# Radiostereometric Analysis Origin Styles: Their Impact on the Accuracy and Precision in the Assessment of Spinal Fusion Success 

By

## Alan J. Spurway

Submitted in partial fulfillment of the requirements
for the degree of Master of Applied Science
at

Dalhousie University

Halifax, Nova Scotia
April 2012

## DALHOUSIE UNIVERSITY

School of Biomedical Engineering

The undersigned hereby certify that they have read and recommend the Faculty of Graduate Studies for acceptance a thesis entitled "Radiostereometric Analysis Origin Styles: Their Impact on the Accuracy and Precision in the Assessment of Spinal Fusion Success" by Alan J. Spurway in partial fulfillment of the degree of Master of Applied Science.

Dated: April 24, 2012

Supervisor:

Readers:

External Examiner:

## DALHOUSIE UNIVERSITY

Date: April 24, 2012


#### Abstract

AUTHOR: Alan J. Spurway TITLE: Radiostereometric Analysis Origin Styles: Their Impact on the Accuracy and Precision in the Assessment of Spinal Fusion Success

DEPARTMENT OR SCHOOL: School of Biomedical Engineering DEGREE: MASc CONVOCATION: October YEAR: 2012


Permission is herewith granted to Dalhousie University to circulate and to have copied for non-commercial purposes, at its discretion, the above title upon request of individuals or institutions. I understand that my thesis will be electronically availible to the public.

The author reserves other publication rights, and neither thesis nor extensive extracts from it may be printed or otherwise reproduced without the author's written permission.

The author attests that permission has been obtained for the use of any copyrighted material appearing in the thesis (other than the brief excerpts requiring only proper acknowledgement in scholarly writing), and that all such use is clearly acknowledged.

## Table of Contents

LIST OF TABLES ..... viii
LIST OF FIGURES ..... x
ABSTRACT ..... xv
LIST OF ABBREVIATIONS USED ..... xvi
GLOSSARY ..... xviii
ACKNOWLEDGEMENTS ..... xxi
CHAPTER 1 - INTRODUCTION ..... 1
1.1 BACKGROUND ..... 1
1.1.1 Spinal Anatomy and Physiology ..... 1
1.1.2 Adolescent Idiopathic Scoliosis ..... 4
1.1.3 Medical Treatment ..... 12
1.1.4 Radiostereometric Analysis ..... 20
1.1.5 RSA Markers ..... 30
1.1.6 Migration Assessment ..... 33
1.2 Previous Work ..... 40
1.2.1 Previous Project Outcomes ..... 40
1.2.2 Previous Limitations ..... 45
CHAPTER 2 - THESIS OBJECTIVES ..... 48
2.1 ObJective \#1: RSA Simulation Precision Validation ..... 48
2.2 Objective \#2: Assessment of Novel RSA Origin Styles Used for Spinal Fusion Success Analysis ..... 49
CHAPTER 3 - THESIS OBJECTIVE \#1: RSA SIMULATION PRECISION VALIDATION ..... 51
3.1 INTRODUCTION ..... 51
3.2 Simulation Precision Validation Methodology ..... 53
3.2.1 Computer Simulated Spine Model ..... 53
3.2.2 Radiostereometric Simulation ..... 63
3.2.3 Simulated RSA Environment ..... 66
3.2.4 Radiostereometric Analysis ..... 72
3.2.5 Simulation Precision Validation ..... 79
3.3 Simulation Precision Validation Results ..... 95
3.3.1 Image Simulation ..... 95
3.3.2 Precision Results ..... 99
3.3.3 Precision Comparison ..... 100
3.4 SimULATION PRECISION VALIDATION DISCUSSION ..... 104
3.4.1 Spinal Fusion Precision Comparison ..... 108
3.4.2 Limitations ..... 109
3.4.3 Conclusion ..... 112
CHAPTER 4 - THESIS OBJECTIVE \#2: ASSESSMENT OF NOVEL RSA ORIGIN STYLES USED FOR SPINAL FUSION SUCCESS ANALYSIS ..... 113
4.1 InTRODUCTION ..... 113
4.1.1 RSA Origin Styles ..... 115
4.2 Origin Style Assessment Methodology ..... 123
4.2.1 Accuracy Assessment ..... 123
4.2.2 Precision Assessment Methodology. ..... 134
4.3 Origin Style Assessment Results ..... 138
4.3.1 Accuracy Assessment Results ..... 138
4.3.2 Precision Assessment Results ..... 149
4.4 Origin Style Assessment Discussion ..... 163
4.4.1 Origin Style Assessment ..... 166
4.4.2 Origin Style Selection ..... 172
4.4.3 Limitations ..... 176
4.4.4 Conclusion ..... 177
CHAPTER 5 - DISCUSSION ..... 178
5.1 THESIS IMPACT ..... 178
5.1.1 RSA Research ..... 178
5.1.2 Spinal Fusion Assessment. ..... 180
5.2 LIMITATIONS ..... 185
5.2.1 Simulation Limitations. ..... 185
5.3 FUTURE WORK ..... 187
5.3.1 Image Simulation Improvements ..... 187
5.3.2 Complete Simulation Validation. ..... 188
5.3.3 Patient Specific Anatomical Information. ..... 189
5.3.4 Vertebral Marking Protocols. ..... 191
5.4 SUMMARY AND CONCLUSION ..... 193
BIBLIOGRAPHY ..... 195
APPENDIX A - CAD DRAWINGS ..... 202
APPENDIX B - THESIS COORDINATE SYSTEMS ..... 206
B. 1 VERTEBRAL COORDINATE SYSTEMS. ..... 206
B. 2 T8 Rotational Coordinate System ..... 207
B. 3 Spinal Coordinate System ..... 208
B.3.1 Precision Movement Coordinate Systems ..... 209
B. 4 RSA Origin Style Coordinate Systems ..... 211
B.4.1 Caudal Coordinate System ..... 212
B.4.2 Apex Coordinate System. ..... 213
B.4.3 Dual Coordinate System. ..... 214
B. 5 RSA COORDINATE SYSTEM ..... 215
APPENDIX C - SIMULATION PROCESS ..... 217
C. 1 Programs Use ..... 217
C. 2 RSA SETUP ..... 217
C. 3 Model Construction and Placement ..... 219
C. 4 PLACEMENT IN THE RSA ENVIRONMENT ..... 220
C. 5 FILE CONVERSION ..... 221
C. 6 POV-RAY PROCESSING ..... 222
C. 7 RS Assessment ..... 224
APPENDIX D - PROGRAMMING CODE ..... 225
D. 1 POV-RAY CODE ..... 225
D.1.1 RSA Image Code ..... 225
D.1.2 Material Attenuation Properties. ..... 232
D. 2 MATLAB CODE. ..... 233
D.2.1 RSA Calculations - Global Reference Frame ..... 233
D.2.2 Apex Rotation Calculation ..... 241
D.2.3 LocalMigration Function ..... 244
APPENDIX E - TABULATED DATA ..... 247
E. 1 Simulation Precision Validation Data ..... 247
E. 2 Precision Validation Calculations ..... 254
E. 3 ACCURACY DATA ..... 258
E. 4 Prediction Interval Accuracy Calculations ..... 309
E. 5 PRECISION DATA ..... 319
E. 6 Precision Calculations ..... 330
APPENDIX F - PLOTS ..... 333
F. 1 Simulation Validation ..... 333
F.1.1 Check for Normalcy. ..... 333
F.1.2 Variance Comparison ..... 349
F. 2 Accuracy Plots ..... 357
F.2.1 X Accuracy ..... 358
F.2.2 Y Accuracy ..... 359
F.2.3 Z Accuracy ..... 360
F.2.4 Rx Accuracy ..... 361
F.2.5 Ry Accuracy ..... 362
F.2.6 Rz Accuracy ..... 363
F.2.7 Translational Accuracy Comparison ..... 364
F.2.8 Rotational Accuracy Comparison ..... 364
F. 3 Precision Plots. ..... 365
F.3.1 Check for Normalcy. ..... 365
F.3.2 Variance Comparison ..... 389
APPENDIX G - ORIGINAL THESIS WORK ..... 399
APPENDIX H - PERMISSION FOR PUBLICATION ..... 402

## List of Tables

Table 1.1: Scoliosis Population Demographics ..... 5
Table 1.2: Probability of Curve Progression Dependant on Detection Age and Curve MAGNitude ..... 12
TABLE 1.3: SUMMARY OF THE ACCURACY RESULTS FROM MADANAT ET AL. (2007) [59] ..... 36
TABLE 1.4: PRECISION RESULT SUMMARY FROM ALLEN ET AL (2004) [63] ..... 39
TABLE 1.5: AVERAGE ACCURACY RESULTS REPORTED BY FRANCIS (2009) [27] ..... 45
Table 2.1: Limits of Clinical Significance ..... 50
TABLE 3.1: ACRONYMS USED FOR ANATOMICAL DIMENSIONS FOR THE VERTEBRAL MODEL ..... 55
TABLE 3.2: ANATOMICAL MEASUREMENTS OF THE SIMULATED VERTEBRAL MODELS ..... 55
TABLE 3.3: SPECIFICATIONS OF THE SIMULATED SPINE MODEL ..... 57
TABLE 3.4: PEDICLE SCREW SIZES USED IN THE SIMULATED SPINAL MODEL ..... 59
TABLE 3.5: LOCATION OF RSA RIGID BODY MARKERS WITHIN THE VERTEBRAL MODELS . ..... 61
TABLE 3.6: Positions of the centers of the RSA Rigid body markers located within the VERTEBRAL MODELS ..... 62
Table 3.7: Simulated Attenuation Coefficients ..... 71
TABLE 3.8: PEDICLE SCREW SIZES USED IN THE SIMULATED SPINAL MODEL ..... 82
TABLE 3.9: NOMINAL DIMENSIONS OF THE PHANTOM MODEL COMPARED TO THOSE OF THE FULL-SIZE SIMULATED SPINAL MODEL ..... 83
TABLE 3.10: LOCATIONS OF THE RSA MARKERS AS DETERMINED FROM THE ASSEMBLED PHANTOM CT SCAN ..... 86
TABLE 3.11: GLOBAL MOVEMENTS OF THE FUSION MODEL ..... 91
Table 3.12: REGIONS OF InTEREST FOR THE PHYSICAL PHANTOM IMAGE ASSESSMENT ..... 95
Table 3.13: Physical Image Properties ..... 96
Table 3.14: Regions of Interest in the Simulate Reference Image ..... 97
Table 3.15: Simulated Image Properties ..... 98
Table 3.16: Superior Precisions generated by the Phantom and Simulated model ASSESSMENTS ..... 99
Table 3.17: Inferior Precisions generated by the Phantom and Simulated model ASSESSMENTS ..... 100
TABLE 3.18: DISTRIBUTION OF THE PRECISION DATASETS ..... 101
TABLE 3.19: SUMMARY OF THE RESULTS OF THE ASSESSMENT OF EQUAL VARIANCE BETWEEN THE PHYSICAL AND SIMULATED MODELS. ..... 103
TABLE 4.1: MANIPULATIONS USED TO ASSESS TRANSLATIONAL ACCURACY OF ONE CARDINAL DIRECTION ..... 127
TABLE 4.2: ROTATIONS INDUCED DURING ROTATIONAL ACCURACY ASSESSMENT ..... 129
Table 4.3: Translational and Rotational Limits of Clinical Significance. ..... 133
TABLE 4.4: GLOBAL MOVEMENTS USED TO ASSESS SYSTEM PRECISION ..... 135
TABLE 4.5: SUPERIOR AND INFERIOR MIGRATION SETS USED IN THE THREE ORIGIN STYLES. ..... 138
Table 4.6: Migration data recorded for the Superior aspect of the Caudal Origin Style UNDERGOING A SIMULATED FAILURE OF THE SUPERIOR SECTION OF THE SPINE ..... 139
Table 4.7: Accuracy in the X Direction calculated for the Caudal Origin Style. ..... 140
TABLE 4.8: TRANSLATIONAL ACCURACIES OF THE THREE PRINCIPLE DIRECTIONS OF THE THREE ORIGIN styles compared to the Limits of Clinical Significance ..... 141
TABLE 4.9: CALCULATED ROTATIONAL ACCURACIES OF THE THREE ORIGIN STYLES ..... 143
Table 4.10: MEASUREMENT BIAS OF THE THREE ORIGIN STYLES. ..... 148
Table 4.11: Bias Error Percentage of respective Limit of Clinical Significance ..... 148
Table 4.12: MIGRATING AND ORIGIN VERTEBRAE OF THE TWO ASPECTS OF PRECISION FOR EACH ORIGIN STYLE ..... 149
TABLE 4.13: PRECISION DATA FOR THE SUPERIOR ASPECT ..... 150
Table 4.14: Precision Outcomes for the Inferior Aspect ..... 151
TABLE 4.15: ASSESSMENT OF THE NORMALCY OF THE SUPERIOR PRECISION DATASETS FOR EACH PRINCIPAL DIRECTION ..... 154
TABLE 4.16: ASSESSMENT OF THE NORMALCY OF THE INFERIOR PRECICION DATASETS FOR EACH PRINCIPAL DIRECTION ..... 154
TABLE 4.17: SUMMARY OF THE STATISTICAL OUTCOME OF THE PRECISION COMPARISON TESTS. ..... 156
Table 4.18: Effective Dose Tissue Weighting Factors. ..... 175

