is the electronic energy. The total energy for a particular nuclear arrangement is given by

\[
E^{\text{total}}(R) = E^{\text{ele}} + \sum_{A<B} \frac{Z_A Z_B}{R_{AB}}
\]  

(2.8)

Equation (2.8) defines the molecular potential energy surface for different nuclear configurations (see Section 2.9).

### 2.4 Hartree-Fock Theory

Due to the inseparable electron-electron repulsion term in (2.6), the electronic Schrödinger equation (2.7) cannot be solved analytically for molecules with more than one electron. Thus, the Hartree-Fock (HF) approximation, or the independent particle model, was devised to break down the many-electron Schrödinger equation (2.7) into a set of one-electron Hartree-Fock equations.

#### 2.4.1 The Hartree-Fock Approximation

In the Hartree-Fock approximation,\(^{3-5}\) all electrons in a molecule are assumed to be independent. More specifically, any electron can be treated as a free electron moving in an effective field of the other electrons where the electron-electron repulsion is treated in an average way. Thus, the motion of each electron can be described by a single electron wave function or the spin orbital \((\chi_i)\); a product of the molecular orbital (a spatial function \(\psi(r_i)\)) and a spin function (\(\alpha \) or \(\beta\)). If the spin orbitals are obtained for each electron, a Hartree product of the spin orbitals can be constructed as a molecular wave
function. However, in order to satisfy the antisymmetry principle, the molecular wave function can be written as a Slater determinant

$$\Psi_0(1,2,...,N) = (N!)^{-\frac{1}{2}}|\chi_1(1)\chi_2(2)...\chi_N(N)|$$

(2.9)

where N is the number of electrons. Representation of the molecular wave function by a single Slater determinant (2.9) is the simplest approximation and is referred to as a single reference or single determinantal wave function.

Hartree-Fock theory is based on the variational method\textsuperscript{3} of quantum mechanics. When a normalized single Slater determinant is used as a trial function for the ground state, the variational principle allows us to obtain the optimum approximate wave function by minimizing the expectation energy with respect to the spin orbitals without directly solving the Schrödinger equation. This mathematical treatment\textsuperscript{4} leads to a set of Hartree-Fock (HF) equations.

$$\hat{F}\psi_i = \varepsilon_i\psi_i \quad i = 1, 2, ..., N$$

(2.10)

$$\hat{F} = -\frac{1}{2}\nabla^2 - \sum_{\lambda} \frac{Z_{\lambda}}{r_{\lambda}} + \sum_j (2\hat{J}_j - \hat{K}_j)$$

(2.11)

where $\hat{F}$ is the Fock operator and $\varepsilon_i$ is the $i^{th}$ orbital energy. The sum over $j$ is over the occupied orbitals. The summation of the Coulomb operator $\hat{J}_j$ and the exchange operator $\hat{K}_j$ describes the effective potential seen by the electron in the $i^{th}$ spin orbital.

Since the Fock operator in equation (2.10) has a functional dependence on the spin orbitals, the HF equations can only be solved by an iterative procedure.
2.4.2 The LCAO Approximation and the Roothaan-Hall Equations

The HF equations can be solved numerically for atoms with the corresponding solutions being the well-known atomic orbitals. However, numerical solution for molecules is impractical. Hence, Roothaan\(^6a\) and Hall\(^6b\) simplified the problem of solving the HF differential equations for molecules to that of solving a set of algebraic equations by using the LCAO approximation in which the unknown molecular orbitals \(\psi_i\) are expanded as a linear combination of a set of atomic orbitals \(\{\phi_\mu\}\)

\[
\psi_i = \sum_\mu C_{\mu i} \phi_\mu
\]  \tag{2.12}

where \(C_{\mu i}\) is a coefficient and \(M\) is the number of atomic orbitals. The atomic orbitals used in the expansion are described by the basis set (see Section 2.5).

Substituting equation (2.12) into the HF equations (2.10), and applying the variational method leads to the Roothaan-Hall equations,

\[
\sum_{\mu=1}^{M} C_{\mu i} (F_{\mu \nu} - \varepsilon_i S_{\mu \nu}) = 0 \quad \nu = 1, 2, ..., M \tag{2.13}
\]

where \(F_{\mu \nu}\) is an element of the Fock-matrix and \(S_{\mu \nu} = \langle \phi_\mu | \phi_\nu \rangle\) denotes the overlap integral. For closed-shell molecules, \(F_{\mu \nu}\) is defined by

\[
F_{\mu \nu} = H_{\mu \nu} + \sum_\lambda \sum_\sigma P_{\lambda \sigma} [(\mu \nu | \lambda \sigma) - \frac{1}{2} (\mu \lambda | \nu \sigma)]
\]  \tag{2.14}

\[
H_{\mu \nu} = \left( \phi_\mu \left| -\frac{1}{2} \nabla^2 - \sum_\Lambda \frac{Z_\Lambda}{r_{i\Lambda}} \right| \phi_\nu \right)
\]  \tag{2.15}
where $P_{\lambda\sigma} = \sum_{i=1}^{\infty} C_{\lambda i} C_{\sigma i}^*$ represents the density matrix and the $(\mu\nu|\pi\sigma)$ are the classical electron-electron repulsion integrals defined by

$$(\mu\nu|\lambda\sigma) = \langle \phi_{\mu}(1)|\phi_{\nu}(1)\frac{1}{r_{12}}|\phi_{\lambda}(2)|\phi_{\sigma}(2)\rangle$$

(2.16)

The $C_{\mu i}$ expansion coefficients can be obtained by standard matrix techniques.

For open-shell molecules, it is more appropriate to introduce different spin orbitals for electrons with different spins. The independent variation of two sets of coefficients leads to the unrestricted Hartree-Fock (UHF) formalism in which more flexibility is given to describe the interactions between same spin electrons and opposite spin electrons. Thus, UHF produces a better description for radical species and for the dissociation of molecules. The main deficiency of the UHF method is that the wave functions are not eigenfunctions of the spin operator $\hat{S}^2$, hence they contain spin contamination from higher multiplicities.

The restricted open-shell Hartree-Fock (ROHF) method is another possible HF-based approach for open-shell molecules. In ROHF all electrons are restricted to be paired except for the electrons in open-shell orbitals. The ROHF wave functions are eigenfunctions of the spin operator, however, the disadvantage of ROHF is that it raises the variational energy. Thus, the ROHF method is not as general and practical as the UHF approach. For example, ROHF does not provide a satisfactory description of bond breaking.
2.5 Basis Functions

As described in the previous section, when iteratively solving the Roothaan-Hall calculations for a molecule of interest, an approximate orbital wave function can be constructed by a linear combination of atomic orbitals of the constituent atoms of the molecule.

For describing the atomic orbitals, two types of functions\textsuperscript{3,4} have received the most widespread use; Slater-type orbitals [an STO: $\phi^{\text{STO}}_{nlm} \propto r^{n-\frac{1}{2}} \exp(-\zeta r) Y_{lm} (\theta, \phi)$] and Gaussian-type orbitals, [a GTO: $\phi^{\text{GTO}}_{kmm} \propto x^k y^m z^n \exp(-\zeta r^2)$], where $\zeta$ depends on the type of orbitals, e.g., s, p, d ...

Both types of orbital have their advantages and weaknesses. Slater-type orbitals correctly describe the orbital cusp at the nucleus of an atom. However, STOs are expensive or impractical for computing electron-electron repulsion integrals for molecular systems. In contrast, Gaussian-type orbitals (GTOs) are computationally very efficient for electron-electron repulsion integrals; but GTOs have the wrong behavior both near and far from the nucleus. However, one can take a linear combination of GTOs $\{ \phi^{\text{GTO}}_p \}$ to give a better description of an atomic orbital ($\phi_\mu$), i.e.,

$$\phi^{\text{CGF}}_\mu = \sum_{p=1}^{M} d_{\mu p} \phi^{\text{GTO}}_p$$  \hspace{1cm} (2.17)

The coefficients $d_{\mu p}$ and the primitive GTO exponents are determined by minimizing the error in the fit of the M GTO's to the exact Slater orbital in a least squares sense. In particular, the optimized ratio of expansion coefficients of a particular set of primitive
GTOs is often fixed to approximate an STO basis function, known as the so-called contracted Gaussian-type basis function. Thus, we are able to use the computationally less-expensive GTOs while minimizing the error introduced by use of GTOs.

An infinite primitive GTO set would fit an atomic orbital precisely, however, one cannot use such a set. Hence, in practical applications, a hierarchy of finite contracted GTO basis sets has been developed.

To improve a basis set, polarization functions and diffuse functions may be included. Polarization functions are basis functions of higher angular momentum, while diffuse functions are basis functions with very small exponents. They can enhance the flexibility of a basis set for describing the anisotropic distribution of the electrons in a molecule. These functions are very important for higher level calculations.\(^7\)

The well-known contracted Gaussian-type basis sets due to Pople and co-workers\(^8-\)^\(^10\) are used throughout this thesis.

### 2.6 Electron Correlation

The general success of Hartree-Fock theory is due to the fact that the average interactions between electrons are the dominant part of electron-electron repulsion. As mentioned in Section 2.4.1, the HF molecular wave function takes the form of a Slater determinant, ensuring that electrons with the same spin are correlated. However, neither the HF molecular wave function nor the HF Hamiltonian considers the instantaneous correlation of electrons of opposite spin. Since every electron tends to avoid coming
close to another, neglect of the instantaneous electron correlation is a defect of Hartree-Fock theory. The total correlation energy is the difference between the exact nonrelativistic total energy and the HF energy obtained in the limit of a complete basis set,

$$E_{\text{corr}} = E^{\text{exact}} - E^{\text{HF}}$$  \hfill (2.18)

Although the correlation energy is usually less than one percent of the total energy, electron correlation effects are often of great importance in quantitative predictions of molecular properties.

2.7 Conventional Correlated Methods

One way to account for electron correlation is to construct an accurate total molecular wave function based on the approximate HF Hamiltonian. One idea is to apply tractable approximations to truncate the exact wave function for desired accuracy. Many different approaches have been developed in wave function-based correlation theory, which are collectively referred to as the conventional correlated methods.

2.7.1 Configuration Interaction

Configuration interaction (CI) theory,\textsuperscript{4,11,12} in which electron correlation effects are included by mixing configurations of excited states into the molecular wave function is conceptually the simplest approach. In CI theory, the excited state configurations are constructed using the HF Slater determinant for the ground state of a system as a single
reference. The determinant formed by moving only one electron from an occupied orbital of the HF configuration to a virtual orbital is called a singly excited configuration. Similarly, by multiple substitutions, doubly and higher excited configurations can be generated. According to the principle of superposition, the exact total molecular function, $\Phi_0$, is given by a linear combination of all the possible configurations

$$\Phi_0 = C_0 \Psi_0 + \sum_i C_i \Psi_i \tag{2.19}$$

where $\Psi_0$ is the HF configuration and the $\Psi_i$ are excited configurations. All coefficients are varied to minimize the expectation value of the energy.

The energy obtained by a full CI treatment for a complete basis set corresponds to the exact non-relativistic energy of the molecular system. For a given basis set of $N$ basis functions, the full CI (FCI) wave function and the corresponding full CI energy are the best possible.

### 2.7.2 Limited Configuration Interaction

While the full CI method will give, in principle, the exact solution to the Schrödinger equation, determining the full CI wave function using moderate basis sets is prohibitive even for small molecules. However, truncated CI methods, where only certain types of excitations are included in the CI wave function expansion (2.19), are suitable for studying various properties of chemical systems. The CIS method in which only single substitutions are included, may provide a proper description of one-electron properties such as dipole moment, while the CID method, in which only the doubly
excited configurations are included, may recover most of the correlation energy. The CISD method, in which all single and double substitutions are included, may further improve the results.

The CIS, CID and CISD methods are feasible for systems with a reasonably large number of electrons and basis functions. Furthermore, these methods are variational, i.e., the energy obtained is an upper bound to the exact energy. However, unlike the full CI method, the CID and CISD methods are not size-consistent, i.e., the energy calculated for a system composed of two fragments infinitely separated is not the same as the sum of the energies of the two separate fragments. This deficiency becomes increasingly apparent as the size of the system increases.

2.7.3 Multireference Configuration Interaction

The multireference configuration interaction method (MRCI) is one approach that may be taken to restore size-consistency by selectively including some triple- and quadruple-excited configurations. Firstly, the reference configurations are selected by a list of the more important excitation-determinants according to their energy contribution in a CISD calculation. Secondly, a subspace of all the singly and doubly excited configurations from the reference configurations is generated. Lastly, a predetermined energy threshold is often chosen for selecting important configurations from the subspace for the configuration interaction calculation. Thus, by systematically varying the basis set, reference space and energy threshold, the MRCI method may approach the full
CI predictions using a reduced number of configurations. However, MRCI methods are not automated and too expensive for general application.

2.7.4 Quadratic Configuration Interaction

Quadratic configuration interaction (QCI)\textsuperscript{15} is an effective approach developed by Pople and co-workers\textsuperscript{15} to restore size consistency, and has found widespread application. QCI methods modify the wave function by adding quadratic terms. Thus, the QCISD method effectively includes contributions from all singles, doubles and some quadruples. However, the QCISD method takes inadequate account of the contributions of triple excitations. Because implementation of QCISDT for large systems is impractical, an approximate version, QCISD(T) has been devised by including the effects of triples via a perturbative approach. The QCI based methods are size-consistent, but not variational.

2.7.5 Møller-Plesset Perturbation Theory

An alternative approach to systematically recovering the correlation energy is Møller-Plesset (MP) perturbation theory,\textsuperscript{16,17} in which the total Hamiltonian of the system (H) is written as the sum of a Hartree-Fock part (\(H_0\)) and a perturbation (\(\lambda V\)):

\[
H = H_0 + \lambda V
\]  

(2.20)

The perturbation, \(V\), is the difference between the exact Hamiltonian operator and the Hartree-Fock Hamiltonian operator, i.e., the difference between the true interelectronic repulsion and the Hartree-Fock interelectronic potential.
According to Rayleigh-Schrödinger perturbation theory, the exact wave function \( \Psi \) and energy \( E \) may be expanded as a Taylor series of \( \lambda \). Thus, they can be written as

\[
\Psi = \Psi^{(0)} + \lambda \Psi^{(1)} + \lambda^2 \Psi^{(2)} + \ldots \tag{2.21}
\]

and

\[
E = E^{(0)} + \lambda E^{(1)} + \lambda^2 E^{(2)} + \ldots \tag{2.22}
\]

The various orders of Møller-Plesset perturbation theory are obtained by setting \( \lambda = 1 \), and truncating (2.21) and (2.22) to various orders. The Møller-Plesset energy to first-order corresponds to the Hartree-Fock energy. Corrections to the energy by including the electron correlation are obtained by going to second order (MP2) and higher-order MPn methods. The MP perturbation theory has the advantage of being size-consistent, however, the energies are not variational.

Both configuration interaction methods and MP perturbation methods belong to conventional correlated methods, which are based on determining the electronic wave function. Computationally, they are often very expensive for incorporating the effects of electron correlation.

### 2.8 Density Functional Theory

Density functional theory is an alternative approach to the electron correlation problem. In comparison to the conventional correlated methods previously discussed, density functional theory\(^{18-20}\) looks at the molecular problem from a different perspective. Only the average number of electrons located at any point in space is considered instead of the motion of individual electrons. Density functional theory attempts to obtain all
information including the wave function from the electron density of the system. This simplicity of DFT has motivated many great developments in the past three decades.

2.8.1 Two Theorems of Density Functional Theory

The foundation, or the two fundamental theorems, of DFT were laid down by Hohenberg and Kohn (HK) in 1964. The first theorem showed that the external potential \( v(r) \) of an N-electron system is uniquely determined by the electron density \( \rho(r) \); the Hamiltonian and wave function of the ground state depend only on the electron density. Thus, the energy of the system can be expressed as a functional of the density

\[
E[\rho] = \int \rho(r) v(r) dr + T[\rho] + V_\alpha[\rho]
\]

(2.23)

where \( T[\rho] \) is the kinetic energy and \( V_\alpha[\rho] \) is the electron-electron interaction energy.

The second theorem is similar to the energy variation principle, in that for any trial electron density \( \rho'(r) \), the corresponding energy \( E[\rho'] \) is an upper bound to the exact energy of the ground state;

\[
E[\rho'] \geq E[\rho]
\]

(2.24)

where \( E[\rho] \) is the true ground-state energy.

2.8.2 The Kohn-Sham Theory

In 1965, Kohn and Sham founded the basis for practical applications of DFT by developing a theory in which the Schrödinger equation for an N-electron interacting
system is replaced with a set of single-particle equations that can provide the electron
density of the original system.

Setting up a non-interacting N electron reference system, Kohn and Sham
introduced N orbitals for N non-interacting electrons. The Hamiltonian is given by

$$\hat{H}_s = \sum_i^n -\frac{1}{2} \nabla_i^2 + V_N(r)$$

while the exact ground-state wave function is a normalized determinant

$$\psi_s = \frac{1}{\sqrt{N!}} |\psi_1 \psi_2 ... \psi_N|$$

where the $\psi_i$ are the N lowest eigenfunctions of the one-electron Hamiltonian

$$\hat{h}_s = -\frac{1}{2} \nabla^2 + V_N(r)$$

$$\hat{h}_s \psi_i = \epsilon_i \psi_i$$

The energy of the non-interacting system in the potential $V_N(r)$ can be obtained,

$$E_s[\rho] = T_s[\rho] + \int V_N(r) \rho(r) dr$$

where $T_s[\rho]$, the exact kinetic energy for the reference system, is given by

$$T_s[\rho] = \sum_i^n \langle \psi_i | -\frac{1}{2} \nabla^2 | \psi_i \rangle$$

For the real interacting N-electron system, the classical Coulomb interaction $J[\rho]$ and the exchange-correlation energy $E_{xc}[\rho]$ need to be included. Thus, the total energy of the real system is given by:

$$E[\rho] = T_s[\rho] + \int V_N(r) \rho(r) dr + J[\rho] + E_{xc}[\rho]$$

where $E_{xc}[\rho]$ is defined by
\[ E_{xc}[\rho] = T[\rho] - \mathcal{T}_s[\rho] + V_{xc}[\rho] - J[\rho] \]  

and \( T[\rho] \) is the exact kinetic energy functional of the real system. Thus, the effective potential can be written as

\[ v_{\text{eff}}(r) = V_N(r) + \int \frac{\rho(r')}{|r - r'|} \, dr' + v_{xc}(r) \]  

\[ v_{xc}(r) = \frac{\delta E_{xc}[\rho]}{\delta \rho(r)} \]  

where \( v_{xc}(r) \) is the exchange-correlation potential.

Equation (2.28) allows a direct combination of the exact kinetic energy functional of the reference system and the effective potential of the real system, leading to the Kohn-Sham (KS) one-electron equations:

\[ (-\frac{1}{2} \nabla^2 + v_{\text{eff}})\psi_i^{KS} = \varepsilon_i \psi_i^{KS} \quad i=1, 2, ..., N \]  

here the eigenfunction \( \psi_i^{KS} \) is the Kohn-Sham orbital. The electron density is obtained by

\[ \rho(r) = \sum_i |\psi_i^{KS}|^2 \]  

The KS equations (2.35) take a form analogous to the Hartree-Fock equations (2.10). When the LCAO approximation (2.12) is applied to the \( \psi_i^{KS} \), the KS equations can be solved in exactly the same manner as the HF equations if the exchange-correlation functional \( E_{xc}[\rho] \) in (2.34) is known.

Unfortunately, the exact form of \( E_{xc}[\rho] \) is unknown. Thus, various models including the local density approximation (LDA)\(^{18,19,23-25}\) and generalized gradient approximations (GGA)\(^{26-31}\) have to be employed for practical calculations.
2.8.3 Local Density Approximation-based Functionals

In KS DFT theory, the first generation of effective approximate functionals for molecular purposes was based on the local spin density approximation (LSDA).\textsuperscript{18,19,23} The LSDA exchange-correlation energy, is defined by

\[ E_{xc}^{\text{LSDA}} = \int \rho(r) E_{xc}^{\text{LSDA}}[\rho^a(r), \rho^b(r)]dr \] (2.37)

where \( E_{xc}^{\text{LSDA}} \) is the exchange correlation energy per particle. All explicit forms of \( E_{xc}^{\text{LSDA}} \) are obtained, based on the assumption that the \( E_{xc} \) can be separated into an exchange functional \( E_x \) and a correlation functional \( E_c \). One such functional is SVWN, which is a linear combination of the Slater exchange term\textsuperscript{24} and the correlation functional fitted by Vosko, Wilk and Nusair.\textsuperscript{25} In general, LSDA performs fairly well. However, it grossly overestimates molecular bond energies.\textsuperscript{29}

2.8.4 Generalized Gradient Approximation-based Functionals

To correct the non-uniformity of the electron density modelled by LSDA, the generalized gradient approximation (GGA) correction is introduced, in which the exchange-correlation functional depends explicitly on both the local densities and the local spin gradients, i.e.,

\[ E_{xc}^{\text{GGA}} = \int [\rho^a(r), \rho^b(r), \nabla \rho^a(r), \nabla \rho^b(r)]dr \] (2.38)
The correlation corrections by Perdew (P86),\textsuperscript{26} Lee, Yang, and Parr (LYP)\textsuperscript{27}, and by Perdew and Wang (PW91)\textsuperscript{28} are in common use. In particular, the LYP functional provides a very good way to calculate correlation energies from electron densities.

The two most popular GGA-corrected exchange functionals are PW86\textsuperscript{30} (Perdew and Wang) and B88 (Becke).\textsuperscript{31}

### 2.8.5 Becke Half and Half Functional

Even the inclusion of GGA-correction to the LSDA approximations lacks chemical accuracy in thermochemical tests.\textsuperscript{32} Inspired by the idea that exact-exchange-plus-LSDA-correlation improves certain atomic applications, Becke proposed a half and half theory based on an adiabatic connection formula.\textsuperscript{33} The Becke half and half functional\textsuperscript{34} is given by

\[
E_{\text{xc}} = \frac{1}{2} E_x + \frac{1}{2} E_{\text{xc}}^{\text{LSDA}}
\]  

(2.39)

where $E_x$ is the exact exchange in KS DFT theory and $E_{\text{xc}}^{\text{LSDA}}$ is the exchange-correlation energy estimated by the LSDA approximation. The Becke half and half functional is reasonably successful for describing bond dissociation behaviour\textsuperscript{35} and predicting reaction barrier heights.\textsuperscript{36}
2.8.6 Becke's Three-parameter Hybrid Functional

Becke's three-parameter hybrid functionals are a linear combination of the exact HF exchange, LSDA for exchange-correlation, and the gradient corrections to exchange and correlation. The original functional\textsuperscript{37a} is expressed by

\[
E_{xc} = E_{xc}^{\text{LSDA}} + a_0 (E_{x}^{\text{exact}} - E_{x}^{\text{LSDA}}) + a_x \Delta E_x^{\text{BS88}} + a_c \Delta E_c^{\text{PW91}} \tag{2.40}
\]

The coefficients $a_0$, $a_x$, and $a_c$ were optimized to be 0.20, 0.72 and 0.81, respectively, by use of a standard set of thermochemical data. Combining Becke's hybrid exchange functional with various correlation functionals yields different DFT methods. For example, the B3LYP method\textsuperscript{37ab} uses the LYP correlation functional.

Due to the inclusion of electron correlation, the DFT procedures are superior to HF methods. Gradient-corrected DFT, in particular Becke's three-parameter hybrid functional, often provides excellent results for molecular properties.

The principal advantages of DFT methods over the conventional correlated methods are the computational efficiency and the small disk requirements. At present, the DFT methods are the preferred choice for molecular systems that are too large to be treated by conventional correlated methods. One disadvantage of DFT is that when it fails there is no systematic way to improve the results as in the conventional correlated methods, other than improving the basis set used.
2.9 Exploring Potential Energy Surfaces

As shown in equation (2.8), within the Born-Oppenheimer approximation, the energy of a molecule can be considered as a function of the positions of the nuclei. Such functions define the potential energy surface of the molecule with all possible nuclear arrangements. Along the potential surface, the determination of equilibrium and transition structures is fundamental to understanding the chemistry of a molecular system. For example, Figure 2.1 shows the potential surface for an S_N2 reaction. Optimizing the equilibrium structures and transition structures for a reaction path is often a challenge in computational chemistry.