## List of Figures

Figure 1.1: ANTERIOR VIEW OF A NORMAL ADULT SPINE ..... 1
Figure 1.2: SAGittal curvatures of the spine ..... 2
Figure 1.3: COMMON STRUCTURES OF THE VERTEBRAE. ..... 4
Figure 1.4: Cobb Measurement of the Scoliotic Curvature ..... 8
Figure 1.5: Summary of the Lenke Curve Classification ..... 10
Figure 1.6: Posterior Spinal Fusion Implants ..... 14
Figure 1.7: Post-OPERATIVE DIAGNOSTIC IMAGING AND ASSESSMENT TREE ..... 17
FIGURE 1.8: PARTS OF A MODERN RSA SYSTEM ..... 22
Figure 1.9: RSA Imaging Set-ups ..... 23
Figure 1.10: ObJECT MAGNIFICATION DEPENDANT ON DISTANCE FROM DETECTOR PLANE ..... 28
Figure 1.11: DEFINITION of THE CROSSING LINE DISTANCE ..... 31
Figure 1.12: Previously developed simulation process ..... 41
Figure 1.13: The Caudal Origin Style utilized by Francis (2009) [27] ..... 42
Figure 1.14: Marker Placement Protocol ..... 44
Figure 1.15: The Apex and Dual Origin Styles for measuring intervertebral migration ..... 47
Figure 3.1: ORTHOGONAL VIEWS OF THE THORACIC VERTEBRA ..... 54
Figure 3.2: CAD model of the T8 vertebra. ..... 56
Figure 3.3: Dimensions and Coordinate System of the assembled Full Size CAD simulated SPINAL MODEL ..... 58
Figure 3.4: Monoaxial pedicle screw used in the L1 vertebra. ..... 59
Figure 3.5: Placement of the \#4 RSA marker in the T4 VErtebra ..... 61
Figure 3.6: AXIAL VIEW OF T8 VERTEBRA SHOWING THE MARKER PLACEMENT WITHIN THE VERTEBRAE. ..... 62
Figure 3.7: RSA Suite at the Halifax Infirmary ..... 63
Figure 3.8: Alignment of the RSA and Spinal Coordinate Systems. ..... 65
Figure 3.9: Model spine in the CAD RSA Environment ..... 67
Figure 3.10: RSA Simulation Process as developed by Francis (2009) [27] ..... 70
Figure 3.11: SURFACE ATTENUATION TECHNIQUE COMPARED TO A PHANTOM MODEL IMAGE ..... 71
FIGURE 3.12: LINEAR ATTENUATION SIMULATION METHOD COMPARED TO A PHANTOM MODEL ..... 72
Figure 3.13: Sample Data output from the MB-RSA software ..... 73
Figure 3.14: Process flow chart of the parallel simulation precision validation. ..... 80
FIGURE 3.15: Modified T8 VERTEBRAL MODEL ..... 81
Figure 3.16: Nominal dimensions and Coordinate System of the Phantom Spinal Model. ..... 83
Figure 3.17: Phantom model on its Plexiglas backing ..... 84
FIGURE 3.18: A SLICE FROM THE CT SCAN PERFORMED ON THE ASSEMBLED PHANTOM MODEL SHOWING THE T8 VERTEBRAL MODEL AND IMPLANTED COMPONENTS ..... 85
Figure 3.19: Simulated Model Marker Distribution ..... 87
Figure 3.20: Comparison of Physical and Simulated images of the L1 vertebral models ..... 88
Figure 3.21: Translational Precision Movement ..... 89
Figure 3.22: Rotational Precision Movement ..... 90
FIGURE 3.23: ETCHED PHANTOM PRECISION ROTATION CENTER. ..... 91
Figure 3.24: Physical Phantom Reference Image Pair with assessed Regions of Interest ..... 96
Figure 3.25: Simulated Phantom Left Reference Image with assessed Regions of Interest ..... 97
Figure 3.26: Calculated Superior Precision ..... 99
Figure 3.27: Calculated Inferior Precision. ..... 100
FIGURE 3.28: TEST FOR EQUAL VARIANCE OF THE RX DIRECTION FOR THE INFERIOR ASPECT. ..... 102
Figure 3.29: Simulated Photon Attenuation Techniques ... ..... 106
Figure 3.30: Magnification Blurring ..... 107
Figure 3.31: A comparison of T4 vertebrae showing the X-ray attenuation techniques ..... 112
Figure 4.1: PROCESS FLOW CHART OF THE TESTING OF THE THREE ORIGIN STYLES ..... 114
Figure 4.2: The Caudal Origin Style and Caudal Coordinate System ..... 116
Figure 4.3: The Apex Origin Style and associated Apex Coordinate System ..... 118
Figure 4.4: Comparison of the image sets required for the Caudal Origin Style and Apex Origin Style ..... 119
Figure 4.5: The Dual Origin Style and Dual Coordinate Systems ..... 122
FIGURE 4.6: EXAMPLE SHOWING THE 95\% PREDICTION INTERVALS VERSUS 95\% CONFIDENCE INTERVALS ..... 124
FIGURE 4.7: INDUCED DISPLACEMENTS USED TO ASSESS SYSTEM TRANSLATIONAL ACCURACY ..... 125
Figure 4.8: Superior Fusion Failure Translational Accuracy Movement. ..... 126
Figure 4.9: Inferior Fusion Failure Translational Accuracy Movement ..... 126
Figure 4.10: Rotational origin of the T8 vertebra ..... 128
Figure 4.11: Rotational Accuracy Movement ..... 129
Figure 4.12: Alignment of the Migration and Reference scenes in MB-RSA ..... 131
Figure 4.13: TransLational Precision Movement ..... 134
Figure 4.14: Rotational Precision Movement. ..... 135
FIGURE 4.15: COMPARISON OF THE TRANSLATIONAL ACCURACIES OF THE THREE ORIGIN TECHNIQUES compared to the Limits of Clinical Significance. ..... 141
FIGURE 4.16: COMPARISON OF THE ROTATIONAL ACCURACIES OF THE THREE ORIGIN TECHNIQUES ..... 143
Figure 4.17: COMPARISON OF THE ROTATIONAL ACCURACIES OF THE THREE ORIGIN STYLES WITHOUT the Limits of Clinical Significance indicators. ..... 144
Figure 4.18: Bland-Altman plot showing the accuracy of the Caudal Origin Technique in the X direction ..... 145
Figure 4.19: Bland-Altman plot showing the accuracy of the Apex Origin Technique in the X direction ..... 145
Figure 4.20: Bland-Altman plot showing the accuracy of the Dual Origin Technique in the X direction ..... 146
Figure 4.21: Comparison of the Translational Accuracy Bland-Altman plots Limits of AGREEMENT ..... 147
Figure 4.22: Comparison of the Rotational Accuracy Bland-Altman plots Limits of Agreement ..... 147
FIGURE 4.23: GRAPHICAL DISPLAY OF THE PRECISION OF THE SUPERIOR ASPECT OF THE THREE ORIGIN STYLES ..... 150
FIGURE 4.24: GRAPHICAL DISPLAY OF THE PRECISION OF THE INFERIOR ASPECT FOR THE THREE ORIGIN STYLES ..... 151
Figure 4.25: Probability Plot for the precision results of the superior aspect of the Apex Origin Style ..... 152
Figure 4.26: Probability Plot for the precision results of the inferior aspect of the Caudal Origin Style ..... 153
Figure 4.27: EXAMPLE OF ONE OF THE TEN VARIANCE COMPARISONS WITH NO STATISTICAL DIFFERENCE ..... 155
FIGURE 4.28: VARIANCE COMPARISON SHOWING STATISTICAL DIFFERENCE PRESENT IN THE Y DIRECTION FOR THE SUPERIOR ASPECT OF THE SPINE PRECISION ..... 157
Figure 4.29: Comparison of the Superior Y Precision of the Apex and Dual Origin Styles ..... 158
Figure 4.30: VARIANCE COMPARISON SHOWING STATISTICAL DIFFERENCE PRESENT IN THE Z DIRECTION FOR THE SUPERIOR ASPECT OF THE SPINE PRECISION ..... 159
FIgURE 4.31: VARIANCE COMPARISON SHOWING STATISTICAL DIFFERENCE PRESENT IN THE X DIRECTION FOR THE SUPERIOR ASPECT OF THE SPINE PRECISION ..... 160
Figure 4.32: Comparison of the Inferior X Precision of the Apex and Dual Origin Styles ..... 161
Figure 4.33: VARIANCE COMPARISON SHOWING STATISTICAL DIFFERENCE PRESENT IN THE RY DIRECTION FOR THE SUPERIOR ASPECT OF THE SPINE PRECISION ..... 161
Figure 4.34: X-RAY images comprising the reference exam for the Caudal Origin Style ..... 163
Figure 4.35: X-RAY IMAGE SETS COMPRISING THE REFERENCE EXAMS FOR THE APEX AND DUAL Origin Styles ..... 164
FIGURE 4.36: A POSTERIOR-ANTERIOR VIEW OF THE SIMULATED SPINE ASSEMBLY SHOWING THE RESIDUAL $20^{\circ}$ RIGHT MAIN THORACIC CURVE ..... 165
Figure 4.37: COMPARISON OF THE THREE EXAMINED ORIGIN STYLES ..... 166
Figure 4.38: VECTOR ADDITION OF THE TRANSLATIONAL ACCURACIES FOR THE THREE ORIGIN STYLES ..... 168
Figure 5.1: T4 Vertebra with marker movement ..... 182
Figure 5.2: Sectional Origin Style ..... 192
Figure B.1: Vertebral Coordinate Systems. ..... 206
Figure B.2: T8 Rotational Coordinate System. ..... 207
Figure B.3: Spinal Coordinate System ..... 208
FIGURE B.4: Location of the translated origin used for the rotational precision ASSESSMENT OF THE PHANTOM SPINAL MODEL ..... 210
Figure B.5: Location of the translated origin used for the rotational precision ASSESSMENT OF THE SIMULATED SPINAL MODEL ..... 211
Figure B.6: The Caudal Coordinate System. ..... 212
Figure B.7: Apex Coordinate System ..... 213
Figure B.8: The Superior and Inferior Coordinate Systems which make up the Dual Coordinate System ..... 215
Figure B.9: Front view of the RSA Coordinate System ..... 216

Figure B.10: Bottom view of the RSA Coordinate System. ........................................................ 216
Figure C.1: CaLibration box and imaging area in the CAD environment..................................... 218
Figure C.2: Image of the fully assembled spine model................................................................ 219
Figure C.3: Planes used to locate model to be imaged. ................................................................ 220
Figure C.4: Simulated model located within RSA environment. ................................................ 220


#### Abstract

The goal of this thesis was to assess the validity of a computer simulated Radiostereometric Analysis (RSA) environment and assess the use of novel migration origin styles for use in the assessment of spinal fusion success in post-surgical adolescent idiopathic scoliosis patients.

A parallel precision study was conducted with a physical phantom and identical computed simulated spinal fusion model. This study was used to conduct a precision validation of the simulate RSA environment. The origin style assessment was done in comparison with the translational and rotational Limits of Clinical Significance defined by Pape et al (2002) and Johnsson et al (2002) respectively [1], [2].

This thesis concluded that the use of a simulated environment is an acceptable method for the creation of phantom RSA research studies. It was also shown that both the Apex and Dual Origin Styles equally accurate and precise.


## List of Abbreviations Used

| 1 AN | Lenke Classification of Scoliotic Curve [3]: <br> 1- Main Thoracic Curve, <br> A- Center Sacral Vertebral Line falls between Lumbar Pedicles <br> N- Normal Thoracic Sagittal Profile |
| :---: | :---: |
| AIS | Adolescent Idiopathic Scoliosis |
| BA | Bland-Altman |
| CAD | Computer Aided Design, referring to the Solid Edge package developed by Siemens, Germany |
| CN | Condition Number |
| CNR | Contrast to Noise Ratio |
| CT | Computed Tomography |
| GCS | Global Coordinate System |
| HBI | Halifax Biomedical Inc ${ }^{(0}$ |
| L1 | The First Lumbar Vertebra |
| LLA | Lower Limit of Agreement |
| LoCS | Limit of Clinical Significance |
| MB-RSA | Model Based RSA Software by Medis specials bv. |
| MRI | Magnetic Resonance Imaging |
| MTPM | Maximum Total Point Motion |
| PA | Posterior-Anterior |
| PI | Prediction Interval |
| POV-Ray | Persistence of Vision Raytracer developed by Persistence of Vision Raytracer Pty. Ltd. |
| RCS | Relative Coordinate System |

RSA - Radiostereometric Analysis or Roentgen Stereogrammetric Analysis

| RS | - | Radiostereometric |
| :--- | :--- | :--- |
| S1 | - | The First Sacral Vertebra |
| SD | - | Standard Deviation |
| SNR | - | Signal to Noise Ratio |
| SP | - | Spinous Process |
| T4 | - | The Fourth Thoracic Vertebra |
| T8 | - | The Eighth Thoracic Vertebra |
| TP | - | Transverse Process |
| ULA | - | Upper Limit of Agreement |

## Glossary

| Accuracy | - An assessment of the closeness of a measurement to the true value. |
| :---: | :---: |
| Adolescent Idiopathic Scoliosis | - Three-dimensional deformity of the spine with no defined cause. |
| Bartlett's Test | - Test for equal variances when all data sets tested are normally distributed. |
| Bland-Altman Plot | - Difference plot developed by Bland and Altman (Lancet 1986) [4]. Also known as a Tukey Difference Plot. |
| Caudal | - Pertaining to the inferior of the spinal column. |
| Centroid | - The geometric center of an object or group of objects. |
| Condition Number | - A measurement of the linearity of a distribution of RSA markers. |
| Control Markers | - The markers in the calibration box that make up the control plane. Used to determine the three dimensional location of the x-ray foci. |
| Cranial | - Pertaining to the superior of the spinal column. |
| Crossing Line Distance | - The length of the shortest perpendicular connection line between a pair of projection lines. |
| Absorbed Dose / <br> Effective Dose | - The energy imparted by ionizing radiation per unit mass of irradiated material (Gy) / A measure of equivalent dose which is weighted for the biological sensitivity of the exposed tissues, relative to the whole body ( Sv ). |
| Fiducial Markers | - The markers in the calibration box that make up the fiducial plane. Used to define the global coordinate system of the RSA environment. |
| Fixation Rod | - Titanium or Cobalt-Chrome rod implanted into the back immobilize and provide initial support to the fused section of the spine. |


| Functional Integrity | - The rigidity of the fused spine section. |
| :---: | :---: |
| Global Coordinate | - The coordinate system used in the RSA environment. |
| System |  |
| Inferior Aspect | - Pertaining to the Inferior section of the spine. A measurement including the L1 vertebra. |
| Inferior Failure | - A simulated failure condition where both the T4 and T8 vertebrae are moved in relation to the L1 vertebra. |
| Kyphosis | - An anterior concavity of the spine in the sagittal plane. |
| Levene's Test | - Test for equal variances when one or more data sets tested are not normally distributed. |
| Lordosis | - A posterior concavity of the spine in the sagittal plane. |
| Lumbar Spine | - The third region of the spine made up of vertebrae L1 through L5. This section makes up the lower back. |
| Marked Vertebrae | - Vertebrae into which RSA markers have been implanted. |
| Marker Cluster | - The three-dimensional distribution of RSA markers that define the pose of a rigid body. |
| Marker Model | - A model that represents the rigid body generated from the markers matched in both the left and right image. |
| Matched Markers | - Markers which are matched in both the left and right image of an RSA exam which have a parallel crossing line distance below 0.1 mm . |
| \#Matched Markers (RSA Output) | - The number of markers in a marker model matched between two RSA exams. |
| Maximum Total Point Motion | - The length of the translation vector of the marker in a marker cluster that has the greatest migration. |
| Origin Style / Origin Technique | - One of the three conditions used to measure intervertebral migration. |


| Phantom Model | - A physical anatomical model built for research or equipment testing. |
| :---: | :---: |
| Pose | - The three dimensional position and orientation of and object. |
| Precision | - A measurement of the system repeatability. The degree which repeated measurements under identical conditions produce the same results. |
| Rigid Body Error | The mean difference in the relative distances between markers from one exam to the subsequent exam. |
| RSA Marker | - Tantalum beads used as radio opaque objects for use in RS assessment. Usually of standard diameter or $0.5,0.8$ or 1.0 mm [5]. |
| Simulated Model | A computer simulated anatomical model used for research. |
| Structural Stability | The osseointegration of the implant into the bone. |
| Superior Aspect | - Pertaining to the Superior section of the spine. A measurement including the T4 vertebra. |
| Superior Failure | - A simulated failure condition where only the T4 vertebra is moved in relation to the T8 and L1 vertebrae. |
| Thoracic Spine | - The second region of the spine made up of vertebrae T1 through T12. The section of the spine where the rib cage attaches. |
| Vertebra/Vertebrae | - Boney segments that makes up the vertebral column or spine. |

## Acknowledgements

I would like to thank my supervisory committee, my supervisor Dr. Ron ElHawary (Department of Surgery), Dr Michael Dunbar (Department of Surgery), Dr. Steven Beyea (Department of Physics and Atmospheric Science), and Dr. Andrew Warkentin (Department of Mechanical Engineering) for their knowledge, time, and advice. I enjoyed my work with the committee and without their support and experience this project would not have been possible.