![Potential Energy Surface Diagram](image)

Figure 2.1 Schematic illustration of the potential energy surface for an S_N2 reaction in the gas phase illustrating equilibrium and transition structures.
2.9.1 Geometry Optimization

Mathematically, equilibrium structures and transition structures are stationary points on the potential energy surface where all first derivatives of the energy with respect to the 3N-6 internal coordinates of a molecular system of N nuclei are zero. They can be obtained analytically under the following requirements

$$\frac{\partial E}{\partial R_i} = 0 \quad i = 1, 2, \ldots, 3N-6. \quad (2.41)$$

2.9.2 Frequency Analysis

Equilibrium structures and transition structures are distinguished by examining the second derivatives of the energy, also referred to as the force constants,

$$\frac{\partial^2 E}{\partial R_i \partial R_j} \quad i, j = 1, 2, \ldots, 3N-6. \quad (2.42)$$

In practice, this is done by analysis of the harmonic vibrational frequency using standard methods. Equilibrium structures are characterized by having all real frequencies because they are minima, while transition structures (first-order saddle points) have exactly one imaginary frequency.
2.9.3 The Zero Point Vibrational Energy Correction

An optimized equilibrium or transition structure is defined on the Born-Oppenheimer vibrationless potential energy surface, in a vacuum, at 0 K. When determining the relative energies of different species, the zero-point vibrational energy (ZPVE) should be included. The ZPVE is calculated as:

$$\text{ZPVE} = \frac{1}{2} \sum_{i} h\nu_i \quad i = 1, 2, \ldots, n$$  \hspace{1cm} (2.43)

where $\nu_i$ is the $i^{th}$ vibrational frequency of the particular species. For transition structures, however, the imaginary frequency is not included in (2.43). Due to the neglect of anharmonicity and incomplete treatment of electron correlation, the calculated harmonic vibrational frequencies are often larger than the experimental vibrational frequencies ($\nu_i$).\textsuperscript{39,40} Thus, ZPVEs are often scaled by an appropriate factor obtained for the level of theory being used.

2.10 Approximation of Environmental Effects

The methods that have been discussed so far are for the gas phase without external environmental effects. While predictions for the gas phase are appropriate for systems that are weakly affected by an environment, approximation of specific environmental effects or bulk environmental effects must be included for a molecule whose nature is significantly modified or altered. For example, environmental effects
must be considered if one wishes to model a solvent-assisted reaction or obtain the zwitterionic structures of an amino acid in the solid state.

2.10.1 Reaction Field Models of Solvation

For chemical systems in solution, a common approach used for describing the electrostatic interaction between solute and solvent is the self-consistent reaction field (SCRF) approach. An advantage of the SCRF approach is that it models the bulk environmental effects at the same level of theory as the molecule is treated.

There are various SCRF methods implemented in GAUSSIAN 94\textsuperscript{41a} and 98\textsuperscript{41b}. They all treat the solvent as a polarizable medium with a dielectric constant, the magnitude of which is a measure of the polarity of the solvent. When a molecule of the gas phase is embedded in a cavity of the dielectric continuum, the dipole of the molecule will induce a dipole in the medium allowing them to interact electrostatically.

![Diagram](image)

Figure 2.2 Schematic representation of the (a) Onsager model, and (b) polarized continuum model

The Onsager model\textsuperscript{42,43} is the simplest method in the SCRF approach. In this method, the solute occupies a fixed spherical cavity (see Figure 2.2a) of radius $a_0$, which is estimated by calculation of the solute volume. Since the Onsager model is very
effective for geometry optimization and frequency calculations, it was combined with DFT methods for predicting zwitterionic radicals derived from amino acids in this thesis.

Another SCRF model that has been used for single point calculations in this thesis is the polarized continuum model (PCM).\textsuperscript{44ab,45} The PCM differs from the Onsager model by defining a more realistic cavity (see Figure 2.2b) built with interlocking spheres centered on the atoms, thus enabling a more accurate description of the solvent effects. The effect of the polarization of the solvent continuum is calculated numerically. Thus, PCM provides a more accurate description of the solvent effect.

2.11 Hyperfine Structure: The Fingerprint of a Radical

The hyperfine structures displayed in an electron spin resonance (ESR) spectrum are the fingerprints of a radical species and may be reproduced by accurate theoretical calculations. As part of the research in this thesis is concerned with calculating the hyperfine structures of amino acid derived radicals, the basics of ESR\textsuperscript{46} and the performance of theory\textsuperscript{47} for interpreting the ESR spectrum are outlined.

2.11.1 Hyperfine Interaction

All radicals have one or more unpaired electrons with intrinsic spin. The possession by an electron of both a negative charge and spin gives rise to a magnetic moment for the unpaired electron,

$$\mu_e = -g_e \beta_e S$$ \hfill (2.44)
where $S$ is the electronic spin, and $g_e$ and $\beta_e$ are the electronic $g$-factor and magneton, respectively.

In addition to the unpaired electron, a radical may contain magnetic nuclei that are necessary for a measurement in magnetic resonance spectroscopy. These magnetic nuclei with nuclear spin and charge can provide other magnetic moments,

$$
\mu_N = g_N \beta_N I
$$

(2.45)

where $I$ is the nuclear spin, and $g_N$ and $\beta_N$ are the nuclear $g$-factor and magneton, respectively.

As the unpaired electron is delocalized in a radical, there is a nonzero probability that the unpaired electron exists at the nucleus. Hence, the magnetic moment of the electron and a nucleus can interact, giving rise to the hyperfine interaction.

### 2.11.2 Isotropic and Anisotropic Hyperfine Coupling Constants

For a given nucleus, the hyperfine interaction can be described by the hyperfine coupling tensor $A$ in the Hamiltonian of the hyperfine interaction,

$$
\hat{H}_m = \hat{I} \cdot A \cdot \hat{S}
$$

(2.46)

where

$$
A = \begin{bmatrix}
A_{xx} & 0 & 0 \\
0 & A_{yy} & 0 \\
0 & 0 & A_{zz}
\end{bmatrix}
$$

(2.47)
The $A_{ii}$ (i=X, Y and Z) are called the principal components of the hyperfine coupling tensor. The $A$ tensor can be separated into two parts,

$$
A = A_{iso} \cdot \begin{bmatrix}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{bmatrix} + \begin{bmatrix}
T_{xx} & 0 & 0 \\
0 & T_{yy} & 0 \\
0 & 0 & T_{zz}
\end{bmatrix}
$$

(2.48)

where $A_{iso}$ is the isotropic hyperfine coupling constant describing the magnitude of the hyperfine interaction, and $T_{xx}$, $T_{yy}$ and $T_{zz}$ ($T_{xx} + T_{yy} + T_{zz} = 0$) are the anisotropic hyperfine coupling constants determining the orientation of the hyperfine interaction.

The isotropic hyperfine coupling arises from a quantum mechanical contact of the unpaired electron and the nucleus. Theoretically, $A_{iso}$ can be calculated via the spin density at the nucleus,

$$
A_{iso} = \frac{4}{3} g_e \beta_e g_N \beta_N < S_z >^{-1} \rho_{a-b}^{a-b}(0)
$$

(2.49)

where $< S_z >^{-1}$ is the eigenvalue of the spin operator $\hat{S}_z$, and $\rho_{a-b}^{a-b}(0)$ is the spin density at the nucleus. The units used for hyperfine coupling constants are typically gauss (G) or megahertz (MHz).

The anisotropic hyperfine coupling constants result from the electron-nuclear magnetic-dipole interactions and reflect the anisotropy of the spin distribution of a radical species. The $ij^{th}$ component of the anisotropic coupling can be computed from

$$
T_{ij} = \frac{1}{2} g_e \beta_e g_N \beta_N < S_z >^{-1} \sum_{\mu,\nu} \rho_{\mu,\nu}^{a-b} < \phi_{\mu} \mid r_{in}^{-1} (r_{in}^2 \delta_{ij} - 3 r_{in,i} r_{in,j}) \mid \phi_{\nu} >
$$

(2.50)

where $\rho_{\mu,\nu}^{a-b}$ is an element of the spin density matrix.
2.11.3 Electron Spin Resonance

The hyperfine coupling constant is an observable in an applied magnetic field \( B \). The interactions between the magnetic field and the electronic and nuclear magnetic moments, together with the hyperfine interaction, contribute to the spin Hamiltonian

\[
\hat{H}_{\text{spin}} = g_e \beta_e B \cdot \hat{S} - g_N \beta_N B \cdot \hat{I} + \hat{I} \cdot A \cdot \hat{S}
\] (2.51)

The first two terms in (2.51) represent the electronic and nuclear Zeeman interactions, respectively. Using the hydrogen atom in an applied magnetic field as an example, the energy splittings arising from the three terms in the spin Hamiltonian are shown schematically in Figure 2.3.

![Schematic diagram](image)

**Figure 2.3** Schematic illustration of the splittings arising from various terms in the spin Hamiltonian for a hydrogen atom (\( \alpha_e, \beta_e \) and \( \alpha_N, \beta_N \) are the electronic and nuclear spin wave functions, respectively).
The spherical distribution of the unpaired electron of the H atom or the free tumbling of a radical in solution can average out the anisotopic components of the hyperfine couplings. The eigenvalues of the spin Hamiltonian for each spin state \( m_s M_i \) are given by

\[
E_{m_s M_i} = g_e \beta_e B_z m_s - g_N \beta_N B_z M_i + m_s M_i A_{iso}
\]

where \( m_s \) and \( M_i \) are the eigenvalues of \( \hat{S}_z \) and \( \hat{I}_z \), respectively, and \( Z \) is the direction of the applied magnetic field.

By applying another oscillating magnetic field perpendicular to the first static field, the \( \Delta m_s = \pm 1 \) and \( \Delta M_i = 0 \) of the selection rule allows transitions to be induced at two resonance frequencies

\[
h \nu_{M_i} = g_e \beta_e B_z + m_s M_i A_{iso} \quad M_i = \pm \frac{1}{2}.
\]

This is the technique of electron spin resonance (ESR) by which the magnitude of the \( A_{iso} \) is measured as the absolute difference between the two resonance frequencies. However, the sign of the hyperfine coupling constants cannot be determined from ESR spectra. For the detection of a very small hyperfine coupling, the related technique of electron-nuclear magnetic double resonance (ENDOR) is more powerful. Similar to ESR transitions, ENDOR transitions are nuclear magnetic resonance transitions induced by applying an oscillating field, but at different frequencies. Using the above \( S = \frac{1}{2} \) and \( I = \frac{1}{2} \) system as an example, the selection rule of \( \Delta M_i = \pm 1 \) and \( \Delta m_s = 0 \) allows two nuclear magnetic resonances to be induced at

\[
h \nu_{m_s} = -g_N \beta_N B_z + m_s M_i A_{iso}, \quad m_s = \pm \frac{1}{2}.
\]
Analogous to ESR, ENDOR measures the $A_{\text{iso}}$ as the difference of the two frequencies of nuclear magnetic resonance.

For radicals with $N$ magnetic nuclei, the hyperfine interaction Hamiltonian is given by

$$\hat{H}_{hf} = \sum_{i=1}^{N} I_i \cdot A_i \cdot \hat{S}$$  \hspace{1cm} (2.55)

where the sum extends over all magnetic nuclei. As the number of coupled nuclei increases, ESR spectra become more complex. For complex spectra, ENDOR has the advantage of discriminating the hyperfine coupling constants arising from different magnetic nuclei in different radiofrequency ranges.

In the solid state, where a particular conformation of a radical is constrained, ESR or ENDOR spectra may provide both the isotropic and anisotropic hyperfine coupling constants for a given magnetic nucleus. This is extremely useful when trying to identify a radical species. However, solid-state ESR spectra are often complex with many overlapping lines and extremely difficult to interpret.

### 2.11.4 Performance of Theory for Calculating Hyperfine Interactions

Isotropic hyperfine coupling constants are related to the spin density at the nucleus. From a theoretical point of view, the origin of the spin density at a nucleus plays a key role in understanding the mechanisms of hyperfine coupling.

Sources of spin density have been traced\textsuperscript{48} from the simplest ROHF method in which net contribution to spin density comes only from the singly occupied molecular
orbital being considered as the zero-order contribution. In comparison, in the UHF formalism, each pair of electrons in a doubly occupied molecular orbital \( \psi_i \alpha(j) \psi_i \beta(k) \) is separately relaxed resulting in a configuration \( \psi_i \alpha(j) \psi_i \beta(k) \) in which the spatial orbital \( \psi_i \) differs slightly from \( \psi_i' \). As a consequence, electron \( k \) of \( \beta \) spin is more likely to be polarized towards the unpaired electron than electron \( j \) of \( \alpha \) spin. This phenomenon is known as spin polarization. The difference between the UHF and ROHF spin densities is considered as a first-order contribution. Higher-order contributions are due mainly to electron correlation effects. Although the weight of each contribution may vary for different radical species, a general trend can be easily seen by the performance of various levels of theory using the CH radical as an example (Table 2.1).^47^48

<table>
<thead>
<tr>
<th>Method</th>
<th>(^1\text{H}^\text{C} )</th>
<th>(^1\text{H}^\text{H} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>ROHF</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>UHF</td>
<td>100.4</td>
<td>-84.4</td>
</tr>
<tr>
<td>MP2</td>
<td>37.4</td>
<td>-31.4</td>
</tr>
<tr>
<td>MP3</td>
<td>31.4</td>
<td>-58.0</td>
</tr>
<tr>
<td>MP4</td>
<td>35.0</td>
<td>-57.6</td>
</tr>
<tr>
<td>CIS</td>
<td>41.4</td>
<td>-57.1</td>
</tr>
<tr>
<td>CISD</td>
<td>30.0</td>
<td>-51.8</td>
</tr>
<tr>
<td>CISDT</td>
<td>45.8</td>
<td>-58.0</td>
</tr>
<tr>
<td>QCISD</td>
<td>43.7</td>
<td>-58.5</td>
</tr>
<tr>
<td>QCISD(T)</td>
<td>42.1</td>
<td>-57.2</td>
</tr>
<tr>
<td>MRCI</td>
<td>45.8</td>
<td>-58.5</td>
</tr>
<tr>
<td>exptl</td>
<td>46.8 ± 2.8</td>
<td>-57.7 ± 0.3</td>
</tr>
</tbody>
</table>

The results suggest that the erroneous behaviour of both the ROHF and UHF methods arises from neglect of higher order corrections, while the good agreement with experiment using the CIS method is due to cancellation of errors. Essentially, the
Theoretical Background

inclusion of single, double and triple excitations at the CISDT, MRCI or QCI levels of theory is necessary for obtaining accurate spin densities at the nuclei for isotropic hyperfine coupling constants. The performance of the theory is consistent with the fact that the probability of the unpaired electron appearing at a nucleus is physically associated with electron correlation.

As discussed previously, DFT methods may effectively include the electron correlation required for the calculation of hyperfine coupling constants. However, various combinations of the exchange functionals and correlation functionals may behave differently in obtaining the spin density. Because the spin density is insufficiently localized in LSDA, the resulting isotropic hyperfine couplings are often highly erroneous. The improvement from LSDA to GGA functionals mainly occurs for the heavy atoms for which the gradient corrections remove excess density from the tails of the core and the valence regions and place it in the core region of the atoms. Thus, GGA functions provide more reliable isotropic hyperfine couplings. In particular, extensive assessment\textsuperscript{47,49} shows that the B3LYP and PWP86 functionals provide the most accurate hyperfine couplings so far. The relative accuracy of various DFT methods and QCISD for the hydroxyl radical is shown in Table 2.2.\textsuperscript{50a-c}

<table>
<thead>
<tr>
<th>Method</th>
<th>SVWN\textsuperscript{a}</th>
<th>PWP86\textsuperscript{a}</th>
<th>B3LYP\textsuperscript{a}</th>
<th>QCISD\textsuperscript{b}</th>
<th>Exptl</th>
</tr>
</thead>
<tbody>
<tr>
<td>$^{17}$O</td>
<td>-1.0</td>
<td>-17.5</td>
<td>-15.6</td>
<td>-17.3</td>
<td>-18.3</td>
</tr>
<tr>
<td>$^1$H</td>
<td>-21.4</td>
<td>-20.8</td>
<td>-22.1</td>
<td>-26.6</td>
<td>-26.2</td>
</tr>
</tbody>
</table>

\textsuperscript{a} with IGLO-III. \textsuperscript{b} with 6-311G+(2df,p).
Clearly, the PWP86 and B3LYP methods exhibit accuracy comparable with high-level conventional correlated methods.

The anisotropic hyperfine coupling components are integrated over all space rather than at only one point of the nucleus, thus, they are less sensitive to the quality of the method employed. At a level of theory that is suitable for the calculation of accurate isotropic hyperfine coupling, accurate anisotropic hyperfine coupling constants can certainly be obtained.

2.11.5 Basis Set Considerations for HFCC Calculations

The accurate description of the spin density at the nucleus for the isotropic hyperfine coupling constant demands high quality basis sets to be used at a suitable level of theory. Due to the deficiency of Gaussian functions not satisfying the cusp condition, a well-chosen basis set has to be used to obtain a good description of the core region. In particular, many s-functions and appropriate polarization functions must be included. In some cases, inclusion of diffuse functions may further improve the results. To meet these complicated requirements, basis sets of triple-zeta quality or better must be used to obtain accurate hyperfine coupling constants.

2.12 General Summary

The Hartree-Fock method is the simplest \textit{ab initio} model that can be employed for studying chemical problems. The basis set used may be adjusted to obtain an improved
description of the molecular orbitals. The Hartree-Fock limit represents the best that can be done with a single electron configuration. The major deficiency of Hartree-Fock theory is its incomplete description of the correlation between the motions of the electrons.

Quantitative predictions often require going beyond the Hartree-Fock level. The conventional electron-correlation methods and the density functional theory are the two main approaches for incorporation of the effects of electron correlation.

A hierarchy of the conventional electron-correlation methods is best illustrated by a Pople diagram, such as shown in Figure 2.4. Following the hierarchy, the exact solution of the non-relativistic Schrödinger equation may be approached in a systematic manner. Such methods may be highly accurate, however, computationally they are often too expensive.

<table>
<thead>
<tr>
<th>HF</th>
<th>MP2</th>
<th>...</th>
<th>CISD</th>
<th>...</th>
<th>QCI</th>
<th>...</th>
<th>Full CI</th>
</tr>
</thead>
<tbody>
<tr>
<td>6-31G(d)</td>
<td>:</td>
<td>:</td>
<td>:</td>
<td>:</td>
<td>:</td>
<td>:</td>
<td>Increasing basis set size</td>
</tr>
<tr>
<td>6-31G(d,p)</td>
<td>:</td>
<td>:</td>
<td>:</td>
<td>:</td>
<td>:</td>
<td>:</td>
<td>Exact solution</td>
</tr>
<tr>
<td>6-31+G(d,p)</td>
<td>:</td>
<td>:</td>
<td>:</td>
<td>:</td>
<td>:</td>
<td>:</td>
<td></td>
</tr>
</tbody>
</table>
It is not possible to construct a similar hierarchical diagram for the DFT methods. The accuracy of density functional theory methods depends on the density functional and also on the basis set used. Functionals, such as B3LYP, that have achieved chemical accuracy with some exceptions, are often the best choice for practical applications. Such methods are computationally less expensive than conventional electron correlation methods, being comparable in cost to Hartree-Fock level calculations. One more feature of the well-behaved DFT methods, such as B3LYP, is that they have been shown to often be less dependent on the size of the basis sets.

The level of theory being employed in a study is conventionally denoted as: method/basis set, e.g., B3LYP/6-31+G(d,p).

2.13 Practical Computational Scheme

Predicting electronic properties begins by searching for the optimal geometry of a molecular system. The reliability of any prediction depends on the quality of the optimized geometry. The molecular geometry depends only on the first derivatives of energy; reasonably accurate geometries can often be obtained at quite modest levels of theory. However, properties such as hyperfine coupling constants and the total energy of a radical species may only converge at a very high level of theory. Thus, single point calculations using more accurate methods with a larger basis set using a geometry obtained at a lower level of theory is often a sensible combination. This technique has been applied in this thesis to reduce computational cost, while maintaining reliable accuracy.
In such a combined computational scheme, the approach taken is conventionally written as

higher level (single point calculation)/lower level (geometry)

2.14 Technical Aspects

The calculations reported in this thesis were performed on IBM RS/6000 workstations in the Department of Chemistry, Dalhousie University and on the IBM SP parallel supercomputer of Dalhousie University. The Gaussian 94\textsuperscript{41a} and Gaussian 98\textsuperscript{41b} suites of programs were used for the geometry optimization and for obtaining the relative energies. The deMon programs\textsuperscript{51} was used for calculating the hyperfine coupling constants.

In this thesis, the quantities reported are in the following units:

<table>
<thead>
<tr>
<th>Property</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative energy</td>
<td>kJ mol\textsuperscript{-1}</td>
</tr>
<tr>
<td>Hyperfine coupling constant</td>
<td>MHz</td>
</tr>
<tr>
<td>Bond length</td>
<td>angstrom (Å)</td>
</tr>
<tr>
<td>Angle</td>
<td>degree</td>
</tr>
</tbody>
</table>

The following conversion factors were used:

1 hartree (a.u.) = 2625.5 kJ mol\textsuperscript{-1}

1 gauss = 2.8025 MHz.
References


M.; Replogle, E. S.; Pople, J. A. GAUSSIAN 98; Gaussian, Inc.: Pittsburgh, PA, 1998.


Radiation Products of Glycine

3.1 Introduction

Recently, there has been a dramatic increase in interest in the functionality of protein radicals.\textsuperscript{1} However, elucidating the reaction mechanisms of radical-containing proteins, or understanding radiation damage to a protein, requires a detailed knowledge of the chemistry and properties of amino acid radicals. Glycine, the simplest amino acid, is often used as an experimental model system\textsuperscript{2-13} in studies of oxidation and reduction reactions of irradiated amino acids.

In 1964, after some years of controversy, Morton\textsuperscript{12} tentatively proposed that the end oxidation and reduction products of glycine were $^+\text{NH}_3\text{C}^\bullet\text{HCOO}^-$ (R1) and $^\bullet\text{CH}_2\text{COO}^-$ (R2'), respectively. It was later shown\textsuperscript{8b} that the species observed was $^\bullet\text{CH}_2\text{COOH}$ (R2) rather than the radical anion $^\bullet\text{CH}_2\text{COO}^-$. In 1997, Brustolon et al.\textsuperscript{4} assigned three newly observed hyperfine coupling tensors to radical $\text{NH}_2\text{C}^\bullet\text{H}_2$. In 1998, Sanderud et al.\textsuperscript{3} showed this to be incorrect, and proposed that the radical was $\text{NH}_2\text{C}^\bullet\text{HCOOH}$ (R3). In addition, they assigned three more observed hyperfine couplings to another conformer of $\text{NH}_2\text{C}^\bullet\text{HCOOH}$. The two experimentally observed
conformers of NH$_2$C$^\bullet$HCOOH are denoted hereafter as R3$^\bullet$ and R3$^\bullet$. In the paper of Sanderud et al.,$^2$ they correspond to Radical IV and Radical III, respectively. The H$_\alpha$ isotropic hyperfine coupling constants (HFCCs) of R3$^\bullet$ (−30.15 MHz) and R3$^\bullet$ (−24.62 MHz) differ significantly. Based on the McConnell relation$^{14}$ and the Gordy-Bernhard$^{15}$ method, the smaller absolute isotropic HFCC in the proposed R3$^\bullet$ was ascribed to non-planarity of the radical centre in the glycine crystal. Furthermore, experimental data$^2$ was used to suggest a twist angle of 24.2$^\circ$ between the OCO and CCN planes in R3$^\bullet$. This is an example where experimental studies can only provide indirect information about the distortion of a radical in a specific environment. The assignment of complicated ESR spectra often requires simulations based on several assumptions. Hence, theoretical calculations of the HFCCs of amino acid radiation products can provide valuable assistance. The present study shows that correct identification of some radiation products of glycine-derived radicals can only be achieved through comparison of experimental and theoretical results. The glycine-derived radicals observed in irradiated glycine crystals at 280 K are shown in Figure 3.1.

In the gas phase chemistry of amino acids, extensive calculations of thermochemical properties have been performed on glycine-derived radicals by Yu et al.$^{16}$ The ESR features of the glycine radical, H$_2$NC$^\bullet$HCOOH, have been studied previously at various levels of theory.$^{17,18}$ However, amino acids exist as zwitterionic
species in the crystalline state and in solution. When irradiated, radicals in a zwitterionic form (such as R1 in Figure 3.1) can be formed. The zwitterionic structure of amino acids and their derived radicals has been a challenge for theoretical chemistry. *Ab initio* calculations on glycine$^{19}$ and its radical$^{20,21}$ have shown that their zwitterionic structures do not correspond to energy minima in the gas phase. Thus, environmental effects must be included for exploring the zwitterionic form of amino acids.