I would like to thank Elise Laende, James Edwards, and Allan Hennigar for their invaluable help with the RSA and statistical aspects of the project, and for taking the time out of their day to answer all my questions and offer their welcome advice. I would like to acknowledge Jason Fong for his early assistance with anatomical structure modeling. I would also like to thank Dr. Waleed Kishta for his help in the assembly of the phantom model and the IWK and NRC CT imaging groups for their time and equipment.

I would like to thank DePuy Spine ${ }^{\mathrm{TM}}$ for providing financial and technical support, specifically the use of the AIS implant CAD models, Halifax Biomedical Inc ${ }^{\odot}$ for use of the Halifax Infirmary RSA suite and calibration box data and the Dalhousie Mechanical Engineering Department for use of their rapid prototyper.

I would also like to thank the School of Biomedical Engineering community for their guidance and support. I would especially like to thank Sandy Mansfield for everything that she has helped me with during my time in graduate studies.

Lastly, I would like to acknowledge my family and friends for their continued support throughout my time spent pursuing my master's degree.

## Chapter 1 - Introduction

### 1.1 Background

### 1.1.1 Spinal Anatomy and Physiology

One of the distinguishing characteristics of vertebrates is the spine, a segmented anatomical structure which runs the length of the back. It provides support necessary for an upright posture while providing flexibility allowing motion in six degrees of freedom; extension (forward bending), flexion (backward bending), side-to-side bending, as well as left and right rotation. This support/flexibility relationship is created through the interactions of rigid vertebral bones, flexible intervertebral discs, and surrounding muscular structures [6], [7].

The spine is made up of thirty-three vertebrae separated into four sections based on vertebral shape. They are the Cervical, Thoracic, Lumbar, and Sacrococcygeal regions, Figure 1.1. The Cervical Spine consists of the seven vertebrae (C1-C7) which support the skull and make up the neck. Inferior to C7 vertebra, the Thoracic Spine consists of twelve vertebrae (T1-T12). These vertebrae are where the ribs posteriorly attach, creating the structural unit of the rib cage. The third section of the spine, located inferior to the thoracic


Figure 1.1: Anterior view of a normal adult spine. Adapted from Gray's Anatomy: the Anatomical Basis of Clinical Practice 40th Anniversary Edition (2008) [6]
region, is that of the Lumbar Spine. This section consists of five vertebrae (L1-L5) which make up the lower back. This section provides the majority of the flexibility found in the back. The fourth and most inferior section, the sacrococcygeal region consists of two sections of the spine: the Sacrum and the Coccyx. The Sacrum is composed of five fused vertebrae and the Coccyx is composed of a separate group of three fused vertebrae, commonly known as the tailbone [6], [7].


Figure 1.2: Sagittal curvatures of the spine. Adapted from Gray's Anatomy: the Anatomical Basis of Clinical Practice 40th Anniversary Edition (2008) [6]

The sections of the spine also delineate the four lateral curves of the normal adult spine: two in kyphosis and two in lordosis, Figure 1.2. A kyphosis is an anterior concavity or curvature in the sagittal plane with a frontward concavity. Conversely a lordosis is a posterior concavity having a rearward concavity [7]. A normal cervical spine has a lordosis ranging from $20^{\circ}$ to $40^{\circ}$ [7]. This is mirrored by the kyphosis present in a normal thoracic
spine which also has a general range of $20^{\circ}$ to $40^{\circ}$ [7]. A normal lumbar spine has a lordosis in the range of $30^{\circ}$ to $50^{\circ}$ [7]. The range of the sacral kyphosis varies greatly between individuals [7].

Due to the proximity to the skull, the first two vertebrae of the cervical spine differ in their anatomical structure to compensate for their different anatomical loading. Their unique anatomy is not discussed in this thesis. The remaining twenty-two vertebrae that make up the cervical, thoracic, and lumbar sections of the spine all share similar anatomy. The general anatomy is shown in Figure 1.3. Each vertebra consists of two sections: the vertebral body and the vertebral arch. The vertebral body is a disk shaped structure made of an outer ring of cortical bone surrounding an area of cancellous bone. Adjacent to the superior and inferior plates of the vertebral body are the intervertebral discs. The intervertebral discs are collagenous structures that allow for movement between two adjacent vertebrae. Attached to the posterior of the vertebral body is the structure known as the vertebral arch. The vertebral arch is made of two pedicles, two laminae, two transverse processes, one spinous process, and four articular processes. This structure encompasses the spinal cord providing protection for the vital nerve cord. The pedicles are two, round post like structures which extend posteriorly from vertebral body. The laminae are flat structures that extend medially from the pedicles, coming together in the center. Attached to the union of the two laminae is the spinous process. The spinous process is a structure which extends posteriorly from the vertebral arch. The transverse processes extend laterally from the posterior ends of the pedicles. Both the spinous and transverse processes act as attachment points for tendons and ligaments. The four articular processes exist as two pairs: the superior and inferior articular processes. They extend superiorly and inferiorly from the union of the pedicles and lamina. The superior articular process creates an interface with inferior articular process from the superior vertebrae creating the facet joints. The facet joints are lubricated with synovial fluid allowing for movement between the two processes. The structures of the articular
processes create movement constraints between the two adjacent vertebrae, limiting how the spine can flex between the two adjacent vertebrae [6], [7].


Figure 1.3: Common structures of the vertebrae. (Adapted from Gray's Anatomy for Students $2^{\text {nd }}$ Edition (2009)) [8].

Each vertebra gets progressively larger the more inferior their placement in the vertebral column. This is due to the increased axial loading present at each descending level. The overall geometry of the spine provides additional resilience to axial loads through the use of the alternating lordoses and kyphoses allowing for the upright posture present in humans keeping the line of gravity over the pelvis [6], [7].

### 1.1.2 Adolescent Idiopathic Scoliosis

The etymology of the word scoliosis is that it was derived from the Greek word Skoliōsis which means "a crookedness" [7], [9], [10]. Scoliosis is defined as "a lateral deviation of the normal vertical line of the spine which, when measured on a radiograph, is greater than $10^{\circ}$ " [10]. A scoliotic curve is considered an Adolescent Scoliotic curve if it is developed after the age of 10 [11]. The etiology of the typical Adolescent Scoliosis
remains unknown and therefore is apt to the moniker idiopathic. Adolescent Idiopathic Scoliosis (AIS) is the most common type of scoliosis [11]. AIS accounts for over $80 \%$ of surgical cases for scoliosis correction [7].

The prevalence of scoliosis in the general adolescent population is small with only 1.5 to 3 percent of the population having curves greater than $10^{\circ}$ when measured on a standing Postero-Anterior (PA) radiograph [10]. The demographics of the scoliotic population as reported by the Tachdjian's Pediatric Orthopaedics and The Pediatric Spine text books are presented in Table 1.1.

Table 1.1: Scoliosis Population Demographics. Data taken from Tachdjian's Pediatric Orthopaedics [10] and The Pediatric Spine [12]. *indicates female-male patient ratio requiring surgical intervention.

| Curve Magnitude | Tachdjian's Pediatric Orthopaedics [10] |  | The Pediatric Spine [12] |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Population Prevalence (\%) | Female-Male Ratio | Population Prevalence (\%) | Female-Male Ratio |
| $>10^{\circ}$ | 1.5-3 | 1.4:1 | 2-3 | 1.4-2:1 |
| $>20^{\circ}$ | 0.3-0.5 | 5.4:1 (7.2:1*) | 0.3-0.5 | 5.4:1 |
| $>30^{\circ}$ | 0.2-0.3 |  | 0.1-0.3 | 10:1 |
| $>40^{\circ}$ |  |  | <0.1 |  |

Scoliotic curves are named for the section of the spine in which they form. For example a thoracic curve is present in the thoracic region of the spine. Scoliotic curves can be broken down into two sub groups: structural and non-structural. Structural curves are the largest curves present and do not bend when imaged in side bending radiographs. Non-structural curves are the smaller curves present in the spine and are shown to bend in side bending radiographs. Non-structural curves are also called compensatory curves as they often appear as an attempt to maintain trunk alignment. As such non-structural curves often resolve after correction of the main structural curves [7].

The existence of scoliosis in a patient can have several adverse effects on that patient. Among these include psychosocial effects, respiratory function impairment, rib prominence, back pain and trunk imbalance. It has been found that the mortality rate of patients who have AIS is comparable to that of the average population [10], [12].

Respiratory function impairment is directly correlated to thoracic curve magnitude. As curve magnitude increases, the impairment also increases. Curves in the lumbar spine do not affect pulmonary function [11]. It has been shown that cardiopulmonary impairment often does not occur in patients with curve magnitudes less than $100^{\circ}$ [10]. No patient who has had adolescent onset idiopathic scoliosis has died due to respiratory failure caused by AIS [11].

There has been no correlation between scoliosis curve magnitude or location and the psychosocial effects that the condition has on the patients. In fact patients who have larger curves are often more accepting of their deformity, experiencing less focus on the cosmetic effects of the deformity than those with lesser magnitude curvatures [11].

A trunk imbalance is the lateral shifting of the line of gravity away from its normal position over the center of the pelvis. Interestingly, smaller magnitude single curves can create larger imbalances than comparably larger magnitude compound curve structures. Compound curves can rebalance the spine producing less of a decompensation and less of a cosmetic impact [11], [12].

### 1.1.2.1 Patient Assessment

The assessment for scoliosis severity varies from patient to patient but includes forward bending tests, plumb line, skin assessment, leg length assessment and radiographic assessment [7], [10-12].

Forward bending tests look for a rib prominence using a scoliometer. A patient is asked to bend forward until the spine is level. If scoliosis is present one side of the back will be raised above the other. The scoliometer is an inclinometer which gives a clinical measurement to this test [7], [10-12].

A plumb line test examines the spine for trunk decompensation. On a standing patient a plumb-bob is used to drop a plumb line from the C7 vertebra straight down the back. This test will indicate wither the trunk is centered over the pelvis or to what degree the trunk is decompensated [7], [11].

The skin is assessed for indicators of underlying conditions. Café au lait spots and axillary freckles indicate possible neurofibromatosis. Dimpling or a hairy patch in the lumbosacral region may indicate a spinal dysraphism. Connective disorders like Marfan syndrome may be indicated by excessive skin or joint laxity [11].

Discrepancies in leg length are also an indicator of scoliosis [7], [10], [11]. Leg lengths are measured from the anterior superior iliac spine or the umbilicus to the medial malleolus for both legs [7].

### 1.1.2.1.1 Radiographic Curve Measurement

The primary method for assessing the magnitude of a scoliotic deformity has been the Cobb Method. This method uses the Cobb Angle which uses a PA radiograph to assess the lateral magnitude of scoliotic curves. The Cobb Method uses lines drawn perpendicular to the endplates of the cranial and caudal vertebrae of the scoliotic curve to determine the radius of curvature. The angle of this intersection is the Cobb Angle for the curve [7], [10-12]. Figure 1.4 shows the determination of the Cobb Angle from a PA view.


Figure 1.4: Cobb Measurement of the Scoliotic Curvature. Adapted from Tachdjian's Pediatric Orthopaedics $3^{\text {rd }}$ Edition (2002) [10].

### 1.1.2.2 Curve Classifications

There have been several methods for the classification of scoliotic curve structures. This thesis utilized the Lenke radiographic classification which is summarized here [3], [7], [12]. This thesis deals with a spinal deformity corrected to a $20^{\circ}$ right 1 AN Lenke classified curve.

### 1.1.2.2.1 Curve Type

The spine column is broken into three regions: The Proximal Thoracic (PT), the Main Thoracic (MT) and the Thoracolumbar/Lumbar (TL/L). From these six curve types are created [3], [7], [12].

Type 1 Main Thoracic (MT)
Type 2 Double Thoracic (DT)
Type 3 Double Major (DM)
Type 4 Triple Major (TM )
Type 5 Thoracolumbar/Lumbar (TL/L)
Type 6 Thoracolumbar/Lumbar, Main Thoracic (TL/L-MT)

### 1.1.2.2.2 Lumbar Spine Modifier

The lumbar modifier is a measurement of the position of the lumbar vertebra with respect to the center vertical sacral line (CVSL) [3], [7], [12]. They are classed as follows: Modifier A The CSVL runs between the pedicles all the way to the stable vertebra. Modifier B The CSVL lies between the medial border of the concave pedicle and the concave margin of the vertebral body at the apex of the lumbar curve.

Modifier C The CSVL lies completely medial to the concave margin of the apex vertebra of the lumbar curve.

Figure 1.5 shows a summary of the Lenke (2001) classification [3].


Figure 1.5: Summary of the Lenke Curve Classification. The 1AN curve was modeled for this thesis. Reproduced with permission from Lenke et al (2001) ${ }^{1}$ [3].
${ }^{1}$ Lenke, L. G., Betz, R. R., Harms, J., Bridwell, K. H., Clements, D. H., Lowe, T. G., \& Blanke, K. (2001). Adolescent idiopathic scoliosis: a new classification to determine extent of spinal arthrodesis. The Journal of Bone and Joint Surgery. American volume, 83-A(8), 1169-81.

### 1.1.2.2.3 Thoracic Sagittal Alignment Modifier

The thoracic sagittal alignment modifier is an indicator of the sagittal alignment of the spine. Three symbols are used to define this quantity. A (+) indicates a hyperkyphotic $\left(>40^{\circ}\right)$ thoracic spine while a $(-)$ indicates a hypokyphotic thoracic spine $\left(<10^{\circ}\right)$. A (N) indicates a normal kyphotic curve of the thoracic spine [3], [7], [12].

### 1.1.2.3 Curve Progression

The risk of curve progression is dependent on many factors. Among these factors include family history, curve size, detection age, length of time until skeletal maturity and gender [7], [10-12]. It has been noticed that adolescent idiopathic scoliosis occurs more frequently in members of the same family. Male patients have approximately one tenth the chance of curve progression than similar female patients [12].

The threshold which defines curve progression has been reported. Tachdjian's defines curve progression as an increase of $5-6^{\circ}$ [10] while others define curve progression as a curve increase over time. Lovell and Winter's Pediatric Orthopaedics define curve progression as a more than $1^{\circ}$ increase over a period of a month [11], while Basic Anatomy and Pathology of the Spine by Medtronic defines curve progression as an increase in curvature of more than $5^{\circ}$ in a six month period [7].

Detection age is a significant factor in assessing wither a scoliotic curve will progress. For example a curve under $19^{\circ}$ detected in a 16 year old patient has a progression potential of $0 \%$ while a $30^{\circ}-59^{\circ}$ curve detected in a $10-12$ year old patent has a $90 \%$ chance of progression [12]. The Pediatric Spine reports the probability of progression of scoliotic curves as shown in Table 1.2 [12].

Table 1.2: Probability of Curve Progression Dependant on Detection Age and Curve Magnitude as reported by The Pediatric Spine [12].

| Curve Magnitude at | Detection Age |  |  |
| :---: | :---: | :---: | :---: |
| Detection (Deg) | $10-12$ | $13-15$ | 16 |
| $<\mathbf{1 9}$ | $25 \%$ | $10 \%$ | $0 \%$ |
| $\mathbf{2 0 - 2 9}$ | $60 \%$ | $40 \%$ | $10 \%$ |
| $\mathbf{3 0 - 5 9}$ | $90 \%$ | $70 \%$ | $30 \%$ |
| $>60$ | $100 \%$ | $90 \%$ | $70 \%$ |

The length of time until a patient reaches skeletal maturity is another factor for assessing the risk of curve progression. A patient undergoing the early stages of their puberal growth spurt is at the risk of a crankshaft phenomenon [10], [11]. Any curve increasing by more than $1^{\circ}$ per month during this early period is likely to be progressive and will require treatment. Curve increases during this early period of more than $0.5^{\circ}$ per month should be monitored closely while increases of less than $0.5^{\circ}$ per month are considered mild [11]. After they reach their peak height velocity, the risk of crankshaft decreases [10].

### 1.1.3 Medical Treatment

The treatment required for scoliosis varies from patient to patient. The treatment path decided upon is determined by curve magnitude, curve classification, health effects and patient psychosocial characteristics [7], [10-12].

### 1.1.3.1 Observation

For deformities under $20^{\circ}$ observation of curve progression is often undertaken [7], [10-12]. Lovell and Winter's Pediatric Orthopaedics recommends that curves under $25^{\circ}$ should be radiographically monitored every four to six months and patients who grow to skeletal maturity with curve magnitudes less than $30^{\circ}$ should be monitored every five
years [11]. Schnuerer (2003) recommends watching for curve magnitude increases of 5$10^{\circ}$ in a six month period indicating curve progression [7].

### 1.1.3.2 Bracing

The next level of medical intervention for the treatment of scoliosis is the prescription of an orthopaedic brace. These braces, worn 16-18 hours a day [7], produce stagnation in the progression of scoliotic curves [7], [10-12]. Braces are designed to arrest curve progression while a patient reaches skeletal maturity and are not a form of permeant correction [7], [10-12].

The use of bracing is indicated if a curve severity is between $30^{\circ}$ and $45^{\circ}$ or with patients who have curves 20 to $30^{\circ}$ who have undergone a curve progression over $5^{\circ}$ [10], [12]. The use of bracing has an upper functionality limit of around $45^{\circ}$ as these curves cannot be controlled with bracing as well as the brace having a demential cosmetic effect [10-12].

Bracing has been found to be successful at halting curve progression (less than a $5^{\circ}$ increase in curve severity) in around 70\% of treated patients [11], [13], [14].

### 1.1.3.3 Surgical Intervention

The choice to undergo a surgical intervention for scoliosis treatment is a complex multifaceted one. The goal of a surgical treatment is to improve alignment of the spine and restore balance while preventing further curve progression. This is done through creating a solid arthrodesis or rigid fusion of a multi-level spine section [10-12]. To create a spinal fusion, rigid implants are used to secure the spine and provide corrective forces. There are several fusion stabilization techniques but this thesis focuses on the use
of a system of pedicle screws and rigid fixation rods implanted using a posterior approach. These screws and rods can be seen implanted in Figure 1.6.


Figure 1.6: Posterior Spinal Fusion Implants A) An image taken from a CT scan showing a vertebra (green outline) implanted with pedicle screws (orange outline). B) Post-operative bi-planar x-rays of a patient who received a spinal fusion using posterior implants.

The implanted screws and rods are there to provide structure while the fusion occurs. The resulting solid fusion is created by bridging bony growths of the posterior region of the vertebrae. These growths form over the facet joints and implanted bone auto and allograft tissue, removing the freedom of movement of the fused sections. This region is expected to perform similar to natural bone, demonstrating standard stiffness and strength properties.

The options for implants used come in a variety of metals including: Stainless Steels, Titanium alloys and Cobalt-Chrome alloys. They are selected for their strength and biocompatibility properties. The fixation rods are machined as long cylinders with diameters of around $5-6 \mathrm{~mm}$. They are bent and cut to length in the operating room and
implanted into the patient. The rods are connected firmly to the pedicle screws and are connected to one another using cross-connectors. The cross-connections create a box configuration (Figure 1.6 B ) which strengthens the implant system. However, the fixation rods are not designed to withstand the full loading of the spine and allow for some bending before a full fusion has taken place. Therefore if a solid fusion does not occur then the stress imparted on the immobilization system will eventually fatigue the rods and they will fail, leading to a loss of correction [11].

There are many considerations that go into selecting a spinal fusion. These considerations include: Curve magnitude (Cobb Angle), Decompensation, Rotation, Proximity to Skeletal Maturity, Progression Despite Bracing, Pulmonary Function, and Psychosocial Considerations [12]. Curves with magnitudes of $40-50^{\circ}$, for skeletally immature patients, or over $50^{\circ}$ for skeletally mature patients are good candidates for spinal fusions [7], [10-12]. In less than $1 \%$ of surgical cases, the required intervention was due to the presence of back pain [12].

The right thoracic curve pattern, like the one used during the course of this research study, is the most common curve pattern seen clinically [11]. The right thoracic curves are most often corrected using a posterior approach [11]. Anterior approaches are undertaken when required but they will result in decreased pulmonary function, at least temporarily, when undertaken for thoracic fusions [11].

The length of the spinal fusions are kept to a minimum as to impinge as little as possible on patient mobility while providing adequate correction [10], [11]. Normally one level proximal to the stable vertebrae is selected [11].

### 1.1.3.4 Diagnostic Follow-Up

It has been estimated that between 20 and $40 \%$ of patients who undergo surgical intervention report that the surgery has failed to relieve their symptoms. In many of these cases, a pseudoarthrosis or non-union has occurred [15]. Therefore it is important that a patient who has undergone a spinal fusion undergo routine follow-up diagnostic assessment. Accurate measures of the arthrodesis is important, especially for those patients who remain symptomatic after surgical intervention [16]. There are currently no universally accepted radiographic assessment criteria for determining fusion success but there are several methods used to attempt to assess the fusion success [16]. Spinal fusions are assessed for two characteristics: structural stability and functional integrity. Structural stability is the assessment of whether the implants have integrated into the vertebrae, or the osseointegration of the implants [1], [17]. The functional integrity is the assessment of the arthrodesis itself; wither or not the fusion acts as a single rigid body or not [1], [17].

The general process in which diagnostic imaging is conducted post-operatively was summarized by Hilibrand et al (1998) [15]. In their diagnostic process all postoperative patients undergo plain radiographs. Those who have suspected non-unions as determined from the plain radiographs are assessed for symptoms. If these patients exhibit pseudoarthrosis symptoms they are imaged using CT imaging. If apparent union is shown but symptoms persist MR imaging is undertaken.


Figure 1.7: Post-operative diagnostic imaging and assessment tree. Adapted from Hilibrand et al (1998) [15]. Green arrows indicate that the patient is positive for non-union assessment. Red arrows indicate that patients do not exhibit non-union characteristics.

### 1.1.3.4.1 Radiographic Imaging

The most prevalent method for assessing the success of spinal fusion is the use of standard radiographs [15], [16]. These radiographs are used as an initial screening for non-union or delayed union and it is recommended that a non-symptomatic patient comply with a radiographic regime of at least two years [15]. Movement of the fused spine is normally assessed using lateral flexion-extension radiographs [18], [19]. It is been widely accepted that criteria for positive fusion is translational movement of the fusion of less than 2 mm [15], [18].

Lam et al (2008) in an analysis of a collection of various studies found that radiographic assessment of spinal fusions carries with it significant error. They reported that translational error is $\pm 2 \mathrm{~mm}$ while rotational measurement error can be as high as $\pm 5^{\circ}$ [20]. The rotational error characteristic is alarming since most non-unions show rotational movements of $2-4^{\circ}$ in helical CT scans [16]. Santos et al (2003) concluded that the use of plain radiographs indicate a higher rate of fusions than helical CT scans due to their inability to detect fine gaps indicating pseudoarthrosis. They concluded that static radiographs are unable to detect non-unions present in spinal fusions [16].

### 1.1.3.4.2 Computed Tomography

The next level of diagnostic assessment for spinal fusions is the use of Computed Tomography or CT scans. These scans provide increased resolution of the imaging area over that of the plain radiograph [15]. This increased resolution allows for CT scans to assess patients who appear to have solid fusions in radiographic assessment but still exhibit symptoms [15].

The use of CT imaging comes with several drawbacks. Chief among those is the high radiation dose administered to the patient [11], [20]. A study by Huda et al (1997) determined that the effective dose experienced by a pediatric patient undergoing a abdominal CT scan is 3.1 to 5.3 mSv [21]. Patients who undergo surgical treatment for scoliosis are often young and are vulnerable to these high radiation dosages during their growth period [20]. More over the use of CT imaging requires more time and expense than traditional plain radiographic imaging [20]. Another drawback for the use of CT imaging is that the non-unions often occur in the axial plane. Even with high resolution imaging having image slices spaced $1-3 \mathrm{~mm}$ apart, these pseudoarthrosis may still be
missed [15]. CT imaging also shows an increased inaccuracy in the measurement of the rotation of vertebrae inclined in the sagittal and coronal planes [20]. Since scoliosis is a three-dimensional deformity, vertebrae are often rotated in several planes leading the rotational measurements recorded by CT scans to be misleading [20]. Due to the high amount of dense implants located in a spinal fusion surgical site large artifacts can be produced during CT imaging [15]. Newer CT software and the use of titanium as an implant material have reduced these artifacts [15].

The nature of CT imaging precludes it from being able to assess the functional integrity of a spinal fusion. It is however able to adequately assess the structural stability of the fusion [17].

### 1.1.3.4.3 Magnetic Resonance Imaging

The third modality of diagnostic imaging used to assess spinal fusion success is Magnetic Resonance Imaging or MRI. MRIs do not have as high a resolution as CT scans but are better able to assess patients who experience mechanical instabilities where both plain radiographs and CT imaging show a solid fusion [15]. This is an assessment of the functional integrity of the spinal fusion [17]. Unfortunately due to the signal generation and acquisition technique, MR imaging is not able to assess the composition of the bone surrounding the implanted surgical screws. This leads to a poor assessment of the structural stability of the spinal fusion [17].

Unlike the two nuclear imaging modalities, MR imaging does not expose patients to radiological doses. Although the use of MR imaging is normally counter indicated where metal is concerned, the use of non-ferrous metals in surgical implants mean that
they are safely imaged using an MRI scanner [15]. MR imaging is associated with high costs compared to standard plain radiographs.

### 1.1.3.4.4 Surgical Exploration

Surgical exploration, as stated by the Bosworth dictum, is the only way to be certain that a spinal fusion has occurred [22]. As such it is considered the "gold standard" for surgical fusion assessment as no other modality can match the assessment accuracy achieved [1], [15]. The use of surgical exploration is not recommended for routine assessment of spinal fusions due to the fact that they are economically impractical, invasive and their associated morbidity [1], [15], [22].

### 1.1.4 Radiostereometric Analysis

Radiostereometric Analysis or RSA is a method of using two registered x-ray images to determine the three dimensional position of marked structures of the body. It was originally developed shortly after the first use of x-rays in medical diagnostics, with the first published use in 1898 [23]. The modern use of RSA for medical diagnostics was pioneered by Selvik in Sweden in the 1970s [5], [23-29]. With the growing use of computers in medical imaging the use of RSA has expanded.

RSA is a highly accurate, three-dimensional measurement method with accuracy ten times over that of conventional radiography [5], [27-30]. Repeated RSA examinations provide low dose temporal assessment of marked body motion [5], [27-29], [31]. The most significant use of RSA has been the study of the micromotion of implanted joint replacements [5], [25], [28-34]. It has been shown that the continual motion of an implant is predictive of implant failure. In a seminal article, Ryd et al (1995) found that the
determination of long term implant performance could be predicted by assessing early implant stability [33]. They found that data recorded in the first two years predicted long term implant performance $85 \%$ of the time [28], [29], [33].

Due to these advantages, RSA has been used extensively in the literature to assess the motion of the spine [1], [2], [5], [24], [27], [35-45]. It has been found to be a good measurement tool to determine the invertebral migration associated with determination of lumbar and cervical spine fusion success [1], [2], [35], [39], [41-43], [46-50]. With the high measurement resolution and low dosage characteristics RSA has the potential to accurately assess the three-dimensional complex migrations associated with multi-level spinal fusions performed for the treatment of adolescent idiopathic scoliosis [27].

### 1.1.4.1 RSA Equipment Setup

All modern RSA equipment setups share common physical components. These common components include: a pair of synchronized x-ray tubes, a pair of image detectors and a calibration box [51]. The main components of an RSA set-up are shown in Figure 1.8. The term calibration cage is also used in the literature instead of calibration box [5], [23-25], [32], [51]. This thesis will use the term calibration box to define the rigid body used to calibrate the RSA images for analysis.


Figure 1.8: Parts of a modern RSA system. Adapted from Kärrholm (1989) [25]
The fiducial and control planes of the calibration box contain a grid work of imbedded markers called the fiducial and control markers. The fiducial markers are used to define the coordinate system of the calibration box. The control markers are used to determine the positions of the x-ray sources or foci [25].

The x-ray tubes provide a synchronized set of x-ray beams which are used to image the interested area at an identical time point. The images must be of an identical time point so that there is no movement of the patient between the images.

The arrangement of the RSA equipment setup is dependent on the required diagnostic information. There are two main equipment arrangements used in RSA studies [29], [52]. The first setup is a biplanar set up where the x-ray tubes and imaging detectors are positioned orthogonal to one another, Figure 1.9 A. In this RSA setup the calibration
cage surrounds the diagnostic imaging area, shown in grey. The second setup used is a uniplanar design, Figure 1.9 B. This design allows for easier patient placement options but has an increase in out-of-plane error [31], [53]. The uniplanar style is utilized by the Halifax Infirmary RSA suite.


Figure 1.9: RSA Imaging Set-ups. A) Biplanar Imaging, B) Uniplanar Imaging. Triangles are x-ray sources, Black lines are x-ray detectors, Blue rectangles are calibration boxes with fiducial and control markers, and the shaded regions are areas of diagnostically important imaging.

The placement of patients in the RSA imaging area during an RSA study should be done so that the patient anatomical directions align with the global coordinate system. For a series of examinations patient placement should be standardized as recommended by Valstar et al (2005) [5]. The alignment and standardization of the patient placement is done to produce measured migrations which are easily correlated with the spine coordinate system.

### 1.1.4.2 Diagnostic Radiographs

Diagnostic radiographs are created through the use of a form of electromagnetic radiation which has a shorter wavelength than visible light, x-rays. The first use of x-rays for medical use was in 1895 [7]. Since then their use has become prevalent in diagnostic medicine. An x-ray is generated using an x-ray tube, projected toward the target subject and imaging detector [7], [12]. These detectors can be either a traditional analog setup, the exposing of photographic style film or the newer style digital detectors. Digital radiography has become widely used in diagnostic medicine despite their higher initial cost and reduced resolution. Digital radiography does provide improvements in an improved contrast resolution, faster image development and post processing image enhancement opportunities. The use of digital radiography also subjects patients to a decreased radiological dose compared to traditional systems [11].

Image quality is a very important factor in the assessment of clinical radiographs. Without adequate image quality diagnostic assessments may be impossible and require the patient to undergo additional imaging, increasing their radiological dose. There are several aspects that go into the determination but for this thesis and the outcomes herein only three main image quality characteristics are discussed. They are: Image Noise, Image Contrast and Image Spatial Resolution.