![Figure 3.1 Schematic illustration of structure of glycine and related radicals generated upon X-ray irradiation of glycine crystals.](image)

There are two strategies to account for environmental effects. One is to build a model by adding discrete molecules around the target molecule. The second strategy is the self-consistent reaction field, the SCRF approach (see Chapter 2). Environmental effects on the structure of R1 have previously been considered by performing a constrained geometry optimization$^{20}$ or by use of the conductor-like polarizable continuum model (CPCM).$^{21}$ Previously, calculations$^{21}$ on the isolated structure of R1 have shown that the isotropic HFCCs are not significantly influenced by the crystalline
environment. In addition, it has been shown\textsuperscript{22} that the Onsager model, using the dielectric constant of water, yields the zwitterionic structure of the alanine radical \( ^{+}\text{NH}_3\text{C}^\text{\`}{\text{H}}_2\text{COO}^- \) and that the resulting HFCCs are in good agreement with experiments.

Density functional theory has been shown to yield very accurate hyperfine coupling constants with great computational advantages\textsuperscript{21,24}. Extensive DFT studies on the radicals formed in irradiated DNA bases and the sugar moiety have shown the success of DFT for biological systems\textsuperscript{25}. In particular, promising DFT results on the alanine radical system\textsuperscript{22,26} have prompted the present systematic study\textsuperscript{27} on glycine-derived radical species in order to obtain greater insight into the properties of irradiated amino acids.

### 3.2 Computational Methods

All geometry optimizations were performed with the B3LYP hybrid density functional (see Chapter 2) in conjunction with the 6-31+G(d,p) basis set using the Gaussian 98 suite of programs.

As noted previously, in solution and in the crystalline state, glycine is in its zwitterionic form, i.e., \( ^{+}\text{NH}_3\text{CH}_2\text{COO}^- \). At the above level of theory, it is not computationally feasible to explicitly include the effects of the crystalline environment. However, one is able to obtain zwitterionic structures of glycine radicals using the standard Onsager model with a dielectric constant for water of 78.39. This approach, as
noted in the Introduction, has been successfully used previously for alanine-derived radicals.\textsuperscript{22}

All stationary points were confirmed to be local minima by harmonic vibrational frequency calculations at the same level of theory. Relative energies of all conformers of R2, R3 and R4 were obtained by performing single point calculations at the B3LYP level in conjunction with the 6-311G(2df,p) basis set using the above optimized geometries and with inclusion of the appropriate zero-point vibrational energy correction\textsuperscript{28} i.e., B3LYP/6-311G(2df,p)/B3LYP/6-31+G(d,p) + ZPVE.

Isotropic and anisotropic hyperfine coupling constant calculations were performed using the deMon program. The PWP86 functional, a combination of Perdew and Wang's exchange functional (PW)\textsuperscript{29} and Perdew's nonlocal correlation functional (P86),\textsuperscript{30} in conjunction with the 6-311G(2d,p) basis set was employed. The (5,4;5,4) family of auxiliary basis sets was used to fit the charge density and the exchange correlation potential. This functional and basis set combination has been shown to give accurate hyperfine coupling constants in studies of alanine,\textsuperscript{22} histidine\textsuperscript{31} and model π-radicals.\textsuperscript{32}

The assessments of methods for accurate calculation of hyperfine coupling constants have been discussed in Chapter 2. However, it should be noted that satisfactory anisotropic HFCCs can definitely be obtained at the present level of theory provided the structure is qualitatively correct, and that comparison of anisotropic hyperfine tensors can be used as a reliable guide to identify radicals when less satisfactory agreement is obtained for the isotropic coupling constants.
3.3 Results and Discussion

The optimized geometries of R1, R2, R3 and R4 are shown schematically in Figure 3.2, while those of experimentally proposed radicals R4' ($^{+}\text{NH}_3\text{CH}_2\text{COC}^+\text{HCOO}^-$) and R2' ($^\text{*}\text{CH}_2\text{COO}^-$) are shown schematically in Figure 3.3.

Figure 3.2 Optimized structures of R1, R2, R3, and R4 (continued over page).
Figure 3.2 Optimized structures of R1, R2, R3, and R4.
3.3.1 Geometry and Hyperfine Couplings of $^{+}\text{NH}_3\text{C}^+\text{HCOO}^-$

The optimized zwitterionic structure of R1 (Figure 3.2) was obtained using the Onsager model with an estimated radius of 3.24 Å. It possesses $C_s$ symmetry having a planar radical centre. Thus, R1 is a typical $\pi$-radical. The computed full hyperfine tensors of R1, as well as the experimental values and other previously calculated values, are listed in Table 3.1. The $H_\alpha$ isotropic HFCC is in good agreement with the experimental value. Similarly, the anisotropic components agree well with the experimental values, although the sign of $T_{xy}$ differs from $T_{xy}^{\text{exp}}$ due to its small value. In addition, comparison of the calculated ($-95.0, -60.4, -21.5$) and the experimental ($-97.5, -61.9, -31.8$) principal components shows that only the $A_{zz}$ component is difficult to reproduce.
Table 3.1: PWP86/6-311G(2d,p) calculated and experimental HFCCs (MHz) of R1.

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<th>$T_{yy}$</th>
<th>$T_{zz}$</th>
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</tr>
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</tr>
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<td>-4.57</td>
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<td>1.71$^d$</td>
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$^a$Ref 2. $^b$Ref 11. $^c$Ref 12. $^d$Ref 10. $^e$Ref 21 (B3LYP/EPR-2 calculated values).

The anisotropic components of the hyperfine tensors of the three amino hydrogens ($H_1$, $H_2$ and $H_3$) are in good agreement with the experimental values. The isotropic HFCCs of $H_1$, $H_2$ and $H_3$ are of similar magnitude as experimental values with the largest differences of 14.15 and 5.99 MHz being observed for $H_2$ and $H_3$, respectively. The isotropic HFCC and anisotropic components of the nitrogen are in good agreement with the experimental values. It can be seen that the calculated $C_a$ HFCC at the PWP86/6-311(2d,p) level is in fair agreement with the experimental value and slightly better than a previous B3LYP/EPR-2 calculated value. The B3LYP/EPR-2 study has shown that the deviation of $C_a$ HFCC based on the optimized zwitterionic structure can be significantly corrected by including the effect of vibrational averaging. The HFCCs of $H_a$ and N, however, are not sensitive to vibrational averaging. Experimentally the sign of the N hyperfine coupling has not been determined, however, it has been suggested to be negative. This is supported by previous theoretical studies and by the present results. In addition, an investigation for the analogous alanine radical, $^{+}\text{NH}_3\text{C}^+\text{CH}_3\text{COO}^-$, obtained a negative sign for the N HFCC.
The average (52.15 MHz) of the isotropic HFCCs of the three amino protons is in good agreement with the experimentally observed value of 49.07 MHz at 280 K, suggesting that the amino group rotates freely at 280 K. Furthermore, it also suggests that at 100 K the orientation of the amino group in glycine crystals is constrained, giving rise to the three specific HFCC tensors of amino protons. Therefore, a detailed investigation was undertaken on the effects on the isotropic HFCCs of H₁, H₂, H₃, Hₐ, Cₐ and N of rotating the amino group about the N—Cₐ bond of R₁. The variation of the isotropic HFCCs as a function of the rotational angle is shown in Figure 3.4. The rotation of the amino group was carried out by incrementally increasing the dihedral angle $\angle H₁NCₐC₁$ by 30°, starting from $\angle H₁NCₐC₁ = 0°$. From Figure 3.4 it can be seen that the isotropic HFCCs of H₁, H₂ and H₃ change dramatically, similar to that observed in the zwitterionic radical of alanine. However, the isotropic couplings of Hₐ, Cₐ and N are almost constant. It is noted that the difference in amplitude of the variation of the HFCC of H₁ and those of H₂ and H₃ is due to the fact that the geometrical parameters of the amino group have been constrained during rotation.

When the amino group is rotated by approximately 5°, the isotropic HFCCs of H₂ and H₃ are in good agreement with the experimental values 62.91 and 83.05 MHz at 100 K, while the isotropic HFCC of H₁ is still less than 5 MHz. These results support the fact that only the hyperfine splittings of two of the three constrained amino protons are easily observed; while the third remains too small to be distinguished from the many lines observed in the ENDOR spectra. Thus, from the HFCC calculations for the isolated R₁ it
can be concluded that the crystalline environment has little direct effect on the ESR spectra of R1, similar to the conclusion of a previous study.\textsuperscript{21}

![Graph](image)

Figure 3.4 Variation of H\textalpha{}, H\textsubscript{1}, H\textsubscript{2}, H\textsubscript{3}, C\textalpha{}, and N isotropic HFCCs with rotational angle of the amino group of R1.

### 3.3.2 Geometry and Hyperfine Couplings of \textsuperscript{•}CH\textsubscript{2}COOH

In 1964, Morton\textsuperscript{12} concluded that the second radical observed in irradiated glycine crystals was the radical anion \textsuperscript{•}CH\textsubscript{2}COO\textsuperscript{−} (R2' in Figure 3.3) with only one H\textalpha{} hyperfine coupling due to two equivalent hydrogens. However, Teslenko et al.\textsuperscript{8b} reported that two forms of \textsuperscript{•}CH\textsubscript{2}COOH (R2 in Figure 3.2) were observed; one at 77 K, the other at 140 K. Three inequivalent hyperfine couplings were observed for the conformer at 77 K, while two were observed for the conformer at 140 K. Recently, similar hyperfine structures were observed\textsuperscript{2} at 100 K with the ambiguous conclusion that the radical may be either \textsuperscript{•}CH\textsubscript{2}COO\textsuperscript{−} or \textsuperscript{•}CH\textsubscript{2}COOH. To clarify this ambiguity, calculations were performed on
both species. The optimized structures of R2 and R2′ are shown in Figures 3.2 and 3.3, respectively. Two conformers of CH₂COOH, R2-I and R2-II (Figure 3.2), were found. R2-I is almost planar, while R2-II is planar. Due to the existence of intramolecular hydrogen bonding R2-II lies 23.4 kJ mol⁻¹ lower in energy than R2-I (see Table 3.2). Interestingly, it was found that R2' is not planar, both oxygen atoms lie out of the H₁C₁H₂ plane. However, R2' was found to possess C₂ symmetry with a planar radical centre.

<table>
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<th>R2′</th>
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<tr>
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</tr>
<tr>
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Table 3.2: PWP86/6-311G(2d,p) calculated and experimental⁴ HFCCs (MHz) of R2-I, R2-II and R2′, and calculated⁵ relative energies (kJ mol⁻¹) of R2-I and R2-II.

³Ref 8b. ⁴B3LYP/6-311G(2d,p)//B3LYP/6-31+G(d,p) + ZPVE.

The calculated and experimental hydrogen HFCC tensors of R2', R2-I and R2-II are listed in Table 3.2. For R2, the isotropic HFCCs and anisotropic components of H₁ and H₂ in R2-I are closest to the experimental values⁸ of the conformer observed at 140 K, while the isotropic HFCCs and anisotropic components of H₁ and H₂ in R2-II are in closest agreement with the experimental values⁸ of the conformer observed at 77 K.
(Table 3.2). The isotropic coupling and anisotropic components of \( H_x \) in both R2-I and R2-II are in reasonable agreement with the experimental values for the conformer observed at 77 K. In the case of R2', the anisotropic components of \( H_1 \) and \( H_2 \) of R2' are in good agreement with the experimental values of both observed conformations. However, the isotropic HFCCs of \( H_1 \) and \( H_2 \) of R2' differ significantly from the experimental HFCCs of both conformers at 77 K and 140 K. Thus, it can be concluded that neither of the conformations observed at 77 K and 140 K is R2', but instead are either R2-I or R2-II. However, as the calculated \( H_1 \) and \( H_2 \) hyperfine tensors of R2-I and R2-II are too close to be definitively assigned, more elaborate theoretical studies incorporating specific crystal and temperature effects, beyond the scope of the present study, will be required in order to make more definitive assignments.

3.3.3 Geometry and Hyperfine Couplings of \( \text{NH}_2\text{C}^*\text{HCOOH} \)

The four optimized conformers of \( \text{NH}_2\text{C}^*\text{HCOOH} \) (denoted as R3-I, R3-II, R3-III and R3-IV) are shown in Figure 3.2. The backbones of R3-II, R3-III and R3-IV are almost planar with all hydrogen atoms close to the \( \text{C}_1\text{C}_\alpha\text{N} \) plane. Due to the significant repulsion between \( H_x \) and \( H_1 \), R3-I is more distorted with the two oxygen atoms being out of the \( \text{C}_1\text{C}_\alpha\text{N} \) plane by more than 7.7°, while \( H_1 \) is distorted out of the \( \text{C}_1\text{C}_\alpha\text{N} \) plane by 36.3°. Accordingly, the radical centres in R3-II, R3-III and R3-IV are less pyramidal than in R3-I. The relative energies in Table 3.3 show that R3-II and R3-III, with intramolecular hydrogen bonding, are more stable than R3-I and R3-IV.
The computed HFCC tensors in R3-I, R3-II, R3-III and R3-IV and the experimental HFCC tensors of R3$^a$ and R3$^*$ are listed in Table 3.3. It is noted that the calculated isotropic HFCCs (-17.01 and -14.27 MHz) of the amino protons of R3-II differ significantly from previously calculated values (10.12 and -4.82 MHz). This difference is most probably due to differences in the DFT optimized geometries used for the HFCC calculations. The optimized geometry obtained as part of this study is in closer agreement with higher-level ab initio calculations, suggesting that the presently calculated HFCCs should be more reliable.

Table 3.3: PWP86/6-311G(2d,p) calculated HFCCs (MHz) of R3-I, R3-II, R3-III, R3-IV and the experimental$^a$ values of R3$^a$ and R3$^*$ and calculated$^b$ relative energies (kJ mol$^{-1}$) of R3-I, R3-II, R3-III and R3-IV

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<th>R3-III</th>
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<td>5.8</td>
<td>23.4</td>
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</tbody>
</table>

$^a$Ref 2. $^b$B3LYP/6-311G(2df,p)//B3LYP/6-31+G(d,p) + ZPVE.

From careful comparison of the calculated HFCCs for the four conformers of R3, they can be divided into two groups, with R3-I in one group and the rest in a second group. The isotropic HFCCs of $H_x$ in R3-II, R3-III and R3-IV are all in similar
agreement with the experimental value of $R_3^\#$ differing by 6-8 MHz, however, they differ significantly from the experimental value of $R_3^\ast$ by at least 12 MHz. The anisotropic components of the $H_\alpha$ HFCC tensor for the above conformers are in similar agreement with the experimental values of both $R_3^\#$ and $R_3^\ast$. Except for the isotropic HFCC of $H_2$ in $R_3$-IV, the isotropic HFCCs and anisotropic components of the two amino protons of $R_3$-II, $R_3$-III and $R_3$-IV are in good agreement with the corresponding experimental values of both $R_3^\#$ and $R_3^\ast$, which are themselves very similar. Larger deviations were found between the calculated isotropic and anisotropic HFCCs of $H_\alpha$ and the experimental values of $R_3^\#$ or $R_3^\ast$ in $R_3$-I than in $R_3$-II to $R_3$-IV. It was found that the computed amino-proton isotropic $H_1$ HFCCs (25.03 MHz) in $R_3$-I and the experimental values $R_3^\#$ and $R_3^\ast$ ($-18.05$ and $-16.87$ MHz, respectively) are of the same magnitude, however, their signs are opposite. In addition, the anisotropic components of $H_1$ in $R_3$-I are in poorer agreement with the experimental values than those of $H_1$ in the second group. Thus, $R_3$-I is neither $R_3^\#$ nor $R_3^\ast$. Although the above calculations using gas-phase optimized structures of $R_3$ could not distinguish between $R_3^\#$ and $R_3^\ast$, $R_3^\#$ is concluded to be one conformer or a mixture of $R_3$-II, $R_3$-III and $R_3$-IV. This is supported by the fact that $R_3$-I is at least 20 kJ mol$^{-1}$ higher in energy than the other three conformers of $R_3$.

The calculated $H_\alpha$ isotropic HFCCs of $R_3$-II, $R_3$-III and $R_3$-IV are in closer agreement with the experimental isotropic HFCC (33.0 MHz) of $R_3$ in solution$^9$ than in the crystal.$^2$ Hence, the deviation of the calculated $H_\alpha$ isotropic HFCCs of $R_3$-II to $R_3$-
IV from the experimental values of R3" is likely due to crystal-packing effects, which are not taken into account by the above calculation.

An experimentally suggested twist angle of 24.2° between the NC\(_{\alpha}\)C\(_1\) and O\(_1\)C\(_1\)O\(_2\) planes in R3° implies that the two amino protons and the two carboxylic oxygens are constrained by intermolecular hydrogen bonding. The effect of the two-plane twist on the H\(_{\alpha}\), H\(_1\) and H\(_2\) HFCCs of R3" was investigated by re-optimizing only H\(_{\alpha}\) related geometrical parameters, i.e., H\(_{\alpha}\)—C\(_\alpha\), \(\angle H_{\alpha}C_{\alpha}C_1\), and \(\angle H_{\alpha}C_\alpha C_1N\) in R3-II, R3-III and R3-IV. The twisting of the NC\(_{\alpha}\)C\(_1\) plane with respect to the O\(_1\)C\(_1\)O\(_2\) plane was carried out by incrementally increasing the absolute value of \(\angle O_2C_1C_\alpha N\) by 10° from 0°. The variation of the isotropic HFCCs of H\(_{\alpha}\), H\(_1\) and H\(_2\) with respect to the twist angle is shown in Figure 3.5.

It can be seen that the three plots exhibit the same pattern. The absolute isotropic HFCC of H\(_{\alpha}\) decreases as the twist angle increases in R3-II, R3-III and R3-IV. The isotropic HFCC of one amino proton (H\(_1\)) increases as the isotropic HFCC of the other amino proton (H\(_2\)) decreases in R3-II, R3-III and R3-IV. As the isotropic HFCCs of H\(_1\) and H\(_2\) become equal (see Figure 3.5), the average (\(H_{1,2}^{\text{ave}}\)) of the isotropic HFCCs of H\(_1\) and H\(_2\) decreases slightly. However, the H\(_{1,2}^{\text{ave}}\) values are all very close to the average of the experimental H\(_1\) and H\(_2\) isotropic couplings in R3° (16.16 MHz). It should be noted that by varying the twist angle, one is able to produce changes in the calculated H\(_{\alpha}\) and H\(_{1,2}^{\text{ave}}\) HFCCs similar to the experimentally observed differences between R3" and R3° (see Table 3.3). Thus, although the calculations are unable to determine the conformation
of R3\(^\circ\), it does support the experimental conclusion that R3\(^\circ\) is only a twisted configuration of R3\(^a\) fixed by intermolecular hydrogen bonding in glycine crystals.

![Graph](image.png)

Figure 3.5 Variation of H\(_1\), H\(_2\), and H\(_{1,2}\)\(^{ave}\) isotropic HFCCs in (a) R3-II, (b) R3-III and (c) R3-IV with the twist angle \(\angle O_2C_1C_\alpha N\) (continued over page).
Figure 3.5 Variation of $H_a$, $H_1$, $H_2$, and $H_{12}$ isotropic HFCCs in (a) R3-II, (b) R3-III and (c) R3-IV with the twist angle $\angle O_2 C_1 C_a N$.

3.3.4 Protonation Effects on the Hyperfine Couplings in $\text{NH}_2C^+\text{HCOOH}$

To complete the theoretical studies of $R3^+$ and $R3^-$, the corresponding protonated radical cation $\text{NH}_2C^+\text{HCO}(\text{OH})_2^+$ ($R3^p$) was investigated. Optimized structures for conformers of $R3^p$ are shown in Figure 3.6. In $R3^p$-I and $R3^p$-III, the protonated carboxylic group is distorted slightly due to the repulsion between $H_1$ and $H_{e2}$, however, the radical centres are almost planar. $R3^p$-II is planar. In $R3^p$-IV, while the two oxygen atoms are distorted out of the $C_1 C_a N$ plane slightly by 2.7°, the rest including the radical centre $C_a$ remains planar. Comparison of the geometries of $R3^p$ with $R3$ suggests that protonation of $R3$ tends to make both the $C_a$ and $N$ centres more planar. However, the
repulsion between H₁ and H₂₂ for a specific orientation can distort the planarity slightly. From the relative energies listed in Table 3.4 it can be seen that R₃ᵢ⁻ is the most stable conformer.

The computed hyperfine coupling tensors in R₃ᵢ⁻, R₃ᵢ⁻, R₃ᵢ⁻ and R₃ᵢ⁻ are shown in Table 3.4. The isotropic HFCC and anisotropic components of Hα in each conformer are in agreement with the corresponding experimental values of R₃⁺. However, the isotropic HFCCs of the two amino protons in R₃ᵢ⁻, R₃ᵢ⁻, R₃ᵢ⁻ and R₃ᵢ⁻ are slightly larger than the experimental isotropic HFCCs. Interestingly, the anisotropic components of the two amino protons in each conformer are in good agreement with the experimental values of R₃⁺. The calculations suggest that to exclude the possibility that R₃ᵢ is R₃⁺, experimental studies of the carboxylic proton are required.

![Figure 3.6 Optimized structures of R₃ᵢ.](image-url)
Table 3.4: PWP86/6-311G(2d,p) calculated HFCCs (MHz) of R3<sup>p</sup> and experimental<sup>a</sup> values of R3<sup>+</sup> and calculated<sup>b</sup> relative energies (kJ mol<sup>-1</sup>) of R3<sup>p</sup>-I, R3<sup>p</sup>-II, R3<sup>p</sup>-III and R3<sup>p</sup>-IV.

<table>
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<tr>
<th>tensor</th>
<th>HFCC</th>
<th>R3&lt;sup&gt;p&lt;/sup&gt;-I</th>
<th>R3&lt;sup&gt;p&lt;/sup&gt;-II</th>
<th>R3&lt;sup&gt;p&lt;/sup&gt;-III</th>
<th>R3&lt;sup&gt;p&lt;/sup&gt;-IV</th>
<th>R3&lt;sup&gt;+&lt;/sup&gt;</th>
<th>exptl</th>
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<td>38.2</td>
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</table>

<sup>a</sup>Ref 2.  <sup>b</sup>B3LYP/6-311G(2d,p)//B3LYP/6-31+G(d,p) + ZPVE.

### 3.3.5 Enhanced Captodative Effects from Protonation

It was postulated that the complementary electron withdrawing (capto) and electron-donating (dative) effect in R3 will enhance its stabilization by delocalization of spin density and charge. It can be seen that R3<sup>p</sup> also has an electron donating group – NH<sub>2</sub> and an electron withdrawing group –C(OH)<sub>2</sub><sup>+</sup>. In order to identify how the spin density delocalizes in captodative type radicals, the spin densities on the C, N and O atoms of R3 and R3<sup>p</sup> were compared (see Table 3.5). It can be seen that more than 50% of the total spin is localized on C<sub>α</sub> in R3, while the rest is mainly localized on the N and carbonyl O. It can be concluded that this type of spin distribution is due mainly to the effect of the spin polarization of the unpaired electron at C<sub>α</sub> on the lone pair electrons of the N and π electrons of the CO double bond of the carboxylic group. In R3<sup>p</sup>, more than
80% of the spin density is almost equally shared between the N, Cα and C1 atoms, while the rest is shared by the two O atoms. Thus, the spin distribution in R3p is significantly different from that seen in R3. The spin density ρ(Cα) > ρ(C1) > ρ(Oi), (i = 1, 2), in R3p can be explained by the spin induction along the chemical bonds by the positive charge of −C(OH)2⁺. Furthermore, the strong electron withdrawing capability of −C(OH)2⁺ in R3p significantly enhances the spin polarization of the lone pair electrons of the N atom. Hence, approximately 30% of the spin density resides on the N. Thus, spin induction and spin polarization together explain the spin distribution ρ(Cα) ~ ρ(N) > ρ(Cα) > ρ(C1) > ρ(O1) ~ ρ(O2) in R3p.

<table>
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<th>System</th>
<th>Cα</th>
<th>N</th>
<th>C1</th>
<th>O1</th>
<th>O2</th>
<th>O1 + O2</th>
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<td>0.079</td>
<td>0.033</td>
<td>0.146</td>
<td>0.179</td>
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<tr>
<td>R3-III</td>
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<td>0.05</td>
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<td>0.021</td>
<td>0.201</td>
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<tr>
<td>R3-IV</td>
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<tr>
<td>R3⁺-I</td>
<td>0.313</td>
<td>0.315</td>
<td>0.239</td>
<td>0.115</td>
<td>0.067</td>
<td>0.182</td>
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<tr>
<td>R3⁺-II</td>
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<td>R3⁺-III</td>
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<td>0.213</td>
<td>0.107</td>
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<tr>
<td>R3⁺-IV</td>
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<td>0.329</td>
<td>0.272</td>
<td>0.103</td>
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### 3.3.6 Geometry and Hyperfine Couplings of NH₂CH₂COC⁺HCOOH

The detection of R4 is a new finding² in the radiation chemistry of glycine crystals at room temperature. Experiments² confidently showed that there is only one Hα coupling tensor in R4 without any other α- and β-proton couplings. This fact prompted Sanderud et al.² to propose a zwitterionic structure (R4⁺) for the dimeric type radical and
to propose a mechanism for the formation of R4' from the reaction of zwitterionic glycine with R2'. However, an assignment of the observed couplings to the correct radiation products is essential for further mechanistic studies. The optimized structures of two possible conformers of R4', obtained using the Onsager model with an estimated radius 4.16 Å, are shown schematically in Figure 3.3.

The carbons and nitrogen in R4'-I form an almost planar skeleton with a nearly planar radical centre. However, O₂ and O₃ lie out of the mean molecular plane by approximately 25°. In R4'-II, the carbons, N and O₁ are coplanar, while the O₂C₃O₃ plane is almost perpendicular to the plane of the molecular skeleton.

The calculated hyperfine coupling tensors of Hₐ in R4'-I and R4'-II as well as the experimental values are listed in Table 3.6. It can be seen that both the isotropic HFCC and anisotropic components of Hₐ in R4'-I and R4'-II differ significantly from the corresponding experimental values. Thus, it is unlikely that R4' is the radical experimentally observed. However, it is quite possible that R4' is in fact not in its zwitterionic form. Hence, the neutral radical NH₂CH₂COC'*HCOOH (R4) was also investigated. Seven conformers of R4 were located, their optimized structures are shown schematically in Figure 3.2.

There are significant skeletal differences between the structures of R4-I to R4-IV and those of R4-V to R4-VII. The four carbon atoms in R4-I to R4-IV form cis-structures while the four carbon atoms in R4-V to R4-VII form trans-structures. The main difference between R4-I, R4-II, R4-III and R4-IV is the bonding position and
orientation of H₆, similarly for R4-V, R4-VI and R4-VII. The radical centre in R4-I, R4-II, R4-III, R4-V, R4-VI and R4-VII is almost planar, while the radical centre in R4-IV (\(\angle H\alpha C\alpha C₃C₂ = -172.6^\circ\)) is distorted by approximately 8° due to repulsion between H₆ and the hydrogen on C₁. In addition, O₂ and O₃ in R4-IV lie out of the C₃C\(\alpha\)H\(\alpha\) plane by 29.4°.

Table 3.6: PWP86/6-311G(2d,p) calculated HFCCs of R4' and R4 with experimental⁴ values and calculated⁵ relative energies (kJ mol⁻¹).

<table>
<thead>
<tr>
<th>system</th>
<th>(\alpha_{iso})</th>
<th>(T_{xx})</th>
<th>(T_{yy})</th>
<th>(T_{zz})</th>
<th>(\Delta E)</th>
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<td>-25.03</td>
<td>1.29</td>
<td>23.73</td>
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</tbody>
</table>

⁴Ref 2. ⁵B3LYP/6-311G(2df,p)//B3LYP/6-31+G(d,p) + ZVE.

The calculated HFCC tensors of H\(\alpha\) in R4-I to R4-VII are listed in Table 3.6. It can be seen that both the isotropic HFCC and anisotropic components of the H\(\alpha\) tensor in R4-I to R4-VII are in close agreement with the corresponding experimental values. Thus, it can be concluded that the experimentally observed radical must be R4 and not R4'. Correspondingly, R4 should be formed from the reaction of the zwitterionic form of glycine with R2, rather than with R2'. Thus, a deprotonation of the amino group in the zwitterionic form of glycine must be involved. However, in order to determine the conformation of R4 and the mechanism by which it is formed, more experimental and theoretical investigations of the radical are required.
3.4 Conclusions

The geometries and hyperfine couplings of the four observed radicals generated from irradiated glycine crystals have been computed using density functional theory. The calculated HFCCs have been compared with experimental values obtained at 295, 100 and 77 K.

A zwitterionic structure of R1 with C₃ symmetry was predicted using the Onsager model. The Hα couplings and the average HFCC of the three amino protons are in good agreement with the experimental values supporting the observation that the amino group in glycine rotates freely at room temperature. A detailed study of the effect of rotating the amino group on the proton HFCCs showed that at 100 K the amino group of R1 is constrained by intermolecular hydrogen bonding to be approximately 5° away from the optimized structure. The small value of the H₁ isotropic HFCC when the rotational angle is 5° supports the fact that the HFCC of one of the three amino protons is too small to be distinguished by the ENDOR technique at 100 K. In addition, the rotation of the amino group was found to have little effect on the HFCCs of Hα, Cα and N in R1.

Two conformers of CH₂COOH (R2-I and R2-II) were found which are able to account for the two forms of R2 observed experimentally, one at 77 K and the other at 140 K. The hyperfine coupling constants of the alternatively suggested radical R2’ (CH₂COO⁻) differ significantly from those observed experimentally. However, the present calculations are unable to unambiguously assign R2-I or R2-II to either experimentally observed conformer.
The HFCCs of three of the four possible conformations of R3 account for the experimental values of R3". However, the deviation of the calculated isotropic HFCC of Hα from experiments suggests that the crystal-packing in glycine has a significant effect on the Hα hyperfine coupling constant of R3". HFCC calculations on the re-optimized structures of R3, with appropriate geometrical constraints support the experimental postulate that the major difference between the two conformations of R3 is the twist between the O1C1O2 and C1CαN planes.

HFCC calculations on the experimentally proposed zwitterionic structure of R4' obtained with the Onsager model differ significantly from the experimental values, showing that R4' could not be the radical observed. However, the seven conformers of R4 all give HFCCs in good agreement with the experimental values. Hence, it is more likely that the radical observed experimentally is R4 (i.e., non-zwitterionic form). Thus, when it is formed from the reaction of the zwitterionic form of glycine with R2, a deprotonation of the amino group in the zwitterionic form of glycine must be involved.

With respect to the theoretical methods employed, it can be seen that density-functional theory is successful in predicting the magnetic properties of amino acid radicals. Furthermore, the Onsager model is found to work as equally well for the glycine radical in its zwitterionic form as originally found for the alanine radical system (see Chapter 4), resulting in structures capable of reproducing the experimental hyperfine coupling constants.
References


Interpreting the Radicals of L-α-alanine

4.1 Introduction

Amino acid radicals are involved in many biological reactions.\textsuperscript{1-3} Considerable attention has been focused on the formation, stability and reactions of protein radicals in biological systems.\textsuperscript{3} In addition, oxidative damage to amino acids is of importance in pharmacology, pathology and radiation biology.\textsuperscript{2b,4} Amino acids were among the first irradiated biomolecules studied by the techniques of electron spin resonance spectroscopy. Fundamental work on X- and γ-irradiated single crystals of amino acids remains an active field.\textsuperscript{5,6} Many studies of the radicals generated by irradiation of L-α-alanine have been published.\textsuperscript{7-19} Particular interest in L-α-alanine has arisen due to its radiation dosimetric properties. Several spin-trapping studies\textsuperscript{20,21} detected only one alanine-derived radical (R1) in polycrystalline samples, and more initial studies assumed that all variations in the ESR spectra of L-α-alanine-derived radicals were given by various properties of the radical R1.\textsuperscript{22-24} However, it has been suggested\textsuperscript{7,17,22-24,25,26} that the spectra of several radicals could be overlapping. This hypothesis was proven by Sagstuen et al.\textsuperscript{6} In their study, two new radicals were clearly detected by a combination of ESR and related techniques. Thus, to date three radicals have been found upon the X-
Interpreting the Radicals of L-α-alanine

irradiation of L-α-alanine crystals at 295 K. The radical structures were tentatively assigned to be those displayed in Figure 4.1.

![Figure 4.1 Structure of L-α-alanine and the proposed radicals formed upon X-irradiation of L-α-alanine crystals at 295 K.]

From a simulated spectrum, it was concluded that radicals R1 and R2 are present in comparable amounts (with an approximate ratio of 60% to 40%). R3 was recognized as a minor species. It was estimated that the α-C spin density of the two proposed conformers of R3 should be on the order of 35-40%. R1 is a deamination product, R2 is a hydrogen-abstraction product, and R3 is a product of hydrogen-abstraction accompanied by proton transfers. Alternatively, R3 could be generated from R2 as will be proposed in a later section. In the radiation chemistry of amino acids, the deamination product can be formed from a protonated anion through a reductive pathway, while the oxidation product can be formed from a cation. In L-α-alanine crystals irradiated at 77 K, an unusual cation has been postulated to explain the ESR spectrum of the oxidation product, but the oxidation product has not been detected. It seems that all radicals generated in irradiated L-α-alanine crystals at 295 K follow the reductive path. However, since the oxidation radical is very unstable, it can abstract hydrogen from an alanine molecule to form R2. Thus, the mechanism leading to R2 is unclear.
Great effort\textsuperscript{17} has been made to obtain a rough estimate of the coordinates of R1 in a unit cell. Although a few considerations\textsuperscript{6} of the geometrical conformation of R2 have been made by considering the Heller-McConnell relation,\textsuperscript{29} relatively less information is available for the structures of R2 and R3. However, further insight into the chemical nature of the radicals may be obtained from theoretical prediction of their structures and hyperfine coupling constants.

DFT has been shown to yield very accurate hyperfine coupling constants (HFCCs) for species such as DNA-related radicals.\textsuperscript{30} This has prompted a systematic study\textsuperscript{31} on L-\(\alpha\)-alanine-derived radicals for a better understanding of the properties of irradiated amino acids.

As mentioned in Chapter 3, amino acids exist as zwitterionic species in the crystalline state and in the solution, and radiation may produce amino acid radicals in a zwitterionic form (such as R2 in Figure 4.1). Because the zwitterionic structures of amino acids and their derived radicals do not correspond to energy minima in the gas phase,\textsuperscript{32,33} a combined computational scheme of the B3LYP method and the Onsager model has been applied for obtaining the zwitterionic structure of the L-\(\alpha\)-alanine-derived radical R2 using the Gaussian 94 program. The other computational details are identical to those in Chapter 3.
4.2 Results and Discussion

4.2.1 Optimized Geometries

The molecular structures of R1, R2 and R3 were fully optimized at the B3LYP/6-31+G(d,p) level. Four different minima for both R1 and R3 were found due to the fact that the proton has two possible positions on each of the oxygen atoms in the carboxylate group. Only one minimum of the zwitterionic form of R2 was found using the standard Onsager model with a dielectric constant (ε) of 78.39 and an estimated radius of 3.76 Å for the spherical cavity. Select geometrical parameters of R1, R2 and R3 are shown in Figure 4.2. The relative energies of the four conformers of R1 and R3 are shown in Table 4.1.

All four structures of R1 and the zwitterionic structure of R2 have a planar skeleton (except for the hydrogen atoms in the methyl and amino groups). Thus, R1 and R2 are typical π-radicals. On the other hand, in all four structures of R3, the nitrogen atom sticks out of the C1C2C3 plane by 3.2 to 6.4°. Thus, the structures of R3 are slightly pyramidal.

The main differences in the four structures of R1 caused by the arrangement of the OHx bond are the reorganization of the atoms in the molecular plane. The largest changes are 0.028 Å in bond length (CO bond) and 11.6° in bond angle (∠O1C1C2). From the relative energies, it can be seen that R1-II and R1-IV with intramolecular
Interpreting the Radicals of L-α-alanine

hydrogen bonding are more stable than R1-I and R1-III. Also, it can be seen that in R1-III the interaction between $H_x$ and the methyl group causes a staggered arrangement of the two $H_y$'s with respect to the OH$_x$ bond.

Figure 4.2 Optimized structures for R1, R2 (using the Onsager model) and R3 at the B3LYP/6-31+G(d,p) level (bond lengths in Å)

Besides a similar change in bond length as discussed for R1, there is a larger difference in the out-of-plane distortion between R3-I and the other three conformers (R3-II, R3-III, and R3-IV). The dihedral angles involving the amino hydrogens and the
two carboxylate oxygen atoms in R3-I differ by at least 10° from the corresponding angles in R3-II, R3-III, and R3-IV. From the relative energies, it can be seen that R3-II and R3-III are more stable than R3-I and R3-IV, due to the intramolecular hydrogen bonding.

<table>
<thead>
<tr>
<th>System</th>
<th>I</th>
<th>II</th>
<th>III</th>
<th>IV</th>
</tr>
</thead>
<tbody>
<tr>
<td>R1</td>
<td>22.9</td>
<td>0.0</td>
<td>29.9</td>
<td>3.8</td>
</tr>
<tr>
<td>R3</td>
<td>37.7</td>
<td>0.0</td>
<td>1.9</td>
<td>28.0</td>
</tr>
</tbody>
</table>

### 4.2.2 Hyperfine Couplings of Radical $^*\text{CH(CH}_3\text{)}\text{COOH}$

The calculated full hyperfine tensors of radical R1 are listed in Table 4.2, together with the experimentally determined tensors for comparison. The isotropic coupling constants of $H_\alpha$ in the four structures of R1 are all close in value, and in good agreement with experiment. The computed $T_{yy}$ component has a different sign from the experimental value, and $T_{zz}$ deviates from the experimental value by as much as 6 MHz for all conformers. These deviations could be caused by crystal-packing effects, which are not accounted for in the gas phase calculations. However, the principal components are in reasonable agreement with the experimental tensors. In addition, the computed average of the methyl proton couplings (the average $A_{iso}$ for $H_\beta$'s is approximately 65 MHz) in each conformer is in good agreement with the experimental value (69.9 MHz). The deviations of the calculated average anisotropic components seem larger than expected, mainly due to their relatively small values. However there is no doubt from the calculations that all four conformers are candidates for the molecular structure of radical R1 in the solid state.
Table 4.2: Comparison of calculated and experimental hyperfine couplings (MHz) of R1.

<table>
<thead>
<tr>
<th>Tensor</th>
<th>HFCC</th>
<th>R1-I</th>
<th>R1-II</th>
<th>R1-III</th>
<th>R1-IV</th>
<th>exptl.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hα</td>
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<td>-54.0</td>
<td>-54.9</td>
<td>-52.9</td>
<td>-56.1</td>
</tr>
<tr>
<td></td>
<td>$T_{xx}$</td>
<td>-32.5</td>
<td>-32.1</td>
<td>-31.7</td>
<td>-30.9</td>
<td>-31.8</td>
</tr>
<tr>
<td></td>
<td>$T_{yy}$</td>
<td>-1.4</td>
<td>-1.7</td>
<td>-1.8</td>
<td>-2.1</td>
<td>3.9</td>
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<td>$T_{zz}$</td>
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<td>-84.0</td>
<td>-86.6</td>
<td>-83.5</td>
<td>-87.9</td>
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<tr>
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<td>-56.7</td>
<td>-54.7</td>
<td>-52.7</td>
</tr>
<tr>
<td></td>
<td>$A_{zz}$</td>
<td>-18.1</td>
<td>-17.8</td>
<td>-21.4</td>
<td>-21.4</td>
<td>-28.3</td>
</tr>
<tr>
<td>Hβ1</td>
<td>$A_{\text{iso}}$</td>
<td>1.7</td>
<td>1.7</td>
<td>2.0</td>
<td>1.5</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$T_{xx}$</td>
<td>-3.9</td>
<td>-4.0</td>
<td>-3.9</td>
<td>-3.6</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$T_{yy}$</td>
<td>-2.8</td>
<td>-2.8</td>
<td>-3.4</td>
<td>-3.4</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$T_{zz}$</td>
<td>6.7</td>
<td>6.8</td>
<td>7.3</td>
<td>7.1</td>
<td></td>
</tr>
<tr>
<td>Hβ2</td>
<td>$A_{\text{iso}}$</td>
<td>96.3</td>
<td>96.9</td>
<td>93.6</td>
<td>97.0</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$T_{xx}$</td>
<td>-4.8</td>
<td>-4.8</td>
<td>-4.7</td>
<td>-4.8</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$T_{yy}$</td>
<td>-3.0</td>
<td>-3.0</td>
<td>-3.1</td>
<td>-3.0</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$T_{zz}$</td>
<td>7.8</td>
<td>7.8</td>
<td>7.8</td>
<td>7.8</td>
<td></td>
</tr>
<tr>
<td>Hβ3</td>
<td>$A_{\text{iso}}$</td>
<td>97.5</td>
<td>98.3</td>
<td>95.2</td>
<td>98.6</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$T_{xx}$</td>
<td>-4.8</td>
<td>-4.8</td>
<td>-4.6</td>
<td>-4.8</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$T_{yy}$</td>
<td>-3.0</td>
<td>-3.1</td>
<td>-3.1</td>
<td>-3.1</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$T_{zz}$</td>
<td>7.9</td>
<td>7.9</td>
<td>7.7</td>
<td>7.9</td>
<td></td>
</tr>
<tr>
<td>$H_{\text{β(ave)}}$</td>
<td>$A_{\text{iso}}$</td>
<td>65.2</td>
<td>65.6</td>
<td>63.4</td>
<td>65.7</td>
<td>69.9</td>
</tr>
<tr>
<td></td>
<td>$T_{xx}$</td>
<td>-4.5</td>
<td>-4.5</td>
<td>-4.5</td>
<td>-4.4</td>
<td>-2.6</td>
</tr>
<tr>
<td></td>
<td>$T_{yy}$</td>
<td>-2.9</td>
<td>-3.0</td>
<td>-3.2</td>
<td>-3.2</td>
<td>-2.3</td>
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<td>$T_{zz}$</td>
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<td>7.5</td>
<td>7.5</td>
<td>7.6</td>
<td>4.8</td>
</tr>
</tbody>
</table>

It has been proposed\textsuperscript{10} that R1 is generated from a primary carboxylate anion radical (Figure 4.3) through a deamination reaction. Mayagawa et al\textsuperscript{12} raised an interesting question of specific proton transfer in irradiated crystalline L-α-alanine at low temperatures, and concluded through an ESR study at 80 K that the transferred proton specifically binds to the O₂ atom in the COO plane in a position directed towards O₁. Later, Muto et al.\textsuperscript{15} re-examined this problem at 77 K using EPR and ENDOR techniques and obtained the opposite conclusion that the transferred proton stereospecifically attaches to O₁ along a direction perpendicular to the COO plane and is trapped outside
the COO plane. This arrangement was supported by a large positive isotropic coupling assigned to the transferred proton at 77 K. If R1 is formed by a deamination reaction from the stereospecifically proton transferred carboxylate anion radical, there will be only one conformer corresponding to R1. However, the calculated HFCCs suggest that the four conformers of R1 could exist simultaneously. In addition, since no evidence exists to exclude a possible proton transfer to O₁ and O₂ at 295 K, there could be an equilibrium between the four conformations. Also, it can be seen from the calculations that this problem cannot be solved by a proton ESR study, because the proton couplings of all conformers are very close to each other.

![Figure 4.3 Proton transfer to the carboxylate anion radical.](image)

### 4.2.3 Hyperfine Couplings of Radical H₃N⁺C⁺(CH₃)COO⁻

In Table 4.3, the computed full coupling tensor from the optimized structure of R2 is listed, along with the experimental hyperfine coupling values for comparison. For all of the protons of the amino group, great discrepancies between the computed isotropic HFCCs and the experimental values were found. However, the average of the three calculated amino proton isotropic HFCCs (47.4 MHz) is quite close to the average of the three experimental couplings (42.2 MHz) and the averages of the anisotropic couplings are also in good agreement. In spite of the above deviations, all the calculated
anisotropic components of the amino protons are in good agreement with the corresponding experimental values. The average of the calculated isotropic coupling constants for the three methyl protons (64.5 MHz) is very close to the experimental average (70.8 MHz). In addition, good agreement for the anisotropic components of the methyl protons is found. These observations confidently show that the optimized structure of radical R2 accounts for the hyperfine couplings in the crystalline environment except for the isotropic couplings of the three amino-group protons. This prompts a careful study of the effects of the rotation about the N—C$_2$ bond on the amino proton HFCCs.

<table>
<thead>
<tr>
<th>Tensor</th>
<th>$A_{iso}^{cal}$</th>
<th>$T_{xx}^{cal}$</th>
<th>$T_{yy}^{cal}$</th>
<th>$T_{zz}^{cal}$</th>
<th>$A_{iso}^{exp}$</th>
<th>$T_{xx}^{exp}$</th>
<th>$T_{yy}^{exp}$</th>
<th>$T_{zz}^{exp}$</th>
</tr>
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<tbody>
<tr>
<td>$H_1$</td>
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<td>10.6</td>
<td>86.3</td>
<td>-6.9</td>
<td>-2.7</td>
<td>9.5</td>
</tr>
<tr>
<td>$H_2$</td>
<td>69.9</td>
<td>-4.9</td>
<td>-4.5</td>
<td>9.4</td>
<td>30.2</td>
<td>-6.1</td>
<td>-4.7</td>
<td>10.7</td>
</tr>
<tr>
<td>$H_3$</td>
<td>69.9</td>
<td>-4.8</td>
<td>-4.5</td>
<td>9.3</td>
<td>10.2</td>
<td>-4.9</td>
<td>-4.8</td>
<td>9.7</td>
</tr>
<tr>
<td>$H_{amino(ave)}$</td>
<td>47.4</td>
<td>-5.1</td>
<td>-4.6</td>
<td>9.8</td>
<td>42.2</td>
<td>-6.0</td>
<td>-4.1</td>
<td>10.0</td>
</tr>
<tr>
<td>$H_{B1}$</td>
<td>2.2</td>
<td>-4.1</td>
<td>-3.9</td>
<td>8.0</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$H_{B2}$</td>
<td>95.5</td>
<td>-4.6</td>
<td>-3.4</td>
<td>8.0</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$H_{B3}$</td>
<td>95.7</td>
<td>-4.6</td>
<td>-3.4</td>
<td>8.0</td>
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<td></td>
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<tr>
<td>$H_{B(ave)}$</td>
<td>64.5</td>
<td>-4.3</td>
<td>-3.6</td>
<td>8.0</td>
<td>70.8</td>
<td>-2.9</td>
<td>-2.7</td>
<td>5.6</td>
</tr>
</tbody>
</table>

The difference between experiment and theory is suggested to arise from the relative orientation of the three amino protons in the L-α-alanine crystals. A detailed investigation of the rotational effects of the amino group about the N—C$_2$ bond on the isotropic HFCCs of the amino protons supports this idea. Figure 4.6 shows the variation in the three amino proton HFCCs as a function of the rotation angle. The rotation of the amino group was carried out by increasing the dihedral angle $H_1NC_2C_1$ by 30° starting from $H_1NC_2C_1 = 0.0°$. 
Figure 4.3 The amino proton HFCCs versus the rotation angle about the N—C\textsubscript{1} bond for R2

From the curve, it can be seen that the isotropic HFCCs of the three amino protons change dramatically, but the anisotropic components fluctuate very little (not shown). This is not surprising since the isotropic component of the HFCC is calculated by summing the contributions only at one particular point in space, while the anisotropic components are computed by integrating over all space. Interestingly, at $H_1NC_2C_1\approx40^\circ$, there is an excellent fit of the calculated isotropic couplings [$H_1$ (30 MHz), $H_2$ (12 MHz) and $H_3$ (86 MHz)] to the experimental values (30.2, 10.2, 86.3 MHz). Thus, it can be concluded that the configuration at $H_1NC_2C_1\approx40^\circ$ corresponds to the structure of R2 in
the L-α-alanine crystal at 295 K, in which the amino protons are fixed by intermolecular hydrogen bonds.

The Onsager model satisfactorily describes the zwitterionic structures of the amino acid radicals, which is required to accurately calculate the HFCCs. Since the experimental results can be explained through a rotation study with this solvation model, more computationally demanding models do not need to be investigated.