### 1.1.4.2.1 Image Noise

Image noise is an issue that can degrade image clarity, impacting spatial resolution and image contrast. Noise adds a random component to the photon signal measurement, adding or subtracting slight contrast variations over the detected imaging area [54], [55]. It is caused by several factors including scatter from the tissues of the patient interacting
with the x-rays (known as scatter), variations in the signal itself as well discrepancies in the photon amplification by the image detector [54], [55]. The standard equation for noise, as stated in The Essential Physics of Medical Imaging (2 ${ }^{\text {nd }}$ Edition) [56], is:

$$
\begin{equation*}
S N R=\frac{N}{\sigma_{b g}}=\frac{N}{\sqrt{N}}=\sqrt{N} \tag{Equation 1.1}
\end{equation*}
$$

where SNR is the Signal-to-Noise Ratio, $N$ is the average number of photons per pixel and $\sigma_{b g}$ is the standard deviation of the photon count in the image background [56].

A method for increasing the SNR, as demonstrated by Equation 1.1, is to simply increase the number of photons hitting the image detector. This unfortunately leads to a proportional increase in radiological does to the patient when the photons are generated at the same energy. If we wanted to increase the SNR by a factor of two, the patient would receive an increase dose on the order of 4 [56]. Due to the nature of RSA imaging, higher energy photons can be emitted for a decreased time duration compared to conventional radiography [41]. In this situation there is actually a decrease in number of emitted photons. With less photons emitted there is a decrease in $N$ and thus a proportional decrease in the SNR. An SNR above 5 will almost always allow for the recognition of image objects [54].

The scatter produced by the interaction of x-rays with tissue degrades image performance. It is dealt with by the implementation of anti-scatter screens. These screens prohibit the ability of oblique x -rays produced during scatter from contacting the image detectors. Only the narrow beams emitted pass through the screens and contact the detectors, producing a detected signal [55]. RSA utilizes higher energy x-rays which
interact less with the patient tissue, therefore scatter is reduced over traditional radiography.

### 1.1.4.2.2 Image Contrast

Image contrast is created by the differing absorption criteria of electromagnetic radiation by the various materials of the body. A denser material, like bone, absorbs higher energy x-rays than does a soft tissue, which has a lower density [7], [54]. The amount of attenuation created by a unit length of material is dependent on their respective attenuation coefficients [54], [55]. Along with density, material thickness variation also creates differences in image contrast. The more material that the x-rays pass through the more attenuation the signal undergoes, increasing image contrast [54], [55]. These differing absorption characteristics and tissue thicknesses allow x-ray technicians to distinguish the different anatomical structures of the body. A material which absorbs all x-rays and stops them from hitting the imaging film are called radio-opaque while materials which only partially absorb x-rays are called radio-lucent [7].

Due to the post-processing abilities inherent in digital radiography, basic image contrast present at the time of exposure is not a strong descriptor of the image contrast potential. The Contrast-to-Noise Ratio (CNR) becomes a more relevant description of the contrast potential. Therefore the noise level of the image becomes very important. As the noise level decreases the image display window can be more tightly refined allowing objects to become more perceptible [56]. The equation for CNR is defines as:

$$
\begin{equation*}
C N R=\frac{\left(\bar{X}_{S}-\bar{X}_{b g}\right)}{\delta_{b g}} \tag{Equation 1.2}
\end{equation*}
$$

where $\delta_{\text {bg }}$ is the standard deviation of the image background, $\bar{X}_{S}$ is the signal of the source and $\bar{X}_{b g}$ is the signal of the image background. The use of the CNR is most effective when used on image areas which general homogeneous signal strengths [54].

### 1.1.4.2.3 Image Spatial Resolution

Spatial resolution is the ability of an imaging modality to distinguish objects as they become smaller or closer together. High spatial resolution means that very small objects which are close together can still be distinguished as two separate, unique entities [56]. When two objects get so close so that their boundaries cannot be distinguished, this is considered the edge of the spatial resolution [56]. Spatial resolution is of particular importance in RSA, as the modality routinely deals with small, closely packed objects and minute relative motions. The accurate registration of the marker locations is dependent on the point spread function of the radiographic system.

Several factors affect the resultant spatial resolution of an imaging modality. These include: subject motion, defocus blur, and image noise [56]. Subject motion is not important in standard radiographic system due to the short image acquisition time. Motion blur becomes more of an issue is long acquisition time systems like during CT or MRI scans [56].

Another factor that impacts spatial resolution is the magnification of the image. Magnification is an unavoidable consequence for projection radiography due to the x-rays diverging from the central source [56]. The further an object is from the detection plane the more it is magnified [56]. An example of this is shown in Figure 1.10.


Figure 1.10: Object magnification dependant on distance from detector plane. $\mathrm{D}^{2}<\mathrm{D}_{1}<\mathrm{D}_{\mathbf{2}}$
The magnification of an object degrades the spatial resolution of the imaged object [56]. The edges are less defined due to the amplification of the projection shadow's area. This is very noticeable in RSA exams where the definition of marker boundaries and centers become more difficult as they are moved away from the image detectors. A clear example of this is the differences between the fiducial and control markers present in all RSA images. The fiducial markers appear smaller with more defined borders then their control marker counterparts.

Image magnification spatial resolution loss could have an impact in scoliosis spinal fusion success assessment as the distance between the detectors and the RSA markers implanted into the spine will vary due to the three-dimensional nature of the deformity. This will cause the positioning of less magnified marker clusters to be more accurate than others which undergo more magnification.

### 1.1.4.2.4 Radiological Dose

Radiological dose in x-ray imaging is often reported as an effective dose in the units of Sievert (Sv). This unit is in Joules absorbed per kilogram of tissue ( $\mathrm{J} / \mathrm{kg}$ ). The effective dose is a method of describing a radiation dose as subjected to the whole body by using weighting factors for the affected organs. The effective dose is defined by the equation:

$$
\begin{equation*}
E=X \times \sum W_{t} \tag{Equation 1.3}
\end{equation*}
$$

where $E$ is the effective whole body dose, $X$ is the amount of radiation dose given to the patient during an x-ray image and $W_{t}$ is the tissue weighting factor. For example a dose experienced by the gonads is given a weighting factor of 0.08 for the whole body subjected to a uniform energy field at the same energy. The tissue weighting factors was introduced in the 1970s and has been periodically updated by the International Commission on Radiological Protection (ICRP). The tissue weighting factors used in this thesis are from the most recent of these updates in 2007 published as ICRP report 103 and republished in The Essential Physics of Medical Imaging (3 ${ }^{\text {rd }}$ Edition) (2012) [54].

Unlike standard skeletal diagnostic imaging, RSA imaging is used to capture highly radio-opaque objects. This allows for the use of higher energy photons which would normally produce inadequate contrast is standard skeletal x-rays [41]. The use of the higher energy x-rays decreases the radiological dose experienced by the patient since these higher energy photons do not get absorbed as easily by the soft tissue of the body [41], [56]. Work by Greene-Donnelly et al (2008) found that using 141 KVp photons for 11.6 mS provided adequate contrast for RSA imaging of the lumbar spine. The use of this higher energy x-ray beam imparted only 0.304 mSv to the patient per RSA image pair.

This resulted in a total dose of 1.52 mSv per visit for a total of approximately 9.1 mSv over the course of their two year study. This is a reduction of $91 \%$ compared to the 18 mSv dose received by patients in another single diagnostic lumbar study [41].

### 1.1.5 RSA Markers

RSA markers are almost exclusively spherical beads made from Tantalum (Ta), atomic number 73 [5]. Tantalum is a radio-opaque material with low reactivity in the body. Implanted Tantalum markers of the size of $0.5 \mathrm{~mm}-1.0 \mathrm{~mm}$ are excellent for use during RSA studies as they are well defined landmarks that provide high image contrast at the high x-ray energies used [5]. Valstar et al. (2005) recommends the use of 6-9 well distributed markers per examined rigid body to provide adequate marker occlusion redundancy [5]. The distribution of these marker should be kept as non-linear as possible [5].

### 1.1.5.1 Marker Location Determination

The location of the markers in three-dimensional space is defined by the back projection of the marker shadows present on the radiographic film. The intersection of these projection lines defines the position of the individual marker. The equations for the determination of the back projection lines was reported by Selvik (1989) [24].

### 1.1.5.1.1 Crossing Line Distance

Due to shadow location identification and calculation errors the projection lines of the rigid body markers rarely intersect in three-dimensional space [27-29], [57]. To compensate for this shortfall the center of the shortest perpendicular crossing line is used as marker location [27-29], [57]. This approximation is only acceptable if the crossing
line distance is less than 0.100 mm . If the crossing line distance is over this threshold the projection line pair is not considered to be from the same marker projection. An example of this crossing line definition is shown in Figure 1.11.


Figure 1.11: Definition of the crossing line distance. Adapted from Kaptein et al. (2005) [52] [27-29], [57]

### 1.1.5.1.2 Marker Cluster Condition Number

Marker distribution is very important for the accurate assessment of motion using RSA. The Condition Number or CN is a method to measure the distribution the RSA marker clusters. The condition number is an important determinate of RSA performance. It is a measure of the linearity of the cluster. The more linear the marker cluster the lessaccurate rotational data can be derived from its migrational assessment. The lower the condition number, the more distributed the marker cluster [5], [27-29], [53].

To derive the condition number, the distances of the markers from an arbitrary mathematical line is drawn through the marker cluster are determined. The three dimensional orientation of the line is driven mathematically so that the lowest condition number is achieved. The equation for the condition number of any given marker cluster is given by Equation 1.4 [5], [27-29], [53]

$$
\begin{equation*}
C N=\frac{1}{\sqrt{d_{1}^{2}+d_{2}^{2}+\cdots+d_{n}^{2}}} \tag{Equation 1.4}
\end{equation*}
$$

where $d$ is the distance of the marker from the mathematical line and $n$ is the number of markers in the cluster.

A well distributed marker cluster has a condition number less than 100 [5], [27]. In general, the lower the condition number, the better the marker cluster is for translational and rotational assessment.

### 1.1.5.1.3 Marker Stability

Marker stability is an assessment of the migration of the individual markers within the surrounding bone. A stable marker is one which forms a solid attachment to the surrounding bone, while an unstable marker fails to form this solid attachment and can migrate within the bone.

Marker stability is an important feature to examine when performing RS assessments. The stability of markers is assessed using the mean error of the rigid body marker cluster fitting [24]. In their RSA guidelines, Valstar et al. (2005) define the acceptable threshold for mean error for a marker cluster as 0.35 mm [5].

### 1.1.6 Migration Assessment

To assess the longitudinal migration of vertebrae involved in a spinal fusion, several post-operative RSA exams must be undertaken. The initial post-operative exam becomes the "Reference Scene" for all future examinations. Comparing the relative positions of the marked segments determined in the examinations taken at diagnostic time points to the relative positions in the reference scene, the intervertebral migration of the spinal fusion can be ascertained.

### 1.1.6.1 System Accuracy Assessment

The dictionary defines accuracy as the "degree of conformity of a measure to a standard or a true value" [58]. In essence accuracy is an assessment of how close a measurement is to the true value produced. For a diagnostic technique to be applicable for use it must exceed the accuracy requirements of the clinical diagnostic threshold. These thresholds are called the Limits of Clinical Significance. For the assessment of the migrations of the spine using RSA Limits of Clinical Significance have been defined in the literature. In a study by Pape et al (2002) examining fusions of the L5 and S1 vertebrae, found that solid fusion can be assumed if observed translational movements are less than $0.3,0.5$, and 0.7 mm in the transverse (X ) (Left/Right), vertical (Y) (Axial along the spine) and sagittal ( $Z$ ) (Anterio-posterior) spinal axes, respectively [1]. These thresholds were used as the translational Limits of Clinical Significance for this thesis. The rotational Limits of Clinical Significance were defined by Johnsson et al (2002) as $2.0^{\circ}, 0.5^{\circ}$ and $0.9^{\circ}$ around the transverse (X), vertical $(\mathrm{Y})$ and sagittal $(\mathrm{Z})$ axes respectively [2]. These two sets of values were used as the Limits of Clinical Significance for this thesis. In their Guidelines for Standardization of Radiostereometry (RSA) of

Implants, Valstar et al (2005) state that the accuracy of a RSA system can be determined by comparing the RSA measurement with a method that has a much more substantial accuracy, on the order of $\mu \mathrm{m}$ [5].

Several studies published in the literature have conducted accuracy assessments of on phantom models. Most use a $95 \%$ Prediction Interval assessment to determine the accuracy of their respective RSA systems [28], [29], [34], [59-61]. Önsten et al (2001) [34] assessed the accuracy of a pair of human and canine femoral component phantom mode. The models were visually aligned with the calibration cages and 14 increments of the femoral component displacement were induced in all three principal directions. The range of these displacements was from zero to 0.5 mm . This process was repeated 5 times for each specimen, for a total of 75 image pairs taken per specimen. The results from this study were an accuracy range for the human specimen of $\pm 0.047 \mathrm{~mm}$ to $\pm 0.121 \mathrm{~mm}$ and $\pm 0.045 \mathrm{~mm}$ to $\pm 0.074 \mathrm{~mm}$ for the canine model. This study also found that the longitudinal (along the axis of the femur) axis showed a higher accuracy than either the sagittal or transverse directions [34].

The study conducted by Bragdon et al. (2002) [26] was the only one presented in this section which did not calculate the system accuracy using a prediction interval method. They conducted a study on a hip arthroplasty phantom in which four displacements in each of the medial, posterior and superior directions were induced. The displacement range for any one displacement direction was from 0.05 mm to 0.2 mm . The induced displacements in this study were not performed independently of one another; therefore the final placement of the femoral component was $0.2 \mathrm{~mm}, 0.2 \mathrm{~mm}, 0.2 \mathrm{~mm}$ (all medial increments, then all posteriorly increments, then all superior increments
respectively) from its original starting position. At each increment a RSA image set was taken. This procedure was repeated 5 times for a total of 85 image pairs per phantom model. The results for this study found that for an acetabular component with a condition number of 55 gave an accuracy range of $\pm 0.0219 \mathrm{~mm}$ to $\pm 0.0861 \mathrm{~mm}$ [26].

In 2005 Madanat et al [60] performed an accuracy study on the use of RSA in the assessment of distal radius fracture healing. They examined both the translational and rotational accuracy of the RSA system. To perform this study, a two section distal radius fraction phantom model was implanted with RSA markers. Into this model 7 migrations along the distal, medial and anterior axes of the range of 0.025 mm to 5.0 mm . An additional 5 migrations were induced in the proximal direction. These displacements were of the range from 0.025 mm to 0.9 mm . To assess rotational accuracy, 4 rotational displacements were induced around the longitudinal and transverse principal axes. The displacements were conducted in both the clockwise and anti-clockwise directions. The rotational migrations were of the range of $1 / 6^{\circ}$ to $2^{\circ}$. This study found a translational accuracy range of $\pm 0.006 \mathrm{~mm}$ to $\pm 0.029 \mathrm{~mm}$ and a rotational accuracy range of $\pm 0.073^{\circ}$ to $\pm 0.187^{\circ}[60]$.

Two years later in 2007 the same research team (Madanat et al 2007) utilized a computer simulated distal radius fracture model to complete a similar RSA assessment study [59]. This study used both a two and three section distal radius fracture model to assess both the translational and rotational accuracy of the RSA system. Due to the unconstrained nature of the simulated environment, complex motions could be induced which were not able to be completed in a physical phantom model. The results from this
study are summarized in Table 1.3 [59]. This was the only study found to conduct an RS analysis in a simulated RSA environment.

Table 1.3: Summary of the accuracy results from Madanat et al. (2007) [59]

|  | Fracture Model Accuracy Results |  |
| :---: | :---: | :---: |
| Accuracy Assessed | 2-Part | 3-Part |
| Translational (mm) | $\pm 0.001$ to $\pm 0.002$ | $\pm 0.003$ to $\pm 0.004$ |
| Rotational (deg) | $\pm 0.009$ to $\pm 0.015$ | $\pm 0.009$ to $\pm 0.031$ |
| Complex Translation (mm) |  | $\pm 0.005$ to $\pm 0.006$ |
| Complex Rotation (deg) |  | $\pm 0.017$ to $\pm 0.120$ |

Also in 2007 Wilson assessed the accuracy of a knee arthroplasty phantom model, assessing both the use of standard RSA and model-based RSA migration assessment [28]. To do this the study induced six displacement increments along the three principal axes of the phantom model. The two migrational assessment techniques were both completed on this set of data. The translational accuracy of the traditional RSA measurement had a range of $\pm 0.025 \mathrm{~mm}$ to $\pm 0.079 \mathrm{~mm}$ while the model-based RSA measurement exhibited and accuracy range of $\pm 0.020 \mathrm{~mm}$ to $\pm 0.063 \mathrm{~mm}$ [28].

Laende et al. (2009) conducted an assessment of the use of a local coordinate system based on the tibial implant component used in a knee arthroplasty [61]. To assess the accuracy in this study 7 displacements in each direction were implemented. The range of these displacements was from 0.05 mm to 3.0 mm . The displacement directions were not tested independently. The displacements were implemented along the X -axis, then the Y-axis, then the Z-axis. This left the final positions of the tibial implant $<3,3,3>$ from its original reference position. Along with the translational accuracy, the rotational accuracy was also assessed. Around each axis the implant was rotated to six discreet displacements. The ranges for the displacements were $1 / 6^{\circ}$ to $6^{\circ}$ for the X and Z axes but
$1 / 6^{\circ}$ to $10^{\circ}$ for the Y-axis. The rotations were not completed in combination. The results from the study found that translational accuracy ranged from $\pm 0.025 \mathrm{~mm}$ to $\pm 0.075 \mathrm{~mm}$ for the conventional RSA system to $\pm 0.021$ to $\pm 0.048$ for RSA using an implant based coordinate system. The rotational accuracy ranged from $\pm 0.061$ o to $\pm 0.153$ o [61].

### 1.1.6.2 System Precision Assessment

Precision is an assessment of the repeatability of diagnostic system. Under identical conditions, multiple measurements of the same parameter should yield the same result. The variations of the recorded measurements yields the system's precision. For in vivo precision assessment Valstar et al (2005) and Makinen et al (2004) advocate the use of double examinations [5], [62]. Double examinations are a pair of RSA exams taken at a single time point, thus eliminating the migration that may occur between exams. This provides a set zero displacement exams from which system precision can be assessed.

Other researchers recommend the repeated measurements of a zero-displacement phantom model to assess system precision [26], [34], [63]. A zero-displacement phantom model is a model in which no inter-segmental movement is induced between RSA exams. These can be used like the in vivo double exams to assess system precision. Unlike the in vivo double exams, the number of zero displacement exams produced is not limited by subject radiological dose. This allows for the phantom precision datasets to have much larger populations than other precision studies.

In their 2001 article, Önsten et al performed a precision assessment on their cadaveric human and canine hip arthroplasty models [34]. Each model was consecutively imaged 5 times in the initial reference position. The models were then moved 0.200 mm
along the three principal axes. At each point, the model was once again consecutively imaged 5 times for a total of 30 images per phantom model. The precision was calculated as the standard deviation of the zero-displacement exams. The longitudinal precision results from this study were: 0.03 mm and 0.04 mm for the human specimen and the canine model respectively [34].

In their study, Bragdon et al (2002) used the errors of the 79 accuracy data points to assess their system accuracy [26]. For the acetabular component with a condition number of 55 the system precision was found to be of the range 0.0055 mm to 0.016 mm [26].

The 2004 cemented canine total hip study conducted by Allen et al assessed three models for precision [63]. The three total hip models examined were a Plexiglas model, a canine simulant Sawbones model and four in vivo canine subjects. The three different models were expected to produce three levels of system precision with the most precise measurements taken on the Plexiglas model and the least precise measurements recorded from the in vivo subjects. The two phantom models were imaged four successive times, having been repositioned in between each image. The four in vivo canine subjects underwent double exams at four post-operative time points. The subjects were repositioned between each RSA exam [63]. The results from this study are summarized in Table 1.4.

Table 1.4: Precision result summary from Allen et al (2004) [63].

| RSA Precision | Precision Assessed |  |
| :---: | :---: | :---: |
| Assessment Model | Translational (mm) | Rotational (deg) |
| Plexiglas | 0.0166 to 0.0188 | 0.009 to 0.040 |
| Sawbones | 0.0091 to 0.0426 | 0.062 to 0.421 |
| In Vivo Canine | 0.0162 to 0.0411 | 0.168 to 0.436 |

In the 2005 Madanat et al article, the distal radius fracture model was used to assess system precision as well as accuracy [60]. A single image RSA exam was completed with the model in the initial, reference position. The model was then moved within the global RSA environment 0.200 mm along each of the three axes (distal displacement along the longitudinal axis, medial and lateral displacement along the transverse axis, and an anterior displacement along the sagittal axis). This study also induced a rotational displacement for precision assessment. The model was rotated $1 / 20$ clockwise about the long axis of the radius. This totaled 26 image pairs used to assess the system precision using a standard deviation approach. The results from this study found that the translational precision was of the range $0.002 \mathrm{~mm}-0.006 \mathrm{~mm}$ and the rotational precision was of the range $0.025^{\circ}$ to $0.096^{\circ}$ [60].

Assessing a total knee arthroplasty, Wilson (2007) reported a standard RSA system translational precision of 0.03 mm to 0.06 mm and a rotational precision of $0.05^{\circ}$ to $0.09^{\circ}$ [28]. These precision were recorded from the assessment of 11 small movements of a zero-displacement phantom model [28].

Laende et al (2009) using a phantom of a tibial implant used in total knee arthroplasties assessed the precision of three different RSA migration assessment styles [61]. They conducted 12 zero-displacement exams with model relocations undertaken between each exam. The precision results presented in this study ranged from 0.017 mm
to 0.044 mm for the translational precision and $0.014^{\circ}$ to $0.049^{\circ}$ for the rotational precision [61].

### 1.2 Previous Work

The use of RSA for examining the movement within spinal fusions is not a novel concept and it has been studied previously by various research groups [1], [39], [47-49], [64]. These studies focused on single level fusions performed on adult patients, determining fusion failure thresholds. After a review of the literature, to my knowledge, the use of RSA to assess the success of multi-level fusions utilized during the surgical treatment of scoliosis is unique to this research center.

The measurement of migration in spinal fusion in a scoliosis model using RSA is a unique challenge. The complex nature of the deformity extends in all three dimensions with vertebral rotations existing around all three axes. The use of pedicle screws and fixation rods introduce many metallic implants which easily occlude markers and limit the RSA field of view. Unlike other spinal fusion studies, the fusions used to treat scoliosis extend over multiple levels increasing intervertebral measurement distances.

### 1.2.1 Previous Project Outcomes

Significant work has been performed by A. Francis (MASc) on the assessment of the implantation of RSA in the evaluation of spinal fusion success during his time with the Dalhousie School of Biomedical Engineering. His work has formed the foundation for the work performed for this thesis [27].

### 1.2.1.1 Computer Simulation

A right main thoracic curve was simulated using the Solid Edge CAD program developed by Siemens, Germany. Tantalum markers and AIS fixation implants were placed in the vertebrae. The Solid Edge assembly file was converted to a Persistence of Vision Raytracer imaging software (POV-Ray, created by Persistence of Vision Raytracer Pty. Ltd.) where a simulated radiographic exam was performed. The conversion was completed using Rhinoceros NURBS Modeling software (McNeel North America) as an intermediary file conversion tool. The resulting images were analyzed using the ModelBased RSA (MB-RSA) program produced by Medis specials bv. An overview of this process can be seen in Figure 1.12 [27].


Figure 1.12: Previously developed simulation process. Reproduced with permission from A. Francis (2009) [27].

### 1.2.1.2 Origin Style

The origin style used in the previous work performed on this project was the standard used in the literature; the Caudal Origin Style. This style uses the inferior vertebrae of the fusion as the origin for assessing all migration between subsequent RSA exams. For the spine model used in the previous project the L1 vertebra was used as the
migration origin while the T 4 and T 8 vertebrae were the migrating marker clusters. This origin style is shown in Figure 1.13.


Figure 1.13: The Caudal Origin Style utilized by Francis (2009) [27]. Green triangles are the migratory vertebrae while the orange pentagon denotes the migration origin marker cluster.

### 1.2.1.3 Marker Placement Protocol

The primary objective of the previous thesis was to develop a marker placement protocol for RS analysis of the post-operative success of posterior spinal fusions performed in the treatment of thoracic adolescent idiopathic scoliosis. The developed protocol ensured that:

- Required accuracy and precision was maintained.
- The placement protocol demonstrated a simulated accuracy of 0.3, 0.5 , and 0.7 mm in the respective transverse, sagittal, and vertical anatomical directions respectively [1], [43], [64].
- All markers were placed in optimal locations
- The vertebrae selected for marker implantation were at the curve apex as well as superior and caudal ends of the curve deformity.
- All are placed in positions are both easily accessible during surgery and not considered dangerous to the patient.
- The markers are well distributed in the vertebrae so that they attain a condition number below 100 [5], [27], [53], [65].
- All markers remain visible without being obscured by the AIS implants and without overlapping in a $30^{\circ}$ RSA perspective.
- Markers are implanted in locations where they will remain stable allowing for a mean error of rigid body fitting of less than 0.35 mm [5], [27].

The resulting marker placement protocol consisted of seven markers distributed throughout the vertebrae. One was implanted at the end of each of the pedicle screw holes, one was implanted in each of the transverse processes, one was implanted in each of the lamina, and the final marker was implanted into the spinous process.[27] The marker placement protocol is shown in Figure 1.14.


Figure 1.14: Marker Placement Protocol. Reproduced with permission from Francis (2009) [27].

This marker placement protocol and migrational measurement origin style demonstrated the required movement sensitivity as shown in Table 1.5.

Table 1.5: Average accuracy results reported by Francis (2009) [27]

|  | Transverse | Sagittal | Vertical |
| :---: | :---: | :---: | :---: | :---: |
| Limits of Clinical Significance (mm) <br> (from Pape et al. (2002)) [1] | 0.300 | 0.500 | 0.700 |
| CAD Simulation: Translation Error (mm)[27] | 0.156 | 0.014 | -0.564 |
| CAD Simulation: Rotation Error (degrees)[27] | 0.1769 | 0.4319 | -0.3965 |

### 1.2.2 Previous Limitations

Due to the novel nature of the work, the required scope of the previous work remained focused resulting in several limitations. The most significant limitation was that physical RSA setup restrictions could not be maintained. It was found that the physical size of the x-ray detectors at the Halifax Infirmary RSA suite are too small to accommodate a full length image of the spine. To compensate for this shortcoming, the equipment setup of the simulated environment was allowed to exceed the real-world physical size constraints by placing the x-ray sources further away from the detectors, thereby increasing available diagnostic imaging area. The end result was that the simulated spine model was able to fit within the area of the detectors [27]. The physical size restrictions are equipment dependant and thus may not affect patient populations examined at other institutions.

The restriction of patient size was mostly based on the nature of the origin style used to assess the intervertebral movement. The use of the Caudal Origin Style requires that the full length of the fusion fit within the diagnostic area. This requirement prohibits
the continued use of the Caudal Origin Style in our research, as it cannot be applied clinically.

To eliminate the full fusion image requirement, two additional origin styles have been suggested. These are the Apex and Dual Origin Styles. These origin styles use two sets of RSA images to section the fusion section into a superior and an inferior section. With the Apex Origin Style the marker cluster located at the apex of the scoliotic curve is used as the origin to assess the movements of the superior and inferior maker clusters. Conversely, the Dual Origin Style uses the superior and inferior marker clusters as the migration origins, assessing the movements of the central cluster. Both of these origin styles divide the spine into a superior and inferior aspect which can be separately imaged, effectively doubling the length of the diagnostic imaging area. These two origin styles are shown in Figure 1.15.


Figure 1.15: The Apex and Dual Origin Styles for measuring intervertebral migration. Left: Apex Origin Style, Right: Dual Origin Style. The green triangles denote the migratory vertebra while the orange pentagons denote the migration origins for each of the origin styles. The green rectangle shows the superior image area while the purple rectangle shows the inferior image area.

## Chapter 2- Thesis Objectives

The overall goal of the project undertaken at the IWK Health Center is to utilize the highly accurate measurement available from Radiostereometric Analysis (RSA) to assess the success of spinal fusions performed during the treatment of Adolescent Idiopathic Scoliosis. There were two main objectives for the completion of this thesis:

Objective 1: To validate the use of the raytracing simulated RSA environment for use in the analysis of the applicability of RSA in the assessment of spinal fusion success.

Objective 2: To develop and analyze two novel migration origin styles used to remove the physical constraints of the RSA suite located at the Halifax Infirmary.

### 2.1 Objective \#1: RSA Simulation Precision Validation

To this researcher's knowledge there has been no parallel study of a physical and simulated spinal phantom to validate the use of the simulated environment to assess the applicability of the use of the simulated RSA environment to assess the use of RSA in spinal fusion success assessment.

Approach: Complete a parallel precision comparison of identical phantom and computer simulated spinal fusion models to assess the validity of the simulated RSA environment. This will examine the system precision of the Halifax Infirmary's RSA suite and its simulated counterpart.

Hypothesis: The simulated RSA environment will accurately reflect the real world counterpart, yielding similar precision values.

Rationale: The use of a simulated RSA environment has been used previously at this institution and in the literature [27], [59]. In both cases, outcomes the accuracies recorded from manipulation of the simulated phantom model were congruent with the expected accuracy threshold of published phantom and clinical RSA research [27], [59].

By assessing the system precision of both environments, the simulation can be assessed for its realism and congruency to the physical RSA environment. If there is no statistical significance between the outcomes of the two environments the simulation can be said that it accurately reflects the systemic error associated with the physical RSA system environment.

### 2.2 Objective \#2: Assessment of Novel RSA Origin Styles Used for Spinal Fusion Success Analysis

Research performed by Francis (2009) found that the current setup of the RSA suite at the Halifax Infirmary severely limited the length of potential patients who could undergo RS assessment of spinal fusions [27]. The maximum allowable length at the current configuration was approximately 300 mm .

Approach: Using a computer simulation of the Halifax Infirmary's RSA environment and a simulated phantom model, create and assess two novel origin styles which would allow for the assessment of spinal lengths over 300 mm . The origin styles will be assessed based on their recorded accuracy and precision. To ensure that the migrational measurement performance is maintained, the novel origin styles will be compared with the Caudal Origin Style used in the literature and previously at this institution. The two novel origin styles introduced are the Apex and Dual Origin Styles.

Hypothesis: These novel origin styles will provide equivalent accuracy and precision outcomes to those of the traditional Caudal Origin Style.