4.2.4 Hyperfine Couplings of \( \text{H}_2\text{NC}^+(\text{CH}_3)\text{COOH} \)

The computed full hyperfine coupling tensors of R3 and the experimentally determined tensors are listed in Table 4.4. Experimentally two coupling tensors were elucidated and assigned to a rapidly rotating methyl group. Investigation of the average of the calculated methyl proton isotropic HFCCs in the four conformers of R3 isolates the conformers into two groups. One group contains only R3-I with an averaged methyl proton isotropic HFCC equal to 41.3 MHz, which is in excellent agreement with one of the experimental values (39.5 MHz). The second group includes R3-II, R3-III, and R3-IV with an averaged methyl proton isotropic HFCC of approximately 35 MHz, which is in excellent agreement with the second experimental value (33.1 MHz). The largest deviation is less than 1.6 MHz. In addition, all of the anisotropic components for both group one and group two are in nearly perfect agreement with the corresponding experimental values. This leads to the conclusion that at least two conformers of R3 exist in the irradiated L-α-alanine crystals at 295 K. R3-I could be one conformer and the
second conformer could be either R3-II, R3-III or R3-IV. Another possibility is that the observed spectra arise from a mixture of all four conformations.

| Table 4.4: Comparison of calculated and experimental hyperfine couplings (MHz) of R3. |
|-----------------|-----|-----|-----|-----|-----|-----|
| tensor         | HFCC | R3-I | R3-II | R3-III | R3-IV | expnl |
| H₉₁           | A₁₀₀ | 1.5  | 2.0  | 46.9  | 19.0  |       |
|               | Tₓₓ   | -3.9 | -3.4 | -3.7  | -3.5  |       |
|               | Tᵧᵧ   | -2.7 | -3.2 | -2.7  | -3.2  |       |
|               | Tᵢᵢ   | 6.6  | 6.6  | 6.4   | 6.6   |       |
| H₉₂           | A₁₀₀ | 61.1 | 61.2 | 56.0  | 71.7  |       |
|               | Tₓₓ   | -3.5 | -3.3 | -3.5  | -3.5  |       |
|               | Tᵧᵧ   | -3.2 | -3.0 | -2.8  | -2.9  |       |
|               | Tᵢᵢ   | 6.7  | 6.4  | 6.3   | 6.4   |       |
| H₉₃           | A₁₀₀ | 60.5 | 43.7 | 1.4   | 15.7  |       |
|               | Tₓₓ   | -3.6 | -3.5 | -3.5  | -3.3  |       |
|               | Tᵧᵧ   | -2.9 | -2.8 | -2.7  | -2.8  |       |
|               | Tᵢᵢ   | 6.6  | 6.3  | 6.2   | 6.1   |       |
| H₉(ave)       | A₁₀₀ | 41.3 | 35.6 | 34.8  | 35.4  | 39.5  |
|               | Tₓₓ   | -3.7 | -3.4 | -3.6  | -3.4  | -2.7  |
|               | Tᵧᵧ   | -3.2 | -3.0 | -2.7  | -3.0  | -2.2  |
|               | Tᵢᵢ   | 6.6  | 6.3  | 6.3   | 6.4   | 5.0   |

Comparison of the molecular structure of R2 with that of R3-I leads to a possible mechanism for the formation of R3-I. In particular, R3-I can be formed from radical R2 through an intramolecular proton transfer. Alternatively, R2 could be formed from R3-I through an intramolecular proton transfer. However, the other three conformers appear to be products of intermolecular proton transfer.

A more interesting correlation of the radical structure to the HFCCs is found when the coplanarity of H₁, H₂, N and C₂ is examined. Table 4.5 lists the sum of the three bond angles of the amino group and the N—C₂ bond length in R3-I, R3-II, R3-III, and R3-IV.
Table 4.5: The sum of the three bond angles (degrees) of the amino group and the N—C$_2$ bond length in R3 (Å).

<table>
<thead>
<tr>
<th>structure</th>
<th>$\angle$H$_1$NC$_2$</th>
<th>$\angle$H$_2$NC$_2$</th>
<th>$\angle$H$_3$NH$_2$</th>
<th>sum</th>
<th>R(N—C$_2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>R3-I</td>
<td>116.1</td>
<td>117.4</td>
<td>112.4</td>
<td>345.9</td>
<td>1.389</td>
</tr>
<tr>
<td>R3-II</td>
<td>120.1</td>
<td>116.8</td>
<td>117.8</td>
<td>354.7</td>
<td>1.368</td>
</tr>
<tr>
<td>R3-III</td>
<td>119.6</td>
<td>117.1</td>
<td>117.1</td>
<td>355.4</td>
<td>1.370</td>
</tr>
<tr>
<td>R3-IV</td>
<td>119.9</td>
<td>117.3</td>
<td>117.3</td>
<td>352.7</td>
<td>1.370</td>
</tr>
</tbody>
</table>

From the results, it can be seen that the amino group of the four conformers tends to be planar, but the sums of the three bond angles fall into two groups. Only R3-I is in the first group, while R3-II, R3-III, and R3-IV are in the second group. The sum of the three bond angles in R3-I is at least 6.8° less than that of the second group. This indicates a larger π-conjugation in the second group. This statement is supported by comparison of the N—C$_2$ bond lengths of the four conformers. All the N—C$_2$ bond lengths in the second group are approximately 0.02 Å shorter than that of R3-I. Thus, the difference in the isotropic HFCCs of the two groups can be interpreted by the spin polarization of the unpaired $\alpha$ spin electron at the C$_2$ atom. More specifically, the more planar the amino group, the more easily the spin polarization from the lone pair electrons of the N atom can occur. Consequently, the more planar the amino group in R3, the lower the $\alpha$ (positive) spin density on the C$_2$ atom, and the more $\alpha$ spin density on the N atom. Hence, the methyl proton isotropic HFCC will be smaller in the more planar radicals.

Table 4.6 lists the spin density of the N, C$_2$, and O atoms in R3, together with the semiempirical molecular orbital values$^6$ for comparison.
Table 4.6: Spin density from DFT(PWP86) and semiempirical\textsuperscript{a} calculations on the C\textsubscript{2}, N and O atoms in R3.

<table>
<thead>
<tr>
<th>atom</th>
<th>R3-I</th>
<th>R3-II</th>
<th>R3-III</th>
<th>R3-IV</th>
<th>semiempirical</th>
</tr>
</thead>
<tbody>
<tr>
<td>C\textsubscript{2}</td>
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<td>0.519</td>
<td>0.521</td>
<td>0.537</td>
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<tr>
<td>N</td>
<td>0.162</td>
<td>0.232</td>
<td>0.222</td>
<td>0.235</td>
<td>0.20</td>
</tr>
<tr>
<td>O\textsubscript{1}+O\textsubscript{2}</td>
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<td>0.185</td>
<td>0.206</td>
<td>0.181</td>
<td></td>
</tr>
<tr>
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<td>0.146</td>
<td>0.183</td>
<td>0.150</td>
<td>0.25</td>
</tr>
</tbody>
</table>

It can be seen that R3-I has a larger spin density on the C\textsubscript{2} atom than the members of the second group. Thus R3-I possesses a larger methyl proton isotropic HFCC than R3-II, R3-III, and R3-IV due to a greater distortion at the amino group and therefore less spin polarization can occur. Also it can be seen that density functional theory calculations give a much better resolution of the spin density distribution compared with the semiempirical methods. The DFT calculations presented herein predict that the spin density residing on C\textsubscript{2} in the four conformers is greater than 51%. The total spin density on O\textsubscript{1} and O\textsubscript{2} is between 18.1% and 20.6%, and the spin density on the single carbonyl carbon is less than 18.8%. The N spin density is between 16.2% and 23.5%. These predictions are numerically different from the semiempirical molecular orbital values (about 45%, 25% and 20% for C\textsubscript{2}, carbonyl oxygen and N atom, respectively).

4.4 Conclusions

The geometries and hyperfine coupling constants of the radiation products of L-\(\alpha\)-alanine have been computed using density functional theory. The calculated results have been compared with the experimental values obtained from X-irradiated crystals of L-\(\alpha\)-alanine. The three main radiation products (R1, R2, and R3) have been discussed.
Four conformations of R1 were optimized and their hyperfine couplings support the experimental assignment to this radical. Unusual discrepancies between the calculated and the experimental values of the $T_{yy}$ and $T_{zz}$ anisotropic components for $H_\alpha$ were observed. These differences could be caused by crystal-packing effects that are not accounted for in the calculations.

The standard Onsager model with a dielectric constant of 78.39 predicts a planar zwitterionic structure for R2. A careful study of the rotational effects of the amino group on the amino proton hyperfine couplings shows that the conformation with $\angle H_1NC_2C_1\approx40^\circ$ corresponds to the R2 structure in the L-$\alpha$-alanine crystals, in which the amino protons are fixed by the intermolecular hydrogen bonds. Thus, the geometry obtained from the Onsager model is adequate to describe the HFCCs in this radical and more complex solvation models are not required to explain experimental results. The calculated hyperfine couplings of R2 show that the crystal environment has little effect on the alanine radical in its zwitterionic form, consistent with a previous investigation of the glycine radical.\textsuperscript{35}

Four conformers were investigated for radical R3 providing much more information about the structure of this radical. The conformers fall into two groups. The averages of the calculated methyl proton hyperfine couplings of each group match the experimental couplings perfectly. These results give solid support to the experimental assignment of the detected tensors. A very good correlation of the structure of the amino group to the spin polarization of the unpaired electron on the C$_2$ atom was found. This correlation accounts for the fact that the methyl proton hyperfine couplings of the four
conformations of R3 fall into two groups and reproduce the two experimentally
distinguishable coupling tensors.

Methodologically, it can be seen again that density functional theory is very
successful in predicting the magnetic properties of amino acid radicals, and that the
Onsager model can predict structures for amino acid radicals in their zwitterionic form
which are accurate enough to reproduce experimental hyperfine coupling constants.

References


Elucidating the Radiation Products of Hydroxyproline

5.1 Introduction

Since the 1950's, electron spin resonance (ESR) techniques have been used to study the radiation chemistry of amino acids.\(^1\) Upon irradiation, an amino acid may form either its primary radical cation or anion by ejection or capture of an electron. These primary radicals may then undergo further reactions, generally by decarboxylation or deamination of the primary radical cation or anion, respectively, to give various secondary radicals. Characterization and identification of the resulting radicals by ESR is often difficult, however, as found in the case of proline and related systems.\(^2-6\)

Of all the essential amino acids, proline is unique in having a five-membered ring with a secondary amino group. In the 1980's, a number of studies were performed on X-ray irradiated L-proline monohydrate,\(^5\) DL-proline-HCl,\(^3\) hydroxyproline-HCl\(^6\) and hydroxyproline\(^2,4\) single crystals. Two conformations were proposed for the hydroxyproline primary radical anion (R1\(^A\)). A number of other hydroxyproline derived radicals were also proposed, including a secondary radical cation (R2\(^C\)) resulting from
decarboxylation, three conformations of secondary radicals resulting from deamination, and radicals resulting from H-abstraction at the C₂ and C₃ positions. In addition, several possible zwitterionic radicals resulting from irradiation of hydroxyproline³ were also proposed. Due to complex and overlapping ESR spectra, however, the exact identification and characterization of many radicals and reaction intermediates was not possible. The experimentally proposed hydroxyproline-derived radicals are shown in Figure 5.1.

Figure 5.1 Schematic illustration of the structures of hydroxyproline and related radicals generated upon X-radiation.

Theoretical chemistry offers a complementary approach to experiment which can be used to gain greater insight into the radicals, and their reactions, produced upon irradiation of amino acids. Indeed, numerous studies have investigated the reliability of various computational schemes for the calculation of the hyperfine couplings of bioradicals. In particular, density functional theory methods have been shown to give reliable structures and hyperfine coupling constants for a range of biological radicals.
derived from amino acids,\(^8\)-\(^{14}\) quinones\(^{15,16}\) and nucleic acid bases.\(^{17}\) For the zwitterionic isomers, however, a slightly modified approach has been found to be necessary. This is due to the fact that the zwitterionic isomers of amino acids and their radicals often do not correspond to energy minima in the gas-phase, as exemplified by glycine\(^{18}\) and its radical.\(^{19,8}\) Thus, in order to obtain such structures the electrostatic effects of the crystalline environment must be taken into account. One approach is to treat electrostatic interactions of neighbouring molecules as a uniform dielectric continuum (Chapter 2). Previous calculations using the Onsager and related models for the zwitterions of glycine\(^{8,9}\) and alanine\(^{10}\) radicals, have been found to yield hyperfine coupling constants in good agreement with experiment.

In the present study, identical computational techniques as those previously used for glycine (in Chapter 3) have been employed to investigate possible radicals formed upon irradiation of hydroxyproline.\(^{20}\)

### 5.2 Results and Discussion

#### 5.2.1 The Radical Anion and Its Protonated Neutral Radical

Experimentally, upon irradiation of hydroxyproline no carboxylate hydrogen interactions were detected.\(^{2,4}\) Thus, the observed \(H_\beta\) hyperfine tensors (see Table 5.1) were assigned to two different conformations of the zwitterionic radical \(R_1^Z\).\(^{2,4}\) The optimized structures of possible conformers of \(R_1^Z\) using the Onsager model with a
radius of 4.35 Å are shown schematically in Figure 5.2, while the corresponding calculated isotropic and anisotropic HFCCs are given in Table 5.1.

Table 5.1: Calculated, PWP86/6-311G(2d,p), HFB HFCCs (MHz) of $R1^Z$, $R1^A$ and $R1^B$ and experimental values. Relative energies (kJ mol$^{-1}$) of the conformers of $R1^A$ and $R1^B$.

<table>
<thead>
<tr>
<th>System</th>
<th>$A_{iso}$</th>
<th>$T_{xx}$</th>
<th>$T_{yy}$</th>
<th>$T_{zz}$</th>
<th>$\Delta E^c$</th>
</tr>
</thead>
<tbody>
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<td>5.8</td>
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<tr>
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<td>0.0</td>
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<td>10.3</td>
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<td>-3.8</td>
<td>8.3</td>
<td>12.5</td>
</tr>
<tr>
<td>$R1^A$-IV</td>
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<td>-2.4</td>
<td>6.0</td>
<td>35.9</td>
</tr>
<tr>
<td>$R1^B$-I</td>
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<td>-3.8</td>
<td>8.9</td>
<td>0.0</td>
</tr>
<tr>
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<td>-3.8</td>
<td>8.9</td>
<td>1.4</td>
</tr>
<tr>
<td>$R1^B$-III</td>
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</tr>
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<td>22.4</td>
</tr>
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<td>-5.2</td>
<td>11.4</td>
<td></td>
</tr>
<tr>
<td>Exptl $^b$</td>
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<td>-4.7</td>
<td>-2.1</td>
<td>6.9</td>
<td></td>
</tr>
</tbody>
</table>

$^a$Ref 2. $^b$Ref 4. $^c$B3LYP/6-311G(2df,p)//B3LYP/6-31+G(d,p) + ZPVE.

Figure 5.2 Optimized structures of $R1^Z$, $R1^A$ and $R1^B$ (continued over page).
Two possible conformers, $R1^Z$-I and $R1^Z$-II, of the zwitterionic radical anion $R1^Z$ were obtained. The main difference between $R1^Z$-I and $R1^Z$-II is the orientation of O$_3$–H$_3$. However, both conformers possess a half-chair conformation with the –C$_3$HOH– moiety forming the apex, see Figure 5.2. The two structures both contain a reasonably
strong intramolecular \( O_1 \cdots H_2 \cdots N \) hydrogen bond (\( r_{O \cdots H} = 1.811 \) Å) between the positively-charged ring \(-NH_2^+\) group and the almost planar (see Table 5.2) anionic carboxylate group. As can be seen from Table 5.1, the calculated \( H_\beta \) HFCCs of \( R1^Z \) differ considerably from the experimentally observed values. Hence, it would appear unlikely that either of the experimentally observed conformers is \( R1^Z \).

Table 5.2: Optimized values of the angle \( \angle O_1C_2O_3C_1^a \) in \( R1^Z \), \( R1^A \) and \( R1^\rho \).

<table>
<thead>
<tr>
<th>Radical</th>
<th>( R1^Z )-I</th>
<th>( R1^Z )-II</th>
<th>( R1^A )-I</th>
<th>( R1^A )-II</th>
<th>( R1^A )-III</th>
<th>( R1^A )-IV</th>
<th>( R1^\rho )-I</th>
<th>( R1^\rho )-II</th>
<th>( R1^\rho )-III</th>
<th>( R1^\rho )-IV</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \angle O_1C_2O_3C_1 )</td>
<td>178.9</td>
<td>-179.8</td>
<td>175.8</td>
<td>160.5</td>
<td>159.5</td>
<td>167.4</td>
<td>133.7</td>
<td>133.8</td>
<td>130.4</td>
<td>130.3</td>
</tr>
</tbody>
</table>

\(^a\)Angles in degrees.

For the non-zwitterionic isomer (\( R1^A \)) of \( R1^Z \), four possible conformers were found; \( R1^A \)-I to \( R1^A \)-IV (see Figure 5.2). The main difference between the four conformers is the orientation of \( O_1 \) or \( O_2 \cdots H_1 \) in the carboxyl group. All are found to have a half-chair conformation with the \(-NH-\) moiety forming the apex except for \( R1^A \)-I for which the \(-C_3H_2OH-\) moiety forms the apex. Since \( R1^A \)-I possesses a strong intramolecular \( O_1 \cdots H_1 \cdots N \) hydrogen bond (\( r_{N \cdots H} = 1.818 \) Å) while the other conformers all possess a weak \( O_1 \cdots H_2 \cdots N \) hydrogen bond (\( r_{O_1 \cdots H_2} > 2.692 \) Å), it can be concluded that the apexes of the \( R1^A \) half-chair structures are dependent on the strength of the hydrogen bond. Interestingly, for \( R1^A \)-II and \( R1^A \)-III the bases of the half-chairs are almost perfectly planar while their carboxylic groups are more pyramidal than those of \( R1^A \)-I and \( R1^A \)-IV (see Table 5.2).
The calculated isotropic and anisotropic H_β HFCCs for all R^1^A conformers are given in Table 5.1. The coupling constants for R^1^A-II and R^1^A-III are very similar, reflecting the close similarities in structure, and are in close agreement with one of the experimentally observed values (exptl I), see Table 5.1. The isotropic coupling constants for R^1^A-I (32.3 MHz) and R^1^A-IV (6.2 MHz), however, differ considerably from either of the experimentally observed values of 23.9 and 61.0 MHz. Furthermore, they also differ significantly from the calculated coupling constants of R^1^A-II and R^1^A-III. These results suggest that the experimentally observed conformer denoted as exptl I in this present study, is most probably R^1^A-II or R^1^A-III, or even possibly a mixture of the two (they are calculated to lie close in energy, see Table 5.1).

The large difference between the two experimentally observed H_β HFCCs suggests that there may in fact be a net change in the charge between the two conformers exptl I and exptl II, i.e., exptl II may in fact be a protonated form of exptl I. Thus, possible protonated conformers of R^1^A were investigated, the resulting radicals now being neutral radicals. Four possible conformers were obtained and can be divided into two groups with respect to the five-membered ring skeletal structures; R^1^P-I, R^1^P-II (group I) and R^1^P-III, R^1^P-IV (group II), see Figure 5.2. The main difference between the two conformers in each group is the O_3-H_3 orientations. Group I possesses relatively stronger intramolecular O_1-H_{1x}⋯N hydrogen bonds (r_N⋯H_{1x}≈2.044 Å), with the –C_3H_2O– moiety forming the apex of the five-membered ring. In contrast, group II possesses weaker intramolecular O⋯H–N hydrogen bonds (r_O⋯H≈2.655 Å), and the –
NH– moiety forms the apex. In both groups, however, the carbon of the protonated carboxylic group has become more pyramidal, as shown in Table 5.2.

The calculated H8 HFCCs of R1^p-I to R1^p-IV are given in Table 5.1. Groups I and II give similar H8 HFCCs. Importantly, however, they differ considerably from those calculated for R1^A. The calculated coupling constants of R1^p are in good agreement with those previously assigned to a conformer of the zwitterion R1^Z and denoted as exptl II in Table 5.1. This suggests that the experimentally observed couplings of exptl II in fact arise from a protonated derivative of the radical anion of hydroxyproline. The calculated relative energies (see Table 5.1) suggest that exptl II is most likely a conformer, or a mixture of both conformers, of group I.

5.2.2 Secondary Radical Cation Formed upon Decarboxylation

Four conformations of R2^C were found and are illustrated schematically in Figure 5.3. As seen in Table 5.3, the two lowest energy conformers are R2^C-I and R2^C-II. In both radicals, the –C4(H2)– moiety forms the apex of the five-membered ring due to the formation of the intramolecular N–H–O1 hydrogen bond. In R2^C-III and R2^C-IV, the –C3(HO1H)– moiety is in the apical position of the five-membered ring, and both radicals lack intramolecular hydrogen bonds.
Elucidating the Radiation Products of Hydroxyproline

Figure 5.3 Optimized structures of R2C.

For R2C-I through R2C-IV, the calculated and experimentally observed HFCCs of Hα, H1, H2, H3 and H4 are listed in Table 5.3. On the basis of their calculated coupling constants, the four conformers can be divided into two groups. One group consists of R2C-I and R2C-II while the other consists of R2C-III and R2C-IV. The coupling constants of the two groups differ significantly, in particular for H1, H3 and, to a lesser extent, H4 (see Table 5.3). The calculated coupling constants of Hα and H2 appear to be less sensitive to the conformation. The calculated HFCCs of H1 in R2C-I and R2C-II are in closest agreement with experiment, while R2C-III and R2C-IV give HFCCs for H3 and, to a lesser degree, H4 in closer agreement with experiment. For all four conformers, the calculated anisotropic HFCCs of each of the five hydrogens listed in Table 5.3 are in
close agreement with the corresponding experimental values. These results suggest that the experimentally observed radical is indeed the decarboxylated secondary radical cation. However, a more precise determination of the conformation is not possible. Explicit consideration of hydrogen bonding and other interactions between the radical cation and the crystalline environment are necessary for a more precise assignment. This is, however, beyond the scope of the methods employed in this study.

Table 5.3: Calculated, PWP86/6-31G(2d,p), HFCCs (MHz) of H\textsubscript{a}, H\textsubscript{b}, H\textsubscript{c}, H\textsubscript{d}, and H\textsubscript{e} in R\textsuperscript{2c}-I to R\textsuperscript{2c}-IV and the experimental values, and relative energies (kJ mol\textsuperscript{-1}).

<table>
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<tr>
<th>tensor</th>
<th>HFCC</th>
<th>R\textsuperscript{2c}-I</th>
<th>R\textsuperscript{2c}-II</th>
<th>R\textsuperscript{2c}-III</th>
<th>R\textsuperscript{2c}-IV</th>
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\textsuperscript{a}Ref 2. \textsuperscript{b}B3LYP/6-311G(2df,p)//B3LYP/6-31+G(d,p) + ZPVE.
5.2.3 Radicals Formed upon Hydrogen Abstraction

The experimental observation of a single hydrogen HFCC of $-54.1$ MHz was assigned to the zwitterion of the radical formed upon hydrogen abstraction from the $C_2$ position: $R_3^Z$. In this present study, the optimized structure of $R_3^Z$ was obtained using the Onsager model, with an estimated radius of 4.19 Å, and is illustrated schematically in Figure 5.4. $R_3^Z$ contains a strong intramolecular $O_1\cdots H_4-N$ hydrogen bond ($r_{O_1\cdots H_4}=1.762$ Å). The $-C_3HOH-$ moiety forms the out-of-plane apex of the ring, causing the radical centre situated at the adjacent $-C_2-$ position to become quite pyramidal by approximately 16°.

The calculated and experimentally observed HFCCs of $H_\alpha$, $H_1$ and $H_2$ in $R_3^Z$ are given in Table 5.4. For $H_\alpha$ the calculated and experimentally observed coupling constants are in close agreement. The calculated isotropic hyperfine couplings of the beta hydrogens $H_1$ and $H_2$ are 106.9 and 13.8 MHz, respectively. Experimentally, only one beta hydrogen coupling of approximately 98 MHz was observed and was suggested to arise from $H_2$, which is in fact close to the HFCC calculated for $H_1$. It is feasible that the second, considerably smaller, beta hydrogen coupling was too small to be observed. These results appear to support the assignment of the zwitterionic radical $R_3^Z$ as the radical observed, however, a reversal of the assignment of the beta hydrogen HFCCs is suggested.

In addition, the neutral non-zwitterionic isomer of $R_3^Z$, hereafter denoted as $R_3^N$, was also investigated. Eight conformers of $R_3^N$ were obtained and are shown
schematically in Figure 5.4. The major difference between each of the conformers is in the orientation of the carboxylic group and the hydroxyl group at the C₃ position.