Rationale: The length of the available imaging area prohibits the assessment of patients who have spinal fusions longer than 300 mm . This work will increase the effective size of the imaging area, increasing the proportion of the patient population that can be assessed in the future using RS analysis.

Action Plan: Parallel accuracy and precision analyses will be performed on all three origin styles to assess their applicability for use in the assessment of spinal fusion success in future clinical research. The accuracy outcomes of the three origin styles will be compared to the translational and rotational Limits of Clinical Significance reported by Pape et al.(2002) and Johnsson et al.(2002) respectively [1], [2]. These Limits of Clinical Significance are shown in Table 2.1. The precision outcomes are expected to be congruent with various precision outcomes reported in the literature [26], [34], [60], [61], [63].

Table 2.1: Limits of Clinical Significance.

|  | $\mathbf{X}$ | $\mathbf{Y}$ | $\mathbf{Z}$ |
| :---: | :---: | :---: | :---: |
| Translational (mm) [1] | 0.3000 | 0.5000 | 0.7000 |
| Rotational (deg) [2] | 2.0000 | 0.5000 | 0.9000 |

# Chapter 3- Thesis Objective \#1: RSA Simulation Precision Validation 

### 3.1 Introduction

Raytracing software has been used in the literature for the assessment of RSA performance. Specifically, in 2007 Madanat et al utilized POV-Ray to simulate movements in a marked distal radius fracture simulation. In their assessment they found "...that a computer simulation model can be accurately used to replace phantom models in the simulation of RSA studies" [59]. The simulation was shown to have "very high correlation" between the induced migrations and the recorded RSA measurements [59]. They surmised that the simulated RSA environment provided an adequate research tool since the accuracy of the simulated system compared well to that of physical RSA systems.

The use of a simulated RSA environment has been previously used at this institution by Francis (2009) [27]. The simulated RSA environment was used to develop a marker placement protocol and to assess the use of RSA in the assessment of the success of spinal fusions.

The use of simulated RSA assessments provides an opportunity for the accurate creation of complex movements. The required use of micrometers and staging limit the movements that can be created on a traditional phantom model. The use of simulated RSA exams provide a vehicle for the further development of model based RSA, by creating a fast and cost-effective means to conduct RSA studies, requiring only
commercially available computing hardware [59]. In fact this entire thesis, except for the physical phantom model, was completed on an over-the-counter, mid to high range computer notebook.

The validation of the simulated RSA environment is a three component process to assess the simulation accuracy, precision and responsiveness. The Madanat et al (2007) study concluded that the use of the simulated system was acceptable due to the similarity of the recorded accuracy values with those previously obtained in separate distal radius fracture phantom studies [59]. The use of the simulated RSA environment has not yet gone through a parallel comparison study with a physical phantom counterpart. This thesis object has completed a parallel precision comparison of the simulated environment with an identical phantom model to validate the systemic errors inherent within the Simulated RSA Environment used clinical research at this institution.

### 3.2 Simulation Precision Validation Methodology

This investigation of the implementation of Radiostereometric Analysis (RSA) for the assessment of spinal fusion success was completed through the use of simulated RSA exams performed on a simulated computer model consisting of three vertebrae and associated AIS implants. The construction of the simulated model and RSA environment are discussed below.

### 3.2.1 Computer Simulated Spine Model

The process for the construction of a Computer Aided Design (CAD) spinal model was developed by D. Breglia of Ohio University (2006) [66]. This method was used previously in project development at this institution by A. Francis (2009) [27]. This section reports upon and details the improvements made to the processes developed by these two individuals.

### 3.2.1.1 Vertebral Models

Using Sold Edge ST2 CAD software (Siemens, Germany) three vertebral models were constructed to represent the vertebrae at the superior and inferior ends of the scoliotic curve as well as the apex of the curve. The modeling technique used was adapted from Breglia (2006) [66] and used by Francis (2009) [59]. The anatomical measurements used for the vertebral models were adapted from two cadaveric studies performed by Panjabi et al (1991, 1992), who conducted studies on both the thoracic and lumbar spine of adult subjects collecting average measurements for both [67], [68]. Figure 3.1 shows the dimensions used to construct the CAD models used in this thesis. The measurements used for vertebral models used in this thesis can be found in Table 3.2 with the dimension
acronyms defined in Table 3.1. New CAD vertebral models were designed for this project to better emulate the data reported by Panjabi et al (1991, 1992) [67], [68]. The coordinate system definitions for each vertebra can be found in Appendix B.


Figure 3.1: Orthogonal views of the thoracic vertebra showing the dimensions and the Vertebral Coordinate System used to construct the vertebral CAD models. (Adapted from and reproduced with permission from Panjabi et al (1991) ${ }^{2}$ ) [67]

[^0]Table 3.1: Acronyms used for anatomical dimensions for the vertebral models from Panjabi et al (1991, 1992) [67], [68].

| Vertebral Part | Dimension | Acronym |
| :---: | :---: | :---: |
| Vertebral Body | End-Plate Width | EPW |
|  | End-Plate Depth | EPD |
|  | Vertebral Body Height | VBH |
| Spinal Canal | Spinal Canal Width | SCW |
|  | Spinal Canal Depth | SCD |
| Pedicle | Pedicle Width | PDW |
|  | Pedicle Height | PDH |
|  | Pedicle Inclination | PDI |
| Spinous Process | Spinous Process Length | SPL |
|  | Spinous Process Inclination | SPI |
| Transverse Process | Transverse Process Width | TPW |
| Suffixes | Superior (upper) | u |
|  | Inferior (lower) | i |
|  | Sagittal | s |
|  | Transverse | t |
|  | Right | r |
|  | Left | I |

Table 3.2: Anatomical measurements of the simulated vertebral models from data reported by Panjabi et al (1991 and 1992) [67], [68].

| Vertebral Part | Linear Dimensions (mm) | Vertebrae |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | T4 | T8 | L1 |
| Vertebral Body | EPWU | 24.5 | 29.5 | 41.2 |
|  | EPWi | 26.0 | 30.5 | 45.3 |
|  | EPDu | 23.3 | 27.9 | 34.1 |
|  | EPDi | 24.5 | 29.4 | 35.3 |
|  | VBH | 16.2 | 18.7 | 23.8 |
| Spinal Canal | SCW | 17.0 | 17.7 | 23.7 |
|  | SCD | 16.2 | 15.9 | 19.0 |
| Pedicle | PDWr | 5.5 | 6.7 | 8.0 |
|  | PDWI | 7.0 | 6.7 | 9.2 |
|  | PDHr | 11.9 | 12.5 | 15.9 |
| Spinous Process | PDHI | 12.2 | 12.5 | 15.8 |
|  | SPL | 51.1 | 52.8 | 67.7 |
| Process | SPI | 32.5 | 32.3 | 20.6 |
|  | TPW | 56.9 | 59.9 | 71.2 |
|  | TPD | 6.25 | 6.5 | 8.3 |
| Pedicle Angles | Angular | Dimensions (deg) |  |  |

The constructed T8 vertebra is shown in Figure 3.2. The articular processes of the vertebrae were not simulated as they are normally removed during implantation of the pedicle screws. The CAD drawings of the three vertebrae have been included in Appendix A.


Figure 3.2: CAD model of the $\mathbf{T 8}$ vertebra.

### 3.2.1.2 Simulated Spine Assembly

The simulated spine was designed to recreate a post-operative main thoracic scoliosis corrected to $20^{\circ}$, simulating a 1 AN curve under the Lenke classifications [3]. The spinal dimensions used in the construction of the spine were previously used by Francis (2009) and represent average adult spine dimensions [27]. The simulated spine model extended from the T4 to the L1 vertebrae which make up the superior and inferior ends of the curve respectively. In total the model was approximately 290 mm long. To simulate the curve, the T 4 and L 1 vertebrae were both rotated about their Z axes $10^{\circ}$ and $-10^{\circ}$ respectively. The T8 vertebra was moved -15 mm along the X axis to simulate the displacement caused by the scoliotic curve. To recreate the normal kyphotic curve present, the T 4 and L 1 vertebrae were rotated $-10^{\circ}$ and $10^{\circ}$ respectively about their Z-axis while the T8 vertebra was translated -15 mm along the Z -axis. For a full list of dimension
specifications of the spine refer to Table 3.3. The spine origin is located at the center of the inferior endplate of the L1 vertebra and is of the same orientation as the RSA Coordinate System. The Spine Coordinate System and RSA Coordinate System are defined in Appendix B. Figure 3.3 shows the final arrangement of the simulated spine model.

Table 3.3: Specifications of the simulated spine model. All distances are measured from the spine origin to the vertebral origin. Rotations are about the vertebral axes.

|  |  | Position (mm) | Rotation (deg) |
| :---: | :---: | :---: | :---: |
| T4 | X | 0.0 | 10 |
|  | Y | 267.0 | 0 |
|  | Z | 0.0 | -10 |
| T8 | X | -15.0 | 0 |
|  | Y | 156.5 | 0 |
|  | Z | -15.0 | 0 |
| L1 | X | 0.0 | -10 |
|  | Y | 0.0 | 0 |
|  | Z | 0.0 | 10 |



Figure 3.3: Dimensions and Coordinate System of the assembled Full Size CAD simulated spinal model.

### 3.2.1.2.1 Pedicle Screw Implants

The monoaxial pedicle screws were implanted into the simulated vertebral models as single assemblies including the pedicle screw itself and the set screw companion, Figure 3.4. The CAD models of the screws were supplied by DePuy Spine ${ }^{\text {tM }}$. The screw sizes used were matched with the size of the corresponding pedicle. The maximum diameter screw that still fit within the confines of the pedicle was used. The length of the pedicle screw was selected on its ability to pass through the vertebral arch and reach securely into the vertebral body. The sizes of the pedicle screws used are show in Table 3.4.


Figure 3.4: Monoaxial pedicle screw used in the $L 1$ vertebra.

Table 3.4: Pedicle screw sizes used in the simulated spinal model

| Vertebra | Screw Length (mm) | Diameter (mm) |
| :---: | :---: | :---: |
| T4 | 30 | 5 |
| T8 | 35 | 5 |
| L1 | 40 | 6 |

The pedicle screws were implanted the full length of their shank into the vertebrae to the union of the shank and the screw head. This placement simulates that of the screws driven into the vertebrae during actual surgical procedures.

### 3.2.1.2.2 Fixation Rod Construction

The models of the AIS fusion fixation rods were driven by the placement of the vertebral models. To create the unique configuration of the left and right fixation rods, three-dimensional curves were created running through the fixation rod grooves in pedicle screw heads. The rod paths were drawn in the full spine assembly using complex keypoint curves.

A swept protrusion was then created with a rod diameter of 5.5 mm along the developed curve. The rod profile was defined by a circle located with the L1 pedicle screw assembly, Figure 3.4. To keep the rods from intersecting with the fixation screws, straight line segments were used at the union of the rod and screws protruding 6 mm orthogonally from the center of the fixation rod groove in each pedicle screw head. At the superior and inferior ends of the spine, the rod was extended 15 mm past the ends of the screw to simulate the full length of the rod in a patient, Figure 3.4. This method of fixation rod construction is novel to this thesis. The previous project work used a rod configuration which drove vertebral placement and created rod-screw interference conditions [27].

### 3.2.1.2.3 Marker Placement

The placement of the markers into the vertebral models was done using anatomical landmarks to attempt to simulate the implantation precision available to a surgeon in the operating room. This is a deviation from the work done previously, where each marker placement was precisely located [27]. The previously used placement style was overly accurate and not something that could be achieved in a surgical setting using dimensions which were accurate to a tenth of a millimeter. The dimensions used to place the markers in this study were fractions of distances of the vertebral model. For example, the \#4 marker in the T4 vertebra is located approximately $1 / 4$ of the way down from the superior edge of the lamina, Figure 3.5.


Figure 3.5: Placement of the \#4 RSA marker in the T4 vertebra. Fixation rod not depicted for clarity.
The positions of the markers were optimized for visibility through trial and error imaging of the reference spine model using the caudal origin style placement. The placement of all markers can be found in Table 3.5 and Table 3.6 as well as depicted in an axial view in Figure 3.6.

Table 3.5: Location of RSA rigid body markers within the vertebral models. Locations are based on the anatomical references of the individual vertebral models.

| Marker Number | Vertebrae |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | T4 |  |  | T8 |  |  | L1 |  |  |
|  | X | Y | Z | X | Y | Z | X | Y | Z |
| 1 | $\begin{gathered} \text { Lateral } \\ 1 / 4 \text { of } \\ \text { TP } \end{gathered}$ | Inferior <br> 1/4 of <br> TP | Center of TP | $\begin{aligned} & \text { Lateral } \\ & 1 / 4 \text { of TP } \end{aligned}$ | Inferior 1/4 of TP | Center of TP | $\begin{aligned} & \text { Lateral } \\ & 1 / 4 \text { of TP } \end{aligned}$ | Center of TP | Center of TP |
| 2 | Center of SP | $\begin{gathered} \text { Inferior } \\ 1 / 3 \text { of } \\ S P \end{gathered}$ | Center of SP | Center of SP | $\begin{gathered} \hline \text { Inferior } \\ 1 / 3 \text { of } \\ \text { SP } \end{gathered}$ | Center of SP | Center of SP | $\begin{gathered} \hline \text { Inferior } \\ 1 / 3 \text { of } \\ S P \\ \hline \end{gathered}$ | Center of SP |
| 3 | $\begin{gathered} \hline \text { Lateral } \\ 1 / 4 \text { of } \\ \text { TP } \end{gathered}$ | Inferior 1/4 of TP | Center of TP | $\begin{aligned} & \text { Lateral } \\ & 1 / 4 \text { of TP } \end{aligned}$ | $\begin{gathered} \hline \text { Inferior } \\ 1 / 3 \text { of } \\ \text { TP } \end{gathered}$ | Center of TP | Lateral <br> 1/4 of TP | Center of TP | Center of TP |
| 4 | Medial $1 / 3$ of <br> Lamina | Superior 1/4 of Lamina | Center of Lamina | Medial $1 / 3$ of <br> Lamina | $\begin{gathered} \text { Inferior } \\ 1 / 4 \text { of } \\ \text { Lamina } \\ \hline \end{gathered}$ | Center of Lamina | Midpoint of <br> Lamina | $\begin{gathered} \text { Inferior } \\ 1 / 3 \text { of } \\ \text { Lamina } \\ \hline \end{gathered}$ | Center of Lamina |
| 5 | Medial $1 / 3$ of <br> Lamina | Superior $1 / 4$ of Lamina | Center of Lamina | Midpoint of Lamina | $\begin{gathered} \hline \text { Inferior } \\ 1 / 4 \text { of } \\ \text { Lamina } \\ \hline \end{gathered}$ | Center of Lamina | Midpoint of <br> Lamina | $\begin{gathered} \hline \text { Inferior } \\ 1 / 3 \text { of } \\ \text { Lamina } \\ \hline \end{gathered}$ | Center of Lamina |
| 6 | Along Screw Path |  | Anterior 1/4 of Vertebra I Body | Along Screw Path |  | Anterior 1/4 of Vertebral Body | Along Screw Path |  | Anterior 1/4 of Vertebral Body |
| 7 | Along Screw Path |  | Anterior $1 / 8$ of Vertebra I Body | Along Screw Path |  | Anterior $1 / 5$ of Vertebral Body | Along Screw Path |  | Anterior $1 / 3$ of Vertebral Body |

Table 3.6: Positions of the centers of the RSA rigid body markers located within the vertebral models. Dimensions are based on the individual Vertebral Coordinate Systems. All dimensions are in mm.

| Marker Number | Vertebrae |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Left <br> Transverse Process | T4 |  |  | T8 |  |  | L1 |  |  |
|  |  | X | Y | Z | X | Y | Z | X | Y | Z |
| 1 |  | 26.00 | 15.75 | -31.00 | 28.00 | 16.50 | -35.50 | 33.00 | 18.00 | -41.00 |
| 2 | Spinous <br> Process | 0.00 | -3.25 | -40.00 | 0.00 | -2.00 | -41.75 | 0.00 | 3.25 | -55.50 |
| 3 | Right Transverse Process | -26.00 | 15.75 | 31.00 | -28.00 | 16.50 | -35.50 | -33.00 | 18.00 | -41.00 |
| 4 | Left Lamina | 4.00 | 9.00 | -30.00 | 5.50 | 10.50 | -34.50 | 6.50 | 10.00 | -40.00 |
| 5 | Right <br> Lamina | -5.00 | 9.00 | -30.00 | -6.00 | 10.50 | -34.50 | -6.50 | 10.00 | -40.00 |
| 6 | Left <br> Pedicle Screw Hole | 4.25 | 8.00 | 1.00 | 4.00 | 9.00 | 2.25 | 1.25 | 14.50 | 15.50 |
| 7 | Right Pedicle Screw Hole | -1.50 | 9.25 | 1.50 | -2.50 | 9.50 | 3.00 | -4.25 | 15.00 | 12.50 |



Figure 3.6: Axial view of $T 8$ vertebra showing the marker placement within the vertebrae.