Figure 5.4 Optimized structures of R₃², and R₃ⁿ (continued over page).
The calculated HFCCs of the eight conformers of $R3^N$ are shown in Table 5.4. The value of $H_\alpha$ is similar for all eight conformers. It can be clearly seen that the calculated $H_1$ and $H_2$ HFCCs of $R3^N$-III to $R3^N$-VIII differ significantly from the experimentally observed values. While the $H_1$ HFCC of $R3^N$-II is close to the experimentally observed value of 98.8 MHz, the $H_2$ HFCC of 30.2 MHz is too large to suggest that it may not have been experimentally observed. For $R3^N$-I, however, the $H_1$ HFCC is in close agreement with the beta coupling observed experimentally, while the $H_2$ HFCC is quite small. Indeed, the calculated isotropic HFCCs of $R3^N$-I are in closer agreement with the experimentally observed values than those of $R3^Z$. Thus, it is not possible to exclude $R3^N$-I as the observed radical, although the $H_\alpha$ anisotropic
components of R3\(^2\) are in closer agreement with the experimental values than those of R3\(^N\).-I.

Table 5.4: Calculated, PWP86/6-311G(2d,p), and experimental HFCCs (MHz) of H\(_a\), H, H\(_2\) in R3\(^Z\) and R3\(^N\) and relative energies (kJ mol\(^{-1}\)) of the conformers of R3\(^N\).

<table>
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<tr>
<th>Tensor</th>
<th>H(_a)</th>
<th>H(_1)</th>
<th>H(_2)</th>
<th>(\Delta E^a)</th>
</tr>
</thead>
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<td>-32.3</td>
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<tr>
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</tr>
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</tr>
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<td>exp(e)</td>
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\(^a\)Ref 2. \(^b\)B3LYP/6-311G(2df,p)//B3LYP/6-31+G(d,p) + ZPVE.

Experimentally,\(^2\) a radical was observed which possessed four beta hydrogen couplings. These were proposed as arising from a radical in which hydrogen abstraction from the C\(_4\) position had occurred. In this present study, four possible conformers of the zwitterionic isomer of such a radical were found (R4\(^Z\)-I to R4\(^Z\)-IV) and are shown schematically in Figure 5.5. The structures were obtained using the Onsager model with an estimated radius of 4.30 Å. All four conformers contain a strong intramolecular O\(_1\)-H\(_1\)-N hydrogen bond (\(r_{O\cdots H}<1.686\) Å) and a radical centre that is pyramidal by approximately 18°. However, in R4\(^Z\)-I the -C\(_4\)- atom forms the apex of the five-membered ring, while in all other conformers the -C\(_3\)- radical centre forms the apex. In R4\(^Z\)-II the -C\(_3\)- radical centre can be considered as trans to the carboxyl group while it can be considered to be cis in R4\(^Z\)-III and R4\(^Z\)-IV.
Figure 5.5 Optimized structures of R4\(^2\).

The calculated HFCCs of the four beta-hydrogens of the four conformers of R4\(^2\) are listed in Table 5.5. The HFCCs for the four conformers differ significantly with ranges of 48.3, 44.4, 37.7 and 48.3 MHz for H\(_{1\beta}\), H\(_{2\beta}\), H\(_{3\beta}\) and H\(_{4\beta}\), respectively. This is due to the quite different orientations of the \(-\text{C}_3\text{OH}^-\) moiety. The calculated HFCCs of R4\(^2\)-I are in reasonable agreement with experiment, although the HFCC of H\(_{2\beta}\) is still considerably lower than that observed experimentally. This difference is most likely due to the effects of the crystalline environment on the structure of the radical. A more detailed and explicit consideration of the effects of the environment, however, is beyond the scope of the methods employed in this present study.
Table 5.5: Calculated, PWP86/6-311G(2d,p), and experimental HFCCs (MHz) of R4^2.

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<tr>
<th>tensor</th>
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</table>

^aRef 2.

5.2.4 Secondary Radicals Formed upon Deamination

Hyperfine couplings of two radicals have been observed experimentally which have been assigned to different conformations of the radical formed upon deamination, R5. One conformation was observed at 77 K,^4 denoted as exptl I, while the second conformation was observed at 125 K,^4 denoted as exptl II. For temperatures intermediate between 77 and 125 K, a mixture of conformations was observed.^2 It was proposed that the conformational difference between exptl I and exptl II may simply be due to protonation of the carboxyl group –COO^-. However, no couplings of a carboxylic proton for the two conformations were observed. Thus, it was unclear whether R5 was in its anionic (R5^A) or neutral protonated (R5^N) form.
Two conformers, $R5^A$-I and $R5^A$-II, of the anionic form of $R5$ were obtained and are shown schematically in Figure 5.6. Both contain an intramolecular $O_1\cdots H_3-N$ hydrogen bond ($r_{O\cdots H} = 2.151$ and $2.240 \text{ Å}$, respectively). The corresponding calculated HFCCs are listed in Table 5.6. The considerable differences between the calculated and experimentally observed HFCCs, particularly for $H_1$, clearly indicate that the observed radicals are not different conformers of the anionic form of $R5$.

Figure 5.6 Optimized structures of $R5^A$ and $R5^N$ (continued over page).
Figure 5.6 Optimized structures of R⁵⁺ and R⁵⁻.

Table 5.6: Calculated, PWP86/6-311G(2d,p), and experimental HFCCs (MHz) of R⁵⁺ and R⁵⁻, and relative energies (kJ mol⁻¹) of the conformers of R⁵⁻.

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<th>Tᵧᵧ</th>
<th>Tₓᵧ</th>
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<th>Tₓₓ</th>
<th>Tᵧᵧ</th>
<th>Tₓᵧ</th>
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</table>

⁴Ref 4. ⁵B3LYP/6-311G(2df,p)/B3LYP/6-31+G(d,p) + ZPVE
For the neutral protonated form of R5, eight possible conformers (R5N-I to R5N-VIII) were obtained and are shown schematically in Figure 5.6. The conformers may be divided into two groups depending on whether or not they contain an intramolecular hydrogen bond between the carboxylic group and the –NH2 moiety. The conformers R5N-I, R5N-II, R5N-III, R5N-V and R5N-VI, hereafter referred to as group I, contain a slightly shortened hydrogen bond between O2 of the carboxylic group and H4 of the –NH2 moiety (2.316 Å < rO⋯H < 2.431 Å). The conformers R5N-IV, R5N-VII and R5N-VIII, hereafter referred to as group II, contain no such hydrogen bond (rO⋯H > 3.661 Å). Consequently, the structures of group II conformers are more open than those of group I.

As can be seen in Table 5.6, these differences in the structures are also reflected in the calculated HFCCs. For the conformers in group I, the calculated Hα, H1 and H2 HFCCs are all grouped in the approximate ranges of –46 to –49, 70 to 80 and 2 to 4 MHz, respectively. These coupling constants are in close agreement with those experimentally observed at 77 K, i.e., exptl I. The small calculated coupling constants of H2 support the experimental postulation that the second beta-hydrogen coupling may have been too small to have been observed. The calculated HFCCs of the group I conformers are very similar to each other. Thus, it is not possible to determine if exptl I is due to one conformer or a mixture of the group I conformers. For conformers in group II, the Hα, H1 and H2 HFCCs are all grouped in the approximate ranges of –50 to –53, 130 to 140 and 21 to 34 MHz, respectively. These coupling constants are in good agreement with the conformer observed at 125 K, i.e., exptl II, with those of R5N-VIII in closest agreement. These results suggest that the major difference between the two
experimentally observed conformers is the presence of intramolecular hydrogen bonding at lower temperatures.

5.3 Conclusions

The structures and HFCCs of possible experimentally observed hydroxyproline-derived radicals have been investigated using density functional theory. The calculated HFCCs have been compared with experimental values.

For the radical anion of hydroxyproline (R1\(^{\text{A}}\)), the zwitterionic isomer (R1\(^{\text{Z}}\)) was obtained using the Onsager model. The calculated isotropic H\(_{\beta}\) HFCC of R1\(^{\text{Z}}\) differs significantly from the two experimentally observed values and previously assigned to different conformations of R1\(^{\text{Z}}\). Thus, it is unlikely that either of the conformations observed is the zwitterion R1\(^{\text{Z}}\). Four possible conformations of the non-zwitterionic form of the radical were also found. Of these, the isotropic and anisotropic H\(_{\beta}\) HFCCs of two possible conformations, R1\(^{\text{A}}\)-II and R1\(^{\text{A}}\)-III, are found to be in good agreement with one of the experimentally observed radicals. The second H\(_{\beta}\) HFCC observed experimentally is found to agree closely with the H\(_{\beta}\) HFCCs calculated for four possible conformations of the protonated derivative of the radical anion, R1\(^{\text{P}}\), in which the carboxylic group has been protonated. On the basis of these results, the two radicals observed, and previously assigned as different conformations of the zwitterion of the primary radical anion, are concluded to be a non-zwitterionic conformer of the primary radical anion and a derivative in which the carboxylic group has been protonated.
Four possible conformers of the secondary radical cation \((R^2C^+)\) formed by
decarboxylation of hydroxyproline were obtained. The calculated HFCCs of the four
conformers support the experimental assignment, however, none completely accounts for
the experimentally observed values. This is most likely due to interactions between the
radical and the crystalline environment, i.e., intermolecular hydrogen bond formation and
crystal packing effects, affecting the experimental values. The exact effect on the HFCCs
is unclear. Thus, a precise determination of the conformation of the observed radical is
not possible without including specific interactions between the radical and the
crystalline environment. This is not feasible for the methods employed in this present
study.

Several possible conformers for radical zwitterions formed by hydrogen
abstraction from the \(C_2\) or \(C_3\) position of the five-membered ring were obtained. The
calculated HFCCs for the zwitterionic radical formed by hydrogen abstraction from the
\(C_2\) position, \(R^3\), are in good agreement with the experimental values. However, a
neutral non-zwitterionic conformer, \(R^4_N-I\), also gives HFCCs in close agreement with the
experimental values. Thus, it is impossible to determine whether or not the radical
observed is the zwitterion. Four conformers, \(R^4-Z-I\), \(R^4-Z-II\) and \(R^4-Z-III\), \(R^4-Z-IV\), for the
radical zwitterion formed by hydrogen abstraction from the \(C_3\) position were obtained.
The HFCCs of all conformers are found to be dependent on the orientation of the –
\(C_3^*\)OH– moiety. The calculated HFCCs of \(R^4-Z-I\) are in closest agreement with
experiment. Thus, it is concluded that the radical observed is \(R^4-Z\), as previously
assigned, and that it possesses a conformation similar to that of \(R^4-Z-I\).
Two possible conformations of the radical anion formed on deamination were obtained. The calculated HFCCs of both conformers are quite similar, however, they differ significantly from the experimentally observed values. Eight possible conformations of the neutral radical, R5N, formed on protonation of the carboxyl group of the radical anion, were obtained. The conformers can be divided into two groups; those that contain an intramolecular hydrogen bond between the carboxylic group and the amino group, and those that do not. The calculated HFCCs of those conformers containing such an intramolecular hydrogen bond (R5N-I, R5N-II, R5N-III, R5N-V and R5N-VI) are in reasonable agreement with each other and are in good agreement with the experimental values observed at 77 K. The calculated HFCCs of those conformers not containing such an intramolecular hydrogen bond (R5N-IV, R5N-VII and R5N-VIII) are also similar to each other, but differ significantly from those which do contain such a bond. However, they are in close agreement with the experimental values observed at 125 K, with those of conformer R5N-VIII in closest agreement. On the basis of these assignments, the change in HFCCs observed on going from 77 K to 125 K is due to the breaking of the intramolecular carboxyl-amino hydrogen bond resulting in a more open structure.

References


Chapter 6

The Cross-linking Mechanisms between Cytosine and Tyrosine

6.1 Introduction

Reactive-oxygen-species (ROS) mediated oxidative stress,\(^1\) which is a disturbance in the oxidant-antioxidant balance in favour of the former, contributes to numerous pathological conditions among which cancer,\(^2\)–\(^6\) Alzheimer's\(^7,8\) and Parkinson's\(^9\) diseases are major problems. Common ROS include singlet oxygen \(^1\text{O}_2\), hydrogen peroxide \(\text{H}_2\text{O}_2\), superoxide anion \(\text{O}_2^-\), hydroxyl radical \(^\cdot\text{OH}\) and hydperoxyl radical \(\text{HOO}^\cdot\). Of these, \(^\cdot\text{OH}\) is thought to be the most damaging.\(^10,11\) Abstraction of hydrogen atoms by \(^\cdot\text{OH}\) from, or addition of \(^\cdot\text{OH}\) to DNA bases, sugars and amino acid residues of proteins produces huge numbers of secondary radicals. There can be up to \(10^3\) oxidative damaging events upon the DNA of each cell in the human body everyday.\(^12\) Extensive experimental studies discovered that the interaction of the \(^\cdot\text{OH}\) radicals with DNA bases results in a diversity of adducts of purines and pyrimidines.\(^13\)–\(^15\) Tandem base lesions within isolated DNA are also mediated by \(^\cdot\text{OH}.\(^16,17\)
The biological importance of oxidative damage to proteins has been considerably less studied. One reason for this, is that the research on protein radicals primarily has focused on their formation and functionality in enzymatic catalysis. For instance, it is commonly known that the tyrosyl radicals play important roles as reactive storage sites or metastable intermediates in a number of enzymes including ribonucleotide reductase, photosystem II, while little is known about its damaging effect. However, recent research on proteins has revealed that the actions of ROS on protein may lead to significant damage via hydrogen abstraction.

In particular, the formation of tyrosyl radicals has been recognized as one typical feature of oxidative stress. Further tyrosyl radical mediated damage includes the formation of protein cross-links via dityrosine and trityrosine, which possibly can serve as a marker for tyrosyl radical-mediated oxidative damage in atherosclerosis and other inflammatory conditions.

As DNA bases and proteins inside the nucleus are attacked by reactive oxygen species, the resulting protein radicals and DNA radicals may give rise to DNA-protein cross-links. In this aspect, radiation biology is well established to probe the oxidative effect of hydroxyl radicals. Ionizing radiation is known to be both mutagenetic and carcinogenic. Much of the cell damage caused by ionizing radiation involves the formation of ·OH radicals. It has been shown that ionizing radiation produces DNA-protein cross-links in living cells and isolated chromatin, which may cause serious problems in DNA replication. Even though great effort has been devoted to elucidating
the mechanisms of DNA lesions and protein damage, the coupled reactions involving biological radical intermediates are poorly understood.

The cross-link structures\textsuperscript{32-38} of pyrimidine bases and various amino acids in aqueous model systems have been characterized via GC-MS techniques. In particular, hydroxyl radical induced cross-linking of cytosine with tyrosine,\textsuperscript{34} thymine with tyrosine\textsuperscript{36} and thymine with lysine\textsuperscript{32} have been studied in detail. For the thymine + lysine system, the direct radical recombination reaction (Scheme 6.1) has been characterized as the major reaction mechanism that leads to the cross-link.\textsuperscript{32,35} For the cytosine + tyrosine or the thymine + tyrosine system, however, the molecular steps by which the \textsuperscript{•}OH radical induces the DNA-protein cross-links are still unclear. Several possible mechanisms based on the identified final products have been hypothesized.\textsuperscript{34,36,38}

Scheme 6.1 Schematic illustration of the radical combination mechanism for the cross-link of thymine and lysine.\textsuperscript{36}
In this chapter, theoretical investigation is focused on the reaction mechanisms of cytosine and tyrosine upon irradiation. Gajewski and Dizdaroglu\textsuperscript{34} reported that a DNA-protein cross-link of cytosine (Cyt) and tyrosine (Tyr) moieties forms in a nucleohistone when exposed to $\gamma$-irradiation. The cross-link was proposed to involve formation of a covalent bond between C$_6$ of cytosine and C$_3$ of tyrosine (the numbering of the atoms of cytosine and tyrosine is shown in Scheme 6.2). Moreover, it has been shown\textsuperscript{38} that the Cyt-Tyr cross-link in the nucleohistone is identical to the cross-link observed in the model experiments of the $\gamma$-irradiated aqueous solution of cytosine and tyrosine. Thus, free cytosine and tyrosine (phenol) have been used to investigate the mechanisms for the relevant cross-link in these systems.

It has been found\textsuperscript{39} that the $^\bullet$OH adds to the C$_5$=C$_6$ of cytosine with a preference at C$_5$ (see 2 in scheme 6.2) to the extent of 87%. In addition, tyrosyl radical\textsuperscript{40,41} (4 in Scheme 6.2) has been found to be the major radical resulting from the reaction of tyrosine with the hydroxyl radical. Thus, the neutral cytosine, tyrosine, cytosine C$_5$-hydroxylated radical and tyrosyl radical moieties are most likely the reactants that generate the Cyt-Tyr cross-link in the nucleohistone. Hence, the cross-linking mechanisms were proposed\textsuperscript{34} as schematically shown in Scheme 6.2: (1) the combination of cytosine C$_5$-hydroxylated radical and tyrosyl radical; (2) the addition of cytosine C$_5$-hydroxylated radical to tyrosine; (3) the addition of the tyrosyl radical to C$_5$ of cytosine and (4) the addition of the tyrosyl radical to C$_6$ of cytosine. The last two mechanisms were suggested to be the addition of tyrosyl radical 4 to the C$_5$=C$_6$ double bond of cytosine 1.\textsuperscript{34} Although only the radical combination mechanism was suggested to account for the formation of the cross-
link in the aqueous vitro system, the radical addition mechanisms have not been eliminated. In each of the above mechanisms, the final cross-link is formed through several steps of reaction. As such it is very important to examine the feasibility of every step of the reaction in each mechanism.

Scheme 6.2 Schematic illustration of the four investigated cross-linking mechanisms of cytosine, tyrosine, cytosine C$_5$-hydroxylated radical and tyrosyl radical in a nucleohistone.
Computationally, density functional theory (DFT) methods have been tested extensively against other accurate correlated methods for prediction of reliable geometries\textsuperscript{42} and reaction barriers.\textsuperscript{43} The reliability and efficiency of DFT methods offers an attractive theoretical approach to gaining insight into large biological systems.\textsuperscript{44,45} In particular, the paramagnetic properties of numerous biological radicals derived from the DNA bases,\textsuperscript{46a-d} sugars\textsuperscript{46e,47} and amino acids\textsuperscript{48a-h} have been extensively studied using density functional theory, and the reaction mechanisms of hydroxyl radical with imidazole, tyrosine, pyrimidine and purine bases have been investigated using B3LYP methods, Hartree-Fock (HF) and MP2 methods.\textsuperscript{49a-c} The unrestricted Hartree-Fock (UHF) and MP2 methods were suggested to suffer from severe spin contamination for radicals, whereas the B3LYP method was shown to be able to suitably describe the potential energy surfaces although it may have problems in locating transition structures in cases where the reaction barrier is very small.\textsuperscript{49c}

Since it has been reported that calculated structures and spin density distributions of phenoxyl radical and tyrosine side chain phenoxyl radical are essentially the same,\textsuperscript{50} the tyrosine and tyrosyl radical are modelled by phenol, 5, and phenoxyl radical, 6, (see Figure 6.1a) in the present study\textsuperscript{51} in order to reduce computational requirements.

### 6.2 Computational Methods

All geometry optimizations were performed with the B3LYP hybrid density functional (Chapter 2) in conjunction with the 6-31G(d,p) basis set using the GAUSSIAN 98 suite of programs. Harmonic vibrational frequencies and zero-point
vibrational energies (ZPVEs) were obtained at the same level of theory. Relative energies were obtained by performing single point calculations at the B3LYP level in conjunction with the 6-311G(2df,p) basis set using the above optimized geometries and by including the zero-point vibrational energy i.e., B3LYP/6-311G(2df,p)//B3LYP/6-31G(d,p) + ZPVE.

The solvent effect on the cross-linking mechanisms was investigated by single point calculations at the B3LYP/6-311G(2df,p) level on the optimized gas phase structures using the polarizable continuum model (PCM)\textsuperscript{52a-c} with a dielectric constant 78.39 for H\textsubscript{2}O. For all open- and closed-shell systems, the unrestricted (UB3LYP) and restricted (RB3LYP) B3LYP procedures have been used, respectively. The symbols U and R have been neglected for simplicity. All energies are in kJ mol\textsuperscript{-1} and bond lengths in angstroms (Å), unless otherwise specified. For the dimeric systems, a prime (') has been used to denote atoms originally on the tyrosine (phenol) moiety.

6.3 Results and Discussion

6.3.1 The Reactivity of the Reactants

The optimized structures of cytosine 1, Cyt-C\textsubscript{5}OH\textsuperscript{+} radical 2, phenol 5 and phenoxy radical 6 are schematically shown in Figure 6.1a. Mulliken charges on the heavy atoms of 1, 2, 5 and 6 and the atomic spin densities larger than 0.10 of the radicals 2 and 6, as calculated at the B3LYP/6-311G(2df,p)//B3LYP/6-31G(d,p) level of theory, are shown in Figures 6.1b and 6.1c, respectively.
Figure 6.1  (a) Optimized structures (bond lengths) of cytosine 1, C$_7$-hydroxylated radical 2, phenol 5 and phenoxy radical 6. (b) Mulliken charges on the heavy atoms of cytosine, C$_7$-hydroxylated radical, phenol and phenoxy radical. (c) Spin density distribution (only absolute values at the atoms larger than 0.10 are shown) of C$_7$-hydroxylated radical and phenoxy radical. Values in parentheses: experimental estimates, ref 59. (d) Possible resonance structures of the phenoxy radical.
The skeletal structure of cytosine is approximately planar. However, the amino group of cytosine is pyramidal by approximately $25^\circ$ ($\angle\text{H}_8\text{N}_7\text{C}_6\text{H}_6=154.7^\circ$). Even if the cytosine-ring shows a normal $\pi$-conjugated pattern, the $C_5-C_6$ bond (1.359 Å) has a localized double bond character, being much shorter than $C-C$ bond of benzene (1.396 Å). Furthermore, it is noted that the charge at $C_5$ is negative (-0.332), while at $C_6$ it is positive (+0.174). This particular charge distribution is associated with the position of the heteroatoms within the cytosine molecule. Since the addition of $^*\text{OH}$ to a polarizable double bond has remarkable selectivity towards an electron rich center, the difference of the charge at $C_5$ and $C_6$ explains why the $^*\text{OH}$ addition to the cytosine $C_5$ dominates the reaction.

The Cyt-C$_5$OH$^*$ radical 2 has a half-chair conformation on the six-membered ring with $C_5$ being the chair-back. The formation of the tetrahedral $C_5$ centre in 2 weakens the $N_1-C_6$ and $C_2-N_3$ double bond character by lengthening these bonds, but enhances the $N_1-C_2$ and $N_3-C_4$ double bond content by shortening the bonds. As a consequence, $C_6$ is pyramidal by $23^\circ$ and becomes a localized radical centre with spin density of approximately 0.708.

The phenol 5 is a planar molecule. The $C-C$ bond distances suggest that the benzene moiety is $\pi$-conjugated. It is interesting to note that the ortho- $C_3$ and $C_5$ have larger negative Mulliken charges than the other carbons of the ring. Hence, the electrophilic addition of Cyt-C$_5$OH$^*$ radical 2 to phenol is suggested to occur on the ortho-carbon sites as proposed in mechanism 2 (see Scheme 6.2). The preference for
addition to C3/C5 has also been noted in the case of direct \(^{1}\text{OH}\) radical attack on tyrosine.\(^{40,49a,55}\)

The structure of phenoxy radical 6 resembles that obtained by Chipman et al.\(^{56}\) at the CASSCF/6-311G(2d,p) level of theory. The main geometrical changes from phenol 5 to phenoxy radical 6 are the shortening of the C4—O, C2—C3 and C5—C6 bonds and the elongation of the C1—C2, C3—C4, C4—C5 and C1—C6 bonds. The C4—O bond length of 1.258 Å is much closer to the C=O double bond of 1.225 Å observed for \(p\)-benzoquinone\(^{57}\) than the calculated phenol C—O single bond length of 1.368 Å or the reported value of 1.381 Å from an electron diffraction measurement.\(^{58}\)

The calculated spin densities are in fair agreement with the experimental values, shown in parentheses in Figure 6.1c. The calculated spin density at the oxygen is approximately 0.434, while the experimental estimate is 0.26.\(^{59}\) The large discrepancy between the values has also been noted earlier,\(^{49d}\) and shown to arise primarily from an erroneous empirical value employed in the McConnell relation used to convert measured hyperfine parameters into spin densities. From either the calculated spin density distribution or the experimental data, it is however clear that most of the unpaired electron is delocalized on the benzene ring. This agrees with the resonance structures of the radical, displayed in Figure 6.1d. Since the C1 site is blocked in the tyrosyl radical (see 4 in Scheme 6.2), the equivalent C3 or C5 positions are the most likely reactive sites. This conclusion supports the proposal\(^{38}\) that the cross-linking site is predominantly on the C3 (C5) carbon.
6.3.2 The Initial Step of the Cross-linking Mechanisms

The four mechanisms shown in Scheme 6.2 are considered as competitive reaction paths in the present study. The feasibility of the initial step of each reaction mechanism may determine its fate. Thus, the potential energy surfaces for the initial step of each reaction mechanism are investigated.

The energy profile for the direct combination of Cyt-C₅OH⁺ radical 2 and phenoxy radical 6 is schematically shown in Figure 6.2a. All attempts to locate a transition structure (TS) for the formation of 1a, including scans of the singlet and triplet energy surfaces, were unsuccessful. The radical combination forming the product 1a is found to be energetically favourable by 157.0 kJ mol⁻¹.

The energy profile for the addition of the Cyt-C₅OH⁺ radical, 2, to the phenol, 5, is schematically shown in Figure 6.2b. The Cyt-C₅OH⁺ radical initially interacts with the phenol forming a hydrogen-bonded complex 2a, lying 10.1 kJ mol⁻¹ lower in energy. The hydrogen-bonding distance between the —OH group of Cyt-C₅OH⁺ radical and the oxygen of phenol is approximately 1.913 Å. The cross-linked product 2e is formed via TS 2b with an activation barrier of 74.6 kJ mol⁻¹. In 2b, the distance between the C₆ of Cyt-C₅OH⁺ radical and the C₃' of phenol is approximately 2.096 Å and the —OH group of the cytosine moiety interacts with the oxygen of phenol at a shorter distance of 1.882 Å. Interestingly, despite the even stronger hydrogen-bond (1.822 Å) in the product 2e, this lies more than 27 kJ mol⁻¹ higher in energy than the isolated reactants.
Figure 6.2 Schematic energy profiles for the initial reaction step (a) mechanism 1 \((2 + 6)\), (b) mechanism 2 \((2 + 5)\), (c) mechanism 3 \((1 + 6)\) addition to \(C_3\) of cytosine, (d) mechanism 4 \((1 + 6)\) addition to \(C_6\) of cytosine, (e) summary of mechanisms 1, 2, 3 and 4 in the gas phase, (f) summary of mechanisms 1, 2, 3 and 4 showing the effects of solvent, by inclusion of the PCM model. (continued over page)
Figure 6.2 Schematic energy profiles for the initial reaction step (a) mechanism 1 \((2 + 6)\), (b) mechanism 2 \((2 + 5)\), (c) mechanism 3 \((1 + 6)\) addition to \(C_3\) of cytosine, (d) mechanism 4 \((1 + 6)\) addition to \(C_6\) of cytosine, (e) summary of mechanisms 1, 2, 3 and 4 in the gas phase, (f) summary of mechanisms 1, 2, 3 and 4 showing the effects of solvent, by inclusion of the PCM model. (continued over page)
Figure 6.2 Schematic energy profiles for the initial reaction step (a) mechanism 1 (2 + 6), (b) mechanism 2 (2 + 5), (c) mechanism 3 (1 + 6) addition to C₃ of cytosine, (d) mechanism 4 (1 + 6) addition to C₆ of cytosine, (e) summary of mechanisms 1, 2, 3 and 4 in the gas phase, (f) summary of mechanisms 1, 2, 3 and 4 showing the effects of solvent, by inclusion of the PCM model.
The changes of the spin density between the cytosine and the phenol moieties from 2a, 2b to 2c are shown in Table 6.1. Essentially, the interaction between the two moieties is purely electrostatic in 2a and the spin is entirely on the cytosine moiety. In 2b, approximately 0.428 of the spin is shifted onto the phenol. In 2c, approximately 0.926 of the unpaired electron is localized on the phenol ring. In particular, the meta-carbons C_2' and C_6' of the phenol possess approximately 0.886 of the total spin density, of which C_6' has the largest spin density of 0.498. Overall, the addition of the Cyt-C_5OH* radical to phenol shifts the unpaired electron from the cytosine moiety to the meta-carbon sites of the phenol ring. The substantially localized double character of the C_1'=C_2' (1.366 Å) and C_4'=C_5' (1.368 Å) bonds suggests that the formation of the C_5—C_3' bond in 2e deforms the π-conjugation of the phenol ring. As a consequence, the cross-linked product 2e is higher in energy than the reactant system.

Table 6.1: The spin density partitioning between cytosine and phenol moieties in 2a, 2b, 2c, 3a, 3b, 3c, 4b and 4c.

<table>
<thead>
<tr>
<th>Spin population</th>
<th>2a</th>
<th>2b</th>
<th>2c</th>
<th>3a</th>
<th>3b</th>
<th>3c</th>
<th>4a</th>
<th>4b</th>
<th>4c</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cytosine moiety</td>
<td>0.999</td>
<td>0.512</td>
<td>0.074</td>
<td>-0.002</td>
<td>0.639</td>
<td>0.889</td>
<td>-0.003</td>
<td>0.628</td>
<td>0.950</td>
</tr>
<tr>
<td>Phenol moiety</td>
<td>0.001</td>
<td>0.428</td>
<td>0.926</td>
<td>1.002</td>
<td>0.361</td>
<td>0.111</td>
<td>1.003</td>
<td>0.372</td>
<td>0.050</td>
</tr>
</tbody>
</table>

The energy profile for the addition of phenoxy radical to the C_5 cytosine position is schematically shown in Figure 6.2c. Initially, the phenoxy oxygen forms a hydrogen bond with the cytosine N_1H (1.996 Å). The resulting reactant complex 3a lies 62.4 kJ mol\(^{-1}\) lower in energy than the isolated reactant system. The formation of the cross-linked product 3e involves an activation barrier of 131.0 kJ mol\(^{-1}\) via TS 3b. In 3b, the cytosine C_5 approaches the C_3' of the phenoxy radical at a distance of 1.862 Å. Product
3c lies 66.3 kJ mol\textsuperscript{-1} higher in energy than the reactant system, and has a weak hydrogen bond (1.937 Å) stabilizing the conformation.

The spin density partitioning between the cytosine and the phenol moieties of 3a, 3b and 3c is shown in Table 1. The spin is essentially localized on the phenoxy moiety in the reaction complex 3a, while more than half (0.639) of the unpaired electronic spin is delocalized onto the cytosine ring in the TS 3b. The formation of the C5-C3' bond in product 3c results in the cytosine ring having a spin density of approximately 0.889, of which 0.698 spin is localized at C6 of cytosine moiety. The localized double bond character of C1'= C2' (1.346 Å) and C5'=C6' (1.356 Å) indicates the loss of a delocalized unpaired electron on the phenol ring. Due to the formation of a localized cytosine C6 radical centre, 3c is higher in energy than the reactant system.

The energy profile for the addition of the phenoxy radical to C6 of cytosine is schematically shown in Figure 6.2d. Phenoxy radical and cytosine form the intermolecular hydrogen bonded complex 4a lying 78.3 kJ mol\textsuperscript{-1} lower in energy (Figure 6.2c). The product 4c is formed via TS 4b with a barrier of 165.0 kJ mol\textsuperscript{-1}. In 4b, the C6 - C3' distance is 1.915 Å. 4c lies approximately 73.4 kJ mol\textsuperscript{-1} higher in energy than the reactants. It should be noted, however, that the N1 position of cytosine is not available in biological systems. Hence, any addition complex will have a different conformation and lie higher on the energy surface than the optimized complex 4a. The activation energy for passing via TS 4b will consequently be lower than the present 165.0 kJ mol\textsuperscript{-1} in the full DNA-protein system. Similar changes (Table 6.1) of the spin density between the
cytosine and phenoxy moiety has been observed from 4a, 4b to 4e as from 3a, 3b to 3c. However, the spin density of 4e is now predominantly localized at the C5 of cytosine.

The product 4e is approximately 7.1 kJ mol\(^{-1}\) higher in energy than the product 3c (see Figure 6.2c) and, more importantly, TS 4b is approximately 18.1 kJ mol\(^{-1}\) higher in energy than TS 3b. Thus, the computed energy surfaces suggest that the addition of the tyrosyl radical to cytosine prefers the C5 site over C6. Hence, it can be concluded that the addition is electrophilic in nature.

For comparison, the gas phase potential energy surfaces of the initial steps are summarized in Figure 6.2e. As the original experiments were performed in aqueous solution, the solvent effects on the potential energy surface are investigated by B3LYP/6-311G(2df,p) single point calculations using the polarizable continuum model (PCM) with a dielectric constant 78.39 of water. The resulting energy profiles of the four mechanisms in solvation are shown in Figure 6.2f. Solvation reduces the barriers of mechanisms 3 and 4 from 131.0 and 165.0 kJ mol\(^{-1}\) to 87.3 and 135.4 kJ mol\(^{-1}\), respectively. In the case of mechanism 2, however, the energy cost required for the formation of 2e increases from 74.6 kJ mol\(^{-1}\) in the gas phase to 127.9 kJ mol\(^{-1}\) upon inclusion of solvent. All the solvated products 1a, 2e, 3e and 4e have a significantly higher relative energy (-112.8, 127.9, 52.2, and 72.6 kJ mol\(^{-1}\)) than in the gas phase (-157.0, 27.9, 66.3 and 73.4 kJ mol\(^{-1}\)).

From the calculated energy profiles in both gas phase and in solution, the initial steps of mechanisms 2, 3 and 4 have significant barriers and are thermodynamically unfavourable. The energetically most favourable of these three is mechanism 3 which in
aqueous phase has a TS ca 53 kJ mol\(^{-1}\) above the reactants, and where the steric 
chemistry of the real system will lift the addition complex significantly above the 
computed minimum. However, of the four mechanisms proposed, the preferred 
mechanism for producing the cross-link between cytosine and tyrosine is the radical-
radical addition. This is found to proceed without barrier, and is the only mechanism to 
provide an exothermic adduct. Thus, for the remainder of this chapter, only possible 
reaction steps that may lead to the final product from intermediate product 1a are 
considered.

### 6.3.3 Mechanisms of the Hydrogen Transfer

After the initial step of the radical-radical combination, three possible 
mechanisms of an internal hydrogen transfer from C\(_{3}'\) to O\(_{2}'\) within 1a (Figure 6.2a) are 
considered. Mechanism A: direct hydrogen transfer from C\(_{3}'\) to the O\(_{2}'\). Mechanism B: 
hydrogen transfer from C\(_{3}'\) to O\(_{2}'\) using a water molecule as a bridge. Mechanism C: 
concerted hydrogen transfers from C\(_{3}'\) to O\(_{1}\) and O\(_{1}\) to O\(_{2}'\) using a water molecule and the 
—O\(_{1}\)H\(_{1}\) group of 1a as bridges. The computed energy profiles of the three possible 
mechanisms are schematically shown in Figures 6.3a-c.

The calculated energy profile of mechanism A is schematically shown in Figure 
6.3a. The hydrogen-transferred product 1c can form via TS 1b with an activation barrier 
of 227.3 kJ mol\(^{-1}\). 1c is 66.3 kJ mol\(^{-1}\) lower in energy than 1a. This pathway is unlikely 
to happen because the barrier is too high.
Figure 6.3 Schematic energy profiles of the hydrogen transfer from C5' to O2' (a) for mechanism A, (b) for mechanism B and (c) for mechanism C in the gas phase (——) and in the presence of H2O using PCM solvation (—). (d) Optimized structures of 1g and 1g'. (continued over page)
The structure of TS 1b suggests that the high barrier is mainly caused by the tension of a four-membered ring C3'-H2'-O2'-C4'. As the reaction was carried out in aqueous solution, water molecules may be specifically involved in the hydrogen transfer reaction. Thus, mechanism B is proposed in order to investigate the role of a water molecule for the hydrogen transfer.
The computed energy profile of mechanism B is schematically shown in Figure 6.3b. Initially, 1a interacts with a water molecule forming a hydrogen bonded complex 1d lying 24.7 kJ mol\(^{-1}\) lower in energy than the isolated reactants. The product complex 1f is formed via a six-membered ring TS 1e. The activation barrier is approximately 109.0 kJ mol\(^{-1}\). As expected it is much lower than the barrier 227.4 kJ mol\(^{-1}\) of mechanism A. 1f lies 114.7 kJ mol\(^{-1}\) lower in energy. Isolation of the 1e + H\(_2\)O from 1f costs 48.4 kJ mol\(^{-1}\). In this particular situation the water molecule clearly acts as a catalyst for the hydrogen transfer. Thus, mechanism B is preferred over mechanism A.

There is a strong hydrogen bonding interaction, with a distance of 1.730 Å, between O\(_1\)--H\(_1\) and O\(_2'\) of 1a (see Figure 6.2a). For this particular conformation, transfer of H\(_2'\) from C\(_3'\) to O\(_1\) may induce a simultaneous transfer of H\(_1\) from O\(_1\) to O\(_2'\). This possible mechanism is equivalent to a net hydrogen transfer from C\(_3'\) to O\(_2'\). Because the distance between H\(_2'\) and O\(_1\) is approximately 2.623 Å, it would be difficult for the direct transfer of H\(_2'\) from C\(_3'\) to O\(_1\) to take place over such a distance. However, a water molecule may catalyze the transfer of H\(_2'\) from C\(_3'\) to O\(_1\), similar to what has been found in mechanism B. Thus, the feasibility of the concerted hydrogen transfers along the chain C\(_3'\) - O\(_{\text{water}}\) - O\(_1\) - O\(_2'\) of mechanism C is investigated.

The computed energy profile of mechanism C is shown in Figure 6.3c. As mentioned in mechanism B, 1a and a water form the reactant complex 1d lying 24.7 kJ mol\(^{-1}\) lower in energy. The formation of the product complex 1f may proceed via TS 1g with a barrier of 59.2 kJ mol\(^{-1}\). The participation of a water molecule and the —O\(_1\)H\(_1\)···
O$_2$' hydrogen bond in the reaction leads to an eight-membered ring structure —C$_{1'}$—H$_2$—
-O$_2$—H$_c$—O$_1$—H$_1$—O$_2$'—C$_{4'}$— of 1g. Because TS 1g is 49.8 kJ mol$^{-1}$ lower in energy
than TS 1e, mechanism C is preferred over mechanism B.

Interestingly, another transition structure 1g' has also been found for mechanism
C. For comparison, the structures of both 1g and 1g' are shown in Figure 6.3d. It can be
seen that 1g distinguishes itself from 1g' by possessing a hydrogen bond between H$_b$ of
the water and the N$_7$ of the cytosine moiety, with a distance of 2.515 Å. 1g lies 4.2 kJ
mol$^{-1}$ lower in energy than 1g' due to the hydrogen bond between H$_b$ and N$_7$. Thus, the
H$_b$···N$_7$ hydrogen-bond assists the concerted hydrogen transfers.

Mechanism C is concluded to be the overall preferred mechanism for the
hydrogen transfer. In particular, the eight-membered ring structure of 1g provides new
insights for mechanisms of hydrogen transfer in biological systems.

As the original experiments were performed in aqueous solution, the solvent
effects on each mechanism have been investigated by performing B3LYP/6-311G(2df,p)
single point calculations using the PCM model. The barriers for mechanism A, B and C
in solution are 279.1, 114.2 and 80.4 kJ mol$^{-1}$, which are higher than they are in the gas
phase (227.3, 109.0 and 59.2 kJ mol$^{-1}$). However, mechanism C is the preferred pathway
in both the gas phase and in solution. For simplicity, only the energy profile in solution
of mechanism C is shown in Figure 6.3c.
6.3.4 Acid-catalyzed Dehydration

Dehydration of 1c leads to the final cross-linked product. Experimentally, 6 M HCl was added for the dehydration step. It was presumed that dehydration of 1c is acid-catalyzed. However, the feasibility of acid catalysis for the dehydration depends on the proton affinity of the O₁ of the —O₁Hₑ group of 1c in Figure 6.3c. The optimized structure of 1h, the protonated form of 1c, is shown in Figure 6.4a.

![Diagram](image)

**Figure 6.4** (a) Schematic drawing of 1h. (b) Schematic energy profile of the dehydration reaction.
The proton affinity of the O$_1$ site of 1c is calculated to be 783.0 kJ mol$^{-1}$; significantly larger than the proton affinity 705.2 kJ mol$^{-1}$ of H$_2$O at the same level of theory. The magnitude of the computed proton affinity of the O$_1$ site suggests that the O$_1$ site is easily protonated under acidic conditions. Thus, the dehydration of 1h should follow the standard reaction mechanism, involving protonation at O$_1$, loss of water (H$_2$O$_1$H), and deprotonation at C$_6$. The formation of the final product 1i via dehydration of 1c is energetically favoured by 43.1 kJ mol$^{-1}$ as shown in Figure 6.4b.

6.4 Conclusions

The cross-linking reaction mechanisms of the DNA cytosine moiety and the tyrosine residue of protein have been investigated by use of the B3LYP density functional theory method. The reactions are modelled by a smaller reaction system of cytosine and phenol and their derived radicals.

The direct combination of the Cyt-C$_5$OH$^*$ radical and phenoxy radical is suggested to be the preferred mechanism with a small or effectively no barrier, while all the radical addition mechanisms examined are suggested to be thermodynamically unfavourable. The cross-linking mechanism identified for the cytosine and tyrosine system in the present study is similar to the experimental findings$^9$ that the hydroxyl radical-induced cross-linking of the thymine and lysine is dominated by a radical recombination mechanism.
The Cross-linking Mechanisms

Of the three possible mechanisms considered for the subsequent hydrogen transfer, mechanism C, by which a net hydrogen transfer from C$_3'$ to O$_2'$ of 1a proceeds by a water assisted chain of concerted hydrogen transfers in transition structure 1g, is suggested to be the most favoured.

Using the PCM model, it has been found that water has significant solvent effects on the cross-linking mechanisms of cytosine and tyrosine. However, the preferred mechanism is suggested to be the same in both the gas phase and in solution.

References


Modelling the Action of an Antitumor Drug: Tirapazamine

7.1 Introduction

A unique feature of many cancerous tumors is the existence of hypoxic regions, that is, regions of oxygen-poor cells.\textsuperscript{1-3} Such cells are often quite resistant to more conventional forms of antitumor treatment such as radiotherapy and chemotherapy.\textsuperscript{4} Consequently, there has been considerable effort to identify potential antitumor drugs that specifically target such cells. One such class of potential hypoxia-specific drugs is the benzotriazine di-\(N\)-oxides of which a particularly promising candidate is 3-amino-1,2,4-benzotriazine-1,4-dioxide,\textsuperscript{5-7} or tirapazamine (shown in Scheme 7.1).

\begin{center}
\includegraphics[width=0.5\textwidth]{scheme71.png}
\end{center}

Scheme 7.1 Schematic illustration of the activation of tirapazamine by one-electron enzymatic reduction.

Tirapazamine has been the subject of extensive experimental investigations,\textsuperscript{8-11} and has been shown to derive its biological activity from its ability to cause DNA
cleavage in hypoxic tumor cells. It is known that in vivo, under hypoxic conditions, tirapazamine may undergo an enzymatic one-electron reduction to form the activated intermediate 2, see Scheme 7.1. It has been proposed that 2 may abstract hydrogen directly from DNA. However, it has been found that 2 decomposes to 3 releasing a hydroxyl radical, and it has been suggested that both 2 and \( \cdot \text{OH} \) are involved in DNA cleavage. In either case, a sugar-C\(_1\)' radical is formed which then reacts further to give the corresponding deoxyribonolactone (Scheme 7.2) and the DNA strand is cleaved. However, radical-mediated DNA cleavage depends on molecular oxygen. Thus, the involvement of 2 and \( \cdot \text{OH} \) does not explain the remarkable selectivity of tirapazamine towards hypoxic tumor cells.

![Scheme 7.2 Schematic illustration of the product distribution for the reaction of tirapazamine with a sugar-C\(_1\)' DNA radical.](image)

Experimentally, it has been suggested that for DNA exposed to \( \gamma \)-radiolysis, the presence of tirapazamine increases the amount of strand cleavage. Hence, it has been proposed that tirapazamine may act as a molecular oxygen surrogate or mimic in radical-
mediated DNA damage reactions. Hwang et al.\textsuperscript{10} have performed a systematic experimental study of the reaction of tirapazamine with sugar-C\textsubscript{1}' DNA radicals. From oxygen isotope labelled product analysis of the final deoxyribonolactone it was found that the reaction proceeds predominantly by direct transfer of an N-oxide oxygen, in particular the O\textsubscript{4} oxygen, of the tirapazamine moiety to the sugar-C\textsubscript{1}' radical. Only a minor amount was derived from direct attack of H\textsubscript{2}O at the sugar-C\textsubscript{1}' position (Scheme 7.2).

For the observed predominant direct oxygen transfer, Hwang et al. and coworkers\textsuperscript{10} proposed the formation of the sugar-drug covalent adduct intermediate 5, which may then react further by two possible mechanisms (see Scheme 7.3). In one mechanism, the cross-linked N—O bond of intermediate 5 cleaves to produce an alkoxy radical. Subsequent reduction of the alkoxy radical forms the sugar-derived species 6 which can then hydrolyse to produce the corresponding deoxyribonolactone which leads to cleavage of the DNA strand. In the alternative mechanism, an initial reduction of 5 occurs to give the neutral intermediate 7. The cross-linked N—O bond then breaks, and hydrogen transfer to the oxygen of the now cleaved N—O bond gives the sugar-derived species 6 which, as described above, can then react further to give deoxyribonolactone and DNA strand cleavage. However, experiments do not differentiate between the two proposed reaction mechanisms.
Scheme 7.3 Schematic illustration of the experimentally proposed mechanisms for the reaction of the sugar-C1' radical with tirapazamine.

For the minor pathway, Hwang et al.\textsuperscript{10} suggested that it may indicate an electron-transfer mechanism by which the sugar-C1' radical activates tirapazamine, i.e., via formation of a sugar-C1' cation intermediate. However, the exact mechanisms by which such an electron transfer may occur were unclear. It has been suggested\textsuperscript{8} that the minor
pathway may proceed via the carbon-carbon covalent adduct intermediate 4, or that the reaction may possibly occur via the carbon-oxygen covalent adduct intermediate 5 (see Scheme 7.3).\textsuperscript{10}

The reliability and computational efficiency of DFT methods offers an attractive theoretical approach to gain insight into large biological systems. Numerous biological radicals derived from the DNA bases,\textsuperscript{13a-d} sugar moiety\textsuperscript{13e,14} and amino acids\textsuperscript{15} have been extensively studied using density functional theory. In the present study, density functional theory methods have been used to investigate the possible mechanisms by which tirapazamine may act as a surrogate for molecular oxygen in radical-mediated DNA cleavage.\textsuperscript{16} At the levels of theory employed in the present study, the reactions of 2'-deoxyuridin-1'-yl radical with tirapazamine were modelled by 8 and 9, respectively (Figure 7.1).

![Chemical Structures](image)

Figure 7.1 The model systems 8 and 9 used in place of 2'-deoxyuridin-1'-yl radical and tirapazamine, respectively. Selected optimized parameters of the neutral and cationic forms of 8 and the neutral and anionic forms of 9 are also shown.
7.2 Computational Methods

All geometry optimizations were performed with the B3LYP hybrid density functional in conjunction with the 6-31G(d) basis set using the GAUSSIAN 98 suite of programs. Harmonic vibrational frequencies and zero-point vibrational energy (ZPVE) corrections were calculated at the same level of theory. Relative energies were obtained by performing single point calculations at the B3LYP level in conjunction with the 6-311G(d,p) basis set using the above optimized geometries and with inclusion of the appropriate scaled\(^{17}\) ZPVE, i.e., B3LYP/6-311G(d,p)//B3LYP/6-31G(d) + ZPVE.

For all open- and closed-shell systems, the unrestricted (UB3LYP) and restricted (RB3LYP) B3LYP procedures were used, respectively. The symbols U and R have been neglected for simplicity.

7.3 Results and Discussion

7.3.1 Oxidation of the Sugar-C\(_1\)' Radical by Tirapazamine

Hwang et al.\(^{10}\) suggested that the sugar-C\(_1\)' radical may be oxidized by tirapazamine to form the sugar-C\(_1\)' cation. The feasibility of electron-transfer from the sugar-C\(_1\)' radical to tirapazamine was probed by comparing the calculated ionization energy of 8 and the calculated electron affinity of 9.
The optimized structures of the sugar-C\textsubscript{1}' neutral radical 8 and its cation, and of the neutral drug 9 and its anion are shown in Figure 7.1. The sugar-C\textsubscript{1}' radical centre of 8 is pyramidal by approximately 36°, while the sugar-C\textsubscript{1}' centre of the corresponding cation is planar. The shortened C—N and C—O bonds in the cation indicate the presence of strong π-electron delocalization across the O—C—N moiety. The optimized structure of 9 is a conjugated system with an almost planar structure. In the corresponding anion, however, O\textsubscript{4} protrudes out of the plane of the six-membered 1,2,4-triazine ring by approximately 4° while the amino group is pyramidal. In both neutral 9 and the anion, the two N—O bonds differ with the N\textsubscript{i}—O\textsubscript{i} bond having relatively more double bond character than the N\textsubscript{4}—O\textsubscript{4} bond.

The calculated ionization potential for the sugar-C\textsubscript{1}' radical 8 is 459.9 kJ mol\textsuperscript{-1}, while the calculated electron affinity of 9 is just 60.7 kJ mol\textsuperscript{-1}. Hence, due to the very large difference between the ionization potential of 8 and electron affinity of 9, it is unlikely that the sugar-C\textsubscript{1}' radical can be oxidized by tirapazamine alone. The effect of protonation on the ability of tirapazamine to oxidize the sugar radical was investigated by comparing the electron affinity of protonated 9 with the ionization potential of 8. The calculated proton affinity (PA) of the O\textsubscript{4} site of 9 is quite large, approximately 896.4 kJ mol\textsuperscript{-1}, suggesting that tirapazamine may be easily protonated. The calculated electron affinity of protonated 9 is 588.4 kJ mol\textsuperscript{-1}. Comparison with the calculated ionization potential (459.9 kJ mol\textsuperscript{-1}) for the sugar-C\textsubscript{1}' radical 8 suggests that protonated tirapazamine is more likely to be able to oxidize the sugar-C\textsubscript{1}' radical to produce the corresponding cation.
It must be noted, however, that the present calculations are performed without inclusion of solvent effects; they are gas-phase calculations. An experimental study\textsuperscript{18} of the pK\textsubscript{a} values of tirapazamine-related N-oxide species suggested that in fact, tirapazamine may not be protonated under physiological conditions.

7.3.2 Formation of Deoxyribonolactone via a C—C Covalent Adduct Intermediate

Possible reaction mechanisms by which the deoxyribonolactone moiety may be formed via some covalent adduct intermediate were also examined. The triazine ring of tirapazamine possesses several possible sites at which the sugar-C\textsubscript{1}' radical may attack and form a covalently cross-linked product. The mechanism for formation of a sugar-C\textsubscript{1}'—triazine-C\textsubscript{3} cross-linked intermediate was investigated and the energy profiles are schematically shown in Figure 7.2.

The addition of the drug (9) to the sugar-C\textsubscript{1}' radical (8) leads to the formation of the hydrogen-bonded complex 1a, lying 23.3 kJ mol\textsuperscript{-1} lower in energy than the initial reactants (Figure 7.2a). The C—C cross-linked product 1c can then be formed by attack of the sugar-C\textsubscript{1}' radical at the C\textsubscript{3} position of the 1,2,4-triazine ring via transition structure (TS) 1b, at a cost of 34.1 kJ mol\textsuperscript{-1}. It should be noted that TS 1b lies higher in energy than the initial reactants by 10.8 kJ mol\textsuperscript{-1}. The product 1c, which is effectively a model of species 4 in Scheme 7.3, lies 28.4 kJ mol\textsuperscript{-1} lower in energy than the initial reactants, and the radical centre is now localized on the O\textsubscript{4} N-oxide oxygen.
Figure 7.2 Schematic energy profile for the formation of (a) the carbon-carbon cross-linked product, and (b) the sugar-C₆ cation via decomposition of the complex 1c.

All attempts to locate possible transition structures for cleavage of the C—C bond of 1c by hydrolysis, i.e., by attack of H₂O at the sugar-C₆' or triazine-C₃ positions or by addition across the C₆—C₃ bond, were unsuccessful. An alternative possible mechanism
is that the C—C cross-link bond may break heterolytically to give the corresponding
sugar cation and 3-amino-1,2,4-triazine radical anion. However, as described above, the
triazine moiety has a relatively low electron affinity while that of its protonated
derivative is considerably higher. Thus, the effects of protonation on the C—C covalent
adduct intermediate 1c, more specifically protonation at the O₄ site, were examined.

Upon protonation, 1c was calculated to dissociate without a barrier to form the
complex 1d, which is illustrated schematically in Figure 7.2b. Complex 1d is an
intermolecularly hydrogen-bonded complex between the sugar-C₁' cation and what can
be thought of as the protonated derivative of the 3-amino-1,2,4-triazine anion. In other
words, protonation of the C—C covalent adduct 1c at O₄ induces an intramolecular redox
reaction, with an electron transfer from the sugar to the drug moiety and cleavage of the
sugar-C₁'—drug-C₃ bond.

Energetically, the dissociation of 1c to give 1d upon addition of a proton at the O₄
position is favoured by approximately 1133.1 kJ mol⁻¹ (not shown), indicating a large
proton affinity for 1c. At the present level of theory, the proton affinity of H₂O is
calculated to be approximately 700 kJ mol⁻¹. Thus, the considerably larger proton
affinity of 1c suggests that once formed it may be easily protonated with little or no
barrier to give 1d. As mentioned above, the present calculations neglect the effects of
solvation. However, from an experimental study¹⁸ of the pKₐ values of tirapazamine-
related radical species, the radicals were more likely to be protonated under physiological
conditions than their closed-shell parents. Furthermore, they suggested that the observed
values may be due to protonation of the N-oxide oxygen rather than at a nitrogen. The
dissociation of complex 1d to the sugar-C\textsubscript{1}' cation and drug derivative (see Figure 7.2b) is calculated to require approximately 136.7 kJ mol\textsuperscript{-1}. The inclusion of solvent effects would stabilize to a greater extent the dissociated products than 1d, thus giving a lower dissociation energy. The above results suggest that the decomposition of 1e may be an alternative indirect oxidation reaction pathway for the generation of the sugar-C\textsubscript{1}' cation.

The resulting fate of the sugar-C\textsubscript{1}' cation is still a matter of much discussion.\textsuperscript{19,20} Hence, possible reactions by which the sugar-C\textsubscript{1}' cation may react directly with H\textsubscript{2}O to give the resulting deoxyribonolactone were also investigated.

### 7.3.3 Formation of Deoxyribonolactone by Reaction of H\textsubscript{2}O with the Sugar-C\textsubscript{1}' Cation.

For the model system, the addition of a single water molecule to the sugar-C\textsubscript{1}' cation results in the formation of complex 1e, lying lower in energy by 47.1 kJ mol\textsuperscript{-1} (Figure 7.3a). The hydrolyzed product 1g is formed by the addition of the water across the C—N bond via TS 1f, at a cost of approximately 178.6 kJ mol\textsuperscript{-1}. 1g lies 19.8 kJ mol\textsuperscript{-1} higher in energy than the initial reactants. The high barrier for the hydrolysis of the sugar-C\textsubscript{1}' cation by a single water is probably due in part to the need to form a tight four-membered ring in TS 1f. Thus, the reaction of the sugar-C\textsubscript{1}' cation with two H\textsubscript{2}O molecules was considered, as one may act as a base to enhance the nucleophilicity of the other, or may assist in stabilizing transition structures or intermediates.
Figure 7.3 Schematic energy profiles for the reaction of the sugar-C$_1$ cation with (a) one water molecule and (b) with two water molecules.
Upon addition of two H$_2$O to the sugar-C$_1'$ cation, they are able to form complex 1h (Figure 7.3b), which lies lower in energy than the initial reactants by approximately 127.3 kJ mol$^{-1}$. In complex 1h, the two water molecules have formed a hydrogen-bond bridge between the amine group at C$_1'$ and with the --OH group at C$_3'$. Addition of a water across the C—N bond assisted by another water is then able to proceed via TS 1i, with a barrier of 115.6 kJ mol$^{-1}$. The final complex formed, 1j, lies approximately 50.2 kJ mol$^{-1}$ lower in energy than the initial reactants. In TS 1i it can be seen that one H$_2$O moiety acts as a proton donor to the amine N, while concomitantly acting as a proton acceptor from the H$_2$O moiety that is attacking the C$_1'$ centre (see Figure 7.3b). It should also be noted that TS 1i lies 11.7 kJ mol$^{-1}$ lower in energy than the initial reactants. Thus, it is possible for complex 1j to be formed directly from the initial reactants via TS 1i, without passing through 1h. Comparison of the above energetics of the mechanisms for hydrolysis by one and two H$_2$O molecules, also provides a very clear example of the effect of explicitly including greater solvent effects for some processes. In order to simplify the calculations performed to determine the fate of complex 1j, the complexed H$_2$O moiety in 1j was neglected, i.e., only reactions of 1g were considered (see Figure 7.4).

The C$_1'$—NH$_3$ bond of 1g may be cleaved via TS 1k with a barrier of just 11.4 kJ mol$^{-1}$ to give the complex 1l, lower in energy than 1g by 5 kJ mol$^{-1}$. The leaving NH$_3$ group may then abstract a proton from the C$_1'$—OH group to give the deoxyribonolactone···NH$_4^+$ complex 1m, lying 111.8 kJ mol$^{-1}$ lower in energy than 1g. At the present level of theory, no transition structure interconnecting 1l and 1m could be
located (as indicated by the hashed line in Figure 7.4). However, in 1j the NH$_3$ moiety is only weakly complexed to the sugar-C$_{1'}$ centre (r(C$_{1'}$−NH$_3$) = 2.702 Å) and is almost perpendicular to the −OH$^+$ group (∠N-C$_{1'}$-OH = 90.8°). Thus, it is most likely that any transition structure interconnecting 1l and 1m will have quite small barriers (Figure 7.4). This may also explain the difficulty in locating the transition structure.

![Schematic energy profile for formation of deoxyribonolactone from the protonated sugar-C$_{1'}$ hydroxylated derivative.](image)

The present calculations show the reaction of the model system cation with one and two water moieties. In DNA itself, the reactions may differ due to the presence of more solvent and the nature of the nucleobase. Such calculations are not practical at the present level of theory. However, the end result of the reaction of the cation with water will be the same: formation of the deoxyribonolactone.
7.3.4 Formation of Deoxyribonolactone via a C—O Covalent Adduct Intermediate.

The predominant mechanism for formation of the deoxyribonolactone moiety was proposed to occur via direct attack, and transfer, of an N-oxide oxygen of tirapazamine, see Introduction (Scheme 7.3). In particular, it was proposed to occur by formation of a bond between the sugar-C₁' radical and tirapazamine via O₄, 5, which could then react further to eventually give deoxyribonolactone. However, no such covalent adduct intermediate was experimentally observed and furthermore, the exact mechanisms by which it may eventually form deoxyribonolactone were unclear. Thus, the mechanism for formation of the proposed C₁'—O₄ covalent adduct intermediate was investigated.

As mentioned previously, when the sugar-C₁' radical and drug interact they can form the intermolecularly hydrogen-bonded complex 1a lying 23.3 kJ mol⁻¹ lower in energy (Figure 7.5). The O₄ N-oxide oxygen can then attack the sugar-C₁' radical site via TS 2a, at a cost of just 16.3 kJ mol⁻¹, to give the C₁'—O₄ covalent adduct intermediate 2b which lies considerably lower in energy by approximately 67.4 kJ mol⁻¹.

Possible reactions of the C—O covalent adduct intermediate 2b were then examined. In particular, formation of the deoxyribonolactone moiety via homolytic cleavage of the O₄—N₄ bond (mechanism A) and via addition of hydrogen (H⁺) to the drug-C₃ radical site of 2b (mechanism B) was investigated. These two mechanisms are the same as those proposed by Hwang et al. (see Scheme 7.3). In addition, considering
the previous findings for the C—C covalent adduct intermediate 1c, the effects of protonation on 2b (mechanism C) were also examined.

Figure 7.5 Schematic energy profile for the formation of the carbon-oxygen cross-linked intermediate.

The schematic energy profile obtained for mechanism A is shown in Figure 7.6a. The O₄—N₄ bond of 2b may cleave homolytically via TS 2c at a cost of just 5.6 kJ mol⁻¹, to give complex 2d, lying lower in energy than 2b by 112.6 kJ mol⁻¹. Complex 2d is an intermolecularly hydrogen-bonded complex between the alkoxy radical derivative (2e) of the sugar-C₄' radical and the drug metabolite (2f). The small barrier to dissociation of 2e may suggest why the C—O covalent adduct intermediate 5 (see Scheme 7.3) was not observed experimentally. 2f corresponds to the model equivalent of 3 (see Scheme 7.1). It requires just 31.0 kJ mol⁻¹ for 2d to dissociate completely to 2e and 2f.
Figure 7.6 Schematic energy profile for (a) mechanism A, (b) for mechanism B (part A) and (c) mechanism B (part B) (see text).
The calculated hydrogen affinity of the alkoxy radical 2e is quite large, approximately 420.5 kJ mol^{-1}. This suggests that such a radical species may relatively easily obtain a hydrogen to form the sugar-C_1' hydroxylated species, 6 in Scheme 7.3. Once the hydroxylated species is formed it may then react further to give the corresponding deoxyribonolactone, with concomitant cleavage of the DNA backbone.

For the proposed^{10} alternative, mechanism B, the calculated hydrogen affinity for the drug-C_3 centred radical 2b is just 241.3 kJ mol^{-1}. This is quite a low hydrogen affinity on account of the enhanced stability of the ring-carbon centred radical. Furthermore, it is significantly lower than that of the alkoxy radical 2e. This suggests that such a process may encounter a considerable energy barrier, as predicted by the empirical relationships of Evans-Polanyi and Semenov.^{21} For completeness, however, the reactions that the hydrogenated derivative 7 (see Scheme 7.3) may undergo to give the deoxyribonolactone moiety was considered. The addition of hydrogen (H^+) to the drug-C_3 radical centre of 2b gives 2g in Figure 7.6b. The schematic energy profiles obtained for further reactions of 2g are shown in Figure 7.6b (part A of mechanism B) for the formation of a sugar-C_1' hydroxylated derivative 2j, and in Figure 7.6c (part B of mechanism B) for the formation of the sugar alkoxy radical 2e. In Figure 7.6b, an intermolecularly hydrogen-bonded complex 2i between the sugar-C_1' hydroxylated derivative (2j) and 2f can form, lying lower in energy by 280.3 kJ mol^{-1}! However, this reaction proceeds via TS 2h at a considerable cost of 176.3 kJ mol^{-1}. Thus, even if 2g were formed, it is unlikely that such a reaction will occur. Alternatively, the O_4—N_4 bond of 2g may undergo homolytic cleavage at a cost of 149.7 kJ mol^{-1} to give the
alkoxyl radical (2e) and the radical drug derivative 2k (Figure 7.6c). While this alternative mechanism still requires a considerable amount of energy, it is significantly less than that required for formation of 2f from 2g. The alkoxy radical formed can then react as described previously to eventually form deoxyribonolactone.

The protonation of 2b (mechanism C) can conceivably occur at several sites on the drug moiety, in particular at the O₁ or O₄ positions. Protonation at the bridging O₄ position results in cleavage of the O₄—N₄ bond to give the sugar-C₁' hydroxylated derivative 2j, while protonation at the O₁ position results in a shortening of the O₄—N₄ bond and a lengthening of the sugar-C₁'—O₄ bond of 2b, i.e., emphasises the sugar–drug nature of 2b. As might be expected, the calculated proton affinity of O₁ (1029.0 kJ mol⁻¹) is higher than that of the bridging O₄ (975.6 kJ mol⁻¹). Thus, while protonation of 2b is not expected to enhance the ability of tirapazamine to transfer an oxygen to the sugar-C₁' radical, it is not expected to inhibit or lead to radically different reaction mechanisms than those already considered above.

7.4 Conclusions

Possible mechanisms by which tirapazamine may react with DNA sugar-C₁' radicals to form the sugar derivative deoxyribonolactone with concomitant cleavage of the DNA strand, have been investigated by use of the B3LYP density functional theory method.
Experimentally proposed mechanisms involving ionization of the sugar-C$_1^\prime$ radical by tirapazamine were investigated. The present results predict the electron affinity of tirapazamine to be considerably lower than the ionization energy of the sugar-C$_1^\prime$ radical. Thus, it is unlikely that the sugar-C$_1^\prime$ radical can be oxidized by tirapazamine. However, the electron affinity of the protonated form of tirapazamine is estimated to be greater than the ionization energy of the sugar-C$_1^\prime$ radical. Hence, protonation of tirapazamine may be a prerequisite for it to oxidize the sugar-C$_1^\prime$ radical.

The proposed formation of a sugar-C$_1^\prime$—drug-C$_3$ covalent adduct intermediate 4 is found to occur with a modest barrier. Protonation of the drug moiety of 4 is predicted to result in heterolytic cleavage of the C—C bond, without a barrier, to give the sugar-C$_1^\prime$ cation.

In both of these above mechanisms, the resulting sugar-C$_1^\prime$ cation will react with solution H$_2$O to give deoxyribonolactone with inclusion of an oxygen from H$_2$O. At the present level of theory, it is impossible to distinguish which mechanism may be responsible for the experimentally observed minor pathway; the conversion of a sugar-C$_1^\prime$ radical to deoxyribonolactone by incorporation of an oxygen from a solution H$_2$O molecule. It is possible that both mechanisms occur to different degrees.

The energetically preferred pathway, in agreement with the experimental observations, occurs via direct attachment of the O$_4$ N-oxide oxygen of tirapazamine at the sugar-C$_1^\prime$ radical centre. This is predicted to be able to occur without a barrier. The transfer of the oxygen O$_4$ can then be completed by homolytic cleavage of the O$_4$—N$_4$ bond, which proceeds with a very small barrier of less than 6 kJ mol$^{-1}$. The resulting
sugar-alkoxyl radical derivative can then relatively easily obtain a hydrogen to form the sugar-C$_1'$ hydroxylated derivative, which can then react further to give the deoxyribonolactone. The present calculations suggest this to be the preferred mechanism for formation of the experimentally observed major product: formation of the deoxyribonolactone by incorporation of an N-oxide oxygen. The experimentally proposed alternative, involving addition of H* to the drug-C$_3$ position of the sugar-C$_1'$—O$_2$-drug intermediate 5, is predicted to not occur due to the low hydrogen affinity of 5.

References


Concluding Remarks and Future Directions

The computational studies in this thesis have focused on the hyperfine coupling constants and reaction mechanisms of biological radicals. This chapter summarizes the global conclusions of the thesis and highlights some possible avenues for future research.

8.1 Amino Acid-derived Radicals

The current studies on the hyperfine coupling constants of amino acid-derived radicals presented a systematic approach for theoretical characterization of the identities of the radicals observed from electron spin resonance spectroscopy. The diversity of the structures of amino acid-derived radicals presented in Chapters 3, 4 and 5 clearly reveals that the complex ESR spectra for a given radical arise from various possible conformations. The computational scheme of density functional theory combined with the Onsager model has been validated for modelling the zwitterionic forms of amino acid-derived radicals. The reliability of density functional theory in predicting the hyperfine coupling constants has been demonstrated by the excellent agreement between the calculated values and the accurate experimental data available for the amino acid derived-radicals. Comprehensive theoretical assignment of the observed hyperfine tensors for R2 of glycine (Chapter 3) and for R1^A, R1^P and R5 of hydroxyproline (Chapter 5) are complementary to previous experimental studies. The size and
complexity of the hydroxyproline-derived radicals illustrates the usefulness and power of theoretical predictions.

Biological radical systems are characterized by specificity in structure. Quantum chemical calculations on isolated amino acid-derived radicals of the gas phase can only go as far as shown in this thesis to describe the origin of the structural specificity. The cases where theory and experiment were not in as close agreement, such as NH₂C⁺HCOOH (Chapter 3) and R₂C⁺ of hydroxyproline (Chapter 5), illustrate the limitations of calculations based on the assumption of small models in the gas phase.

A possible future extension of the present study on the hyperfine coupling properties of amino acid-derived radicals could be the validation of computational schemes for describing the crystal effects on the conformations and therefore, the hyperfine coupling constants of a target radical embedded in extended model systems. Computationally, the DFT + SCRF strategy¹ or the ONIOM method² are potentially effective. With the DFT + SCRF strategy for an extended model, the most important neighbour molecules of the target are explicitly included and treated at the same electronic level of theory as applied to the target, while the macroscopic environmental effects are incorporated into the SCRF method. In the ONIOM method, an essentially complete model, such as a unit cell, can be used. However, the large model system is divided into different layers according to their contributions to the properties in question, and the target layer is treated with a high level of theory, while the other layers are modelled with lower levels of theory to reduce computational cost. Such computational
strategies for investigations of biological systems in condensed phases are being tested on prototypical applications.

8.2 Mechanisms of Biological Radical Reactions

The mechanistic studies of DNA—protein cross-links (Chapter 6), and the modelling of the actions of tirapazamine (Chapter 7) have provided great insight into the reactions of biological radical systems. The advantages of computational chemistry are illustrated by the quantitative predictions of molecular structures, charge and spin distributions, energy profiles and activation energies. For example, the advantages of theoretical studies can be seen in the concerted hydrogen transfer mechanism (Chapter 6); without obtaining the optimized structure of the intermediate product 1a, chemists were unlikely to foresee such a alternative reaction pathway. Hence, as experimental investigations often provide only indirect information, a complete picture of the reaction mechanisms of interest can be drawn with the tools of computational chemistry.

The study of the cross-linking mechanisms between cytosine and tyrosine can be extended to other cross-linking systems such as thymine with tyrosine or lysine in nucleohistones. As the formation of tyrosyl radicals has been recognized as a typical feature of oxidative stress in physiological conditions, and the coupling between tyrosyl radicals is believed to be a prime marker of oxidative stress in many diseases, further research on the reaction mechanisms of the reactions between tyrosyl radicals is of great importance.
The present study of tirapazamine represents the first computational investigation of an antitumor drug at such a high level of theory. As described in Chapter 7, the energetically preferred pathway occurs via direct attachment of the O₄ N-oxide oxygen of tirapazamine to the sugar-C₁′ radical centre. The transfer of the O₄ oxygen can then be completed by homolytic cleavage of the O₄—N₄ bond. In addition to elucidating the reaction mechanism for such an important antitumor drug, such studies also give greater insight into the chemistry of N-oxide compounds and thus potentially other drugs.

A possible future extension of the present study on tirapazamine could be a systematic study of related representatives of N-oxide family compounds. In particular, the mono-N-oxide metabolites 1 and 2 shown in Figure 8.1 are of particular interest. The detection of 1 and 2 has suggested that both of the N-oxide oxygens of tirapazamine possess similar reactivity with regards to cleavage of DNA strands. A complete computational study of one N-oxide oxygen of tirapazamine has been presented in the thesis. The reactivity of the other oxygen could be investigated. Of 1 and 2, the major metabolite is 1. Importantly, 1 and 2 are more reactive for inducing DNA strand cleavage than the parent drug. However, the possible reaction mechanisms by which this may occur are uncertain. Moreover, 1 is found to react with the sugar-C₁′ radical in single strand DNA three times faster than 2, however, 2 is two times more efficient than 1 in double strand DNA. Thus, further theoretical work could be carried out for exploring this related chemistry.
3-amino-1,2,4-benzotriazine-1-oxide  3-amino-1,2,4-benzotriazine-4-oxide

Figure 8.1 The metabolites of tirapazamine.

8.3 Outlook

At the present stage, high-level electronic structure calculations have only just started to be employed for solving the problems of biological radical systems at a realistic scale. Its best applications have been on the prediction of molecular properties, such as hyperfine coupling constants. Modelling the configurations of biological radical systems with inclusion of the effects of the environment from hydrogen bonding, van der Waals and steric interactions remains a great challenge to theoretical studies. However, an increasing amount of work with model systems at the DFT level of theory has appeared in the literature.8,9

The work presented in this thesis clearly illustrates the strengths of density functional theory in modelling the properties and reactions of biological radical systems. There is a potentially endless number of interesting questions to be answered for biological radicals. With the advancement of new methodologies in computational
chemistry and the development of faster computer architectures, the dream of reliable and accurate large-scale quantum mechanical calculations on biological radical systems will increasingly become a reality.

References