### 3.2.2 Radiostereometric Simulation

To analyze the application of RSA in the assessment of spinal fusion success this thesis utilized a process of creating computer simulated RSA exams. This process is similar to the use of phantom models which are standard in clinical research. The use of a computer based simulation provided the potential for extremely precise inputs and absolute control over the testing environment. Any implemented displacement or positioning of the model within the simulated environment was, in effect, perfect. This removed a source of error found in physical phantom models, where the input itself has a measurement error associated with it. The process for the simulation of RSA images was first developed at this institution by Francis (2009) forming the basis for the simulation method in this thesis [27].

### 3.2.2.1 Physical Facilities



Figure 3.7: RSA Suite at the Halifax Infirmary. single calibration box.

The x-ray sources used are located above the patient during imaging. They can only be extended to a maximum of 1.6 m above the image detectors due to ceiling height restrictions. The system is designed to operate with the $x$-ray sources being set at an angle of $30^{\circ}$ to the image detectors, with equipment bulk prohibiting a more acute setting. During previous project work conducted by A. Francis (2009), to fit the spine model within the imaging area the simulated $x$-ray sources were artificially moved to 1.9 m above the x-ray detectors [27]. As well the previous simulation tested an earlier RSA setup which used a calibration box and x-ray source set up which utilized a configuration where the x-ray beam struck the image detectors at a $20^{\circ}$ incident angle [27].

The RSA suite has been updated and now uses Canon CXDI-55C digital x-ray detectors. They have a detection area of $353 \times 430 \mathrm{~mm}$ with a resolution of $2208 \times 2688$ pixels, approximately 5.9 million pixels. The pixel size of the detectors is $160 x 160 \mu \mathrm{~m}$ [69]. The two image detectors are located side-by side and are approximately 20 mm below the fiducial plane of the calibration box.

The calibration box used was designed and built by Halifax Biomedical Inc. (HBI). The calibration box was designed to be used with off-planar x-ray images placed at an incident angle of $30^{\circ}$. The calibration box consists of 37 control markers and 45 fiducial markers spread over the right and left images. The calibration box also contains box identification marker clusters and left and right image identifiers. The placement of the markers is unique to the specific calibration box and is proprietary information of HBI.

### 3.2.2.2 Patient Placement

The placement of the patient was designed to reflect the probable clinical placement of a patient undergoing RS analysis. The placement of the patient was aligned with the global coordinate system and was standardized throughout the study in accordance with the recommendations of Valstar et al (2005) [5].

The model was placed in a supine position on a level plane. This simulated a patient lying flat on their back on a level examination table. The model was axially aligned with the RSA imaging area such that the Y axis of the spinal model ran parallel to the Y axis of the RSA environment. In this placement all model spinal axes are parallel to the corresponding RSA Coordinate System axes. This alignment of the coordinate systems is shown in Figure 3.8.


Figure 3.8: Alignment of the RSA and Spinal Coordinate Systems. Adapted from Kaptein et al (2006) [70].

In a clinical setting, this patient placement would be achieved by laying the patient on their back on a flat level examination table. The patient's superior/inferior axis would then be approximately aligned with the Y axis of the RSA equipment. Although alignment variations may occur between patients due to the unique configuration of their deformity, the individual patients should not experience significant misalignments of the two coordinate systems during the series of post-operative exams. Slight misalignments in patient placement are common between exams in all RSA applications as patient alignment is always approximated at time of examination. The use of relative motion between two rigid segments allows for the correction of this error.

The placement of the patient in this orientation within the RSA environment creates images in which the patient's left and right directions are reversed from image left and right. This is a departure from the normal fusion assessment coronal x-rays but is the standard convention for anteroposterior chest x-rays.

### 3.2.3 Simulated RSA Environment

The simulated RSA environment was designed to mimic that of the physical system available at the Halifax Infirmary. The simulation environment was built in two sections: one in the Solid Edge CAD (Siemens, Germany) environment and one in the Persistence of Vision Raytracer (POV-Ray) (Persistence of Vision Raytracer Pty. Ltd.) environment.


Figure 3.9: Model spine in the CAD RSA environment. Orange Box: Calibration box. White Prism: Diagnostically significant imaging area. The Spinal Coordinate System is shown.

The CAD RSA environment consists of a mock-up of the calibration box and was used to locate the spine model within the diagnostic imaging area, Figure 3.9. The origin of the spine was placed so that the model is approximately centered within the imaging area.

The second simulated environment is that of the POV-Ray imaging environment. This environment contains the simulated calibration box, detector plates, and x-ray sources. The POV-Ray environment was the only environment of the project which used a left-handed coordinate system. To compensate for this discrepancy, the placement of the spine in the CAD environment was adjusted to align with the POV-Ray calibration box and light sources. A more detailed description of this adjustment appears in Appendix C.

The calibration box was constructed as a system of 1 mm spheres placed in an identical layout as specified for the physical calibration box. It was processed as a separate POV-Ray .INC file, which eliminated the requirement of including every sphere in each image file. This allows for easy updates of the image environment for the future
use of new calibration boxes. As with the fiducial and control markers, the image and calibration box identifying markers were also simulated. The inclusion of these markers, although not vital to the calculation of RSA migration measurements, adds to the realism of the simulated RSA environment.

To simulate the detectors in the POV-Ray environment, two $353.3 x 430.1 \mathrm{~mm}$ white planes were constructed to match the size and position of the detectors. The shadows of the simulated phantom model are projected onto these surfaces. Two cameras, or view points, were placed in front of the planes to capture the image of the shadows projected on to the planes. One camera was used for each image. The locations of the cameras within the RSA Coordinate System are $<-105$, 175, $633>\mathrm{mm}$ and $<740$, 175, $633>\mathrm{mm}$ for the right and left images respectively The field of view for these cameras was adjusted to view only the dimensions of the real world x-ray detectors. The rendered image was produced with a $2208 \times 2688$ pixel resolution to match that of the physical detectors.

The x-ray sources were simulated by the placement of the image light source within the POV-Ray environment. The focus of a physical x-ray source is not a singular point but an area source. To simulate this area source, grids of twenty-five individual point sources were arranged in a $3 x 3 \mathrm{~mm}$ area. The locations of the x -ray foci were located 1.6 m above at an angle of $30^{\circ}$ to the detector planes. The positions of the foci in the RSA Coordinate System were $<-184,175,1580>\mathrm{mm}$ and $<1019,175,1580>\mathrm{mm}$ for the right and left images respectively.

Due to the POV-Ray shadow process, the images produced are colour negatives of physical x-rays. For this thesis, an image showing white shadows on a black background denotes a real physical x-ray of a phantom model. Conversely, an image showing a black shadow on a white background denotes a simulated x-ray produced using the following method. This convention is maintained unless otherwise stated.

### 3.2.3.1 Image Simulation

The process for the simulation of RSA images was originally developed by Francis (2009) [27]. With the previously created simulation process, a CAD model of the spine and calibration box is created using Solid Edge CAD software (Siemens, Germany). This CAD model is converted into a single POV-Ray (Persistence of Vision Raytracer Pty. Ltd.) file through the intermediary program; Rhinoceros, a NURBs modeling software (McNeel North America, US). In the POV-Ray file, light sources, cameras and detector planes were created to simulate the RSA environment. The overview of the conversion process is depicted in Figure 3.10 with the step-by-step instructions for the current simulation process found in Appendix C.


Figure 3.10: RSA Simulation Process as developed by Francis (2009) [27].
Significant improvements were made to the image simulation process to better emulate the conditions found in actual radiographic images. Chief among the changes was the alteration of the x-ray signal attenuation method. The previous work focused on a surface attenuation technique to create different material contrasts [27]. With the surface attenuation method, whenever a simulated photon interacted with a surface, a percentage of the signal was blocked while the remainder was allowed to continue on toward the detector planes. The thickness of the material was not taken into consideration with this method. This created an over-definition of each surface which incorrectly increased the contrast of thin objects with many surface layers, and produced low contrast where thick objects had few surfaces for interaction. This issue was most noticeable in the area of the screw thread, shown in Figure A, when compared to a similar thread imaged in a physical phantom model, shown in Figure 3.11 B. The simulated x-ray images produced are colour negatives compared to traditional x-ray images.


Figure 3.11: Surface attenuation technique (A) compared to a phantom model image (B).
To improve the modeling technique, a novel material attenuation technique was implemented. Each material was given its own linear attenuation coefficient providing the required material contrast. The coefficients for the four simulated materials are listed in Table 3.7. Interface admittance is the percentage of the signal that is transmitted through the surface interface while the linear attenuation coefficient is the half-strength thickness used for the simulated material.

Table 3.7: Simulated Attenuation Coefficients

|  | Interface <br> Admittance | Linear Attenuation <br> Coefficient $(\boldsymbol{\mu})$ |
| :---: | ---: | ---: |
| Bone | 0.97 | 100.00 mm |
| Titanium | 0.90 | 4.20 mm |
| Cobalt-Chrome | 0.75 | 2.70 mm |
| Tantalum | 1.00 | 0.21 mm |

As the simulated photon passed through the objects of the simulated spine their signal strength was decreased linearly depending on the thickness of the object. The linear attenuation coefficients were qualitatively developed to match the contrast present in phantom model studies, an example of the visual matching is shown in Figure 3.12. This process recreates the depth contrast present in actual images as well as creating edge blurring.


Figure 3.12: Linear attenuation simulation method (A) compared to a phantom model (B).

### 3.2.4 Radiostereometric Analysis

The simulated image pairs comprising the RSA exams were analyzed using Model-Based Radiostereometric Analysis v3.31 (MB-RSA software) developed by Medis specials bv. based in the Netherlands.

Marker identification was completed using a detection algorithm built into the MB-RSA software. Markers not identified by the algorithm were manually identified using a marker identification tool. The markers were also manually checked to confirm that the software correctly centered the identifier over the visual center of the marker shadow. This was most significant in locations where the marker was occluded by metal implants. The marker contrast was affected causing errors in location of marker centers during automatic marker identification.

Each marker cluster was assessed for marker visibility and cluster distribution in each reference RSA exam. To evaluate marker visibility, the number of matched markers in each cluster was assessed. A matched marker was classed as being visible in both the left and right images as well as having a crossing line distance of less than 0.1 mm . Optimally, all seven markers implanted into each vertebra would be visible and matched.

Unfortunately, due to x-ray foci and pedicle screw placement, the marker \#7 implanted in the L1 vertebrae was not able to be re-positioned to a location where it would be visible.

From the matched markers in each rigid body segments marker models were created. Marker models are vital in generating migration data. The MB-RSA software uses marker models to match marker clusters between follow-up exams. A matrix method for calculating the intervertebral migrations of the fused spine is shown in Section 3.2.4.1.

For each marker cluster the program calculates the CN , rigid body error, number of matched markers, the Maximum Total Point Motion (MTPM) and the translational vector and rotational matrix. A sample of this data is presented in Figure 3.13.

| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Reference: L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Xref | Xmig | x | Y | z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid Body Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum Total Point Motion |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 20.0235 | -0.0143 | 0.1165 | 0.0881 | 0.0472 | 0.0225 | 7 | 6 | 0.1471 | 0.0099 | 18.5 | 19.8 | 20.1579 |
| 0 | 2 | -0.0391 | 19.9844 | 0.1162 | 0.0430 | -0.0063 | 0.3203 | 3 | 6 | 0.0148 | 0.0240 | 34.4 | 19.8 | 19.9992 |

Figure 3.13: Sample Data output from the MB-RSA software. Data recorded from the 20 mm inferior failure accuracy assessment.

The markers of an individual cluster are not uniquely identified by the MB-RSA software between follow-up exams. To match the markers, the software calculates the distance from one marker to the remainder in the cluster for each exam. The program pairs markers between exams by which exhibit the least difference in intra-cluster distance using a least mean squares regression. The "\# Matched Markers" result in Figure 3.13 indicates the number of markers in the marker model which were matched between the two RSA exams. Only markers in the marker models with a corresponding counterpart in both analyzed RSA exams are used to calculate the rigid body motion of the vertebral segment.

When computing migrations during in vivo situations, marker loosening can be a factor. The software uses a 'Rigid Body Match Threshold' to eliminate unstable markers. If the intra-cluster motion exceeds 0.5 mm , then the migratory marker is excluded from use in rigid body migration calculations. Since there is no marker movement during testing in this thesis, the elimination of unstable markers was not observed.
'Rigid Body Error' is the mean difference in the calculated intra-cluster marker distances between one RSA exam and another. It is a measure of the overall stability of a marker cluster and should not exceed 0.35 mm , as advised by Valstar et al (2005) [5]. The marker distribution within their respective marker models was assessed using the CN . A desirable distribution was one that had a resultant CN of less than 100 [5], [27]. A higher CN is an indicator of a poorly distributed marker cluster. A poorly distributed marker cluster provides less information than is required to derive the marker cluster pose matrix. This leads to higher measurement error associated with the calculated rigid body migration.

### 3.2.4.1 Global Migration Calculation

The initial post-operative exam is used as the "Reference Scene" for subsequent follow-up examinations. Comparing the relative positions of the vertebral marker clusters with their positions in the reference scene, a longitudinal assessment of the intervertebral migration can be created.

All measured migration of the vertebrae is calculated from the centroids of the individual marker clusters. The centroid of the marker clusters are defined by Equation 3.1, Equation 3.2, and Equation 3.3.

$$
\begin{aligned}
& X_{C}=\frac{x_{1}+x_{2}+\cdots+x_{n}}{n} \\
& Y_{C}=\frac{y_{1}+y_{2}+\cdots+y_{n}}{n} \\
& Z_{C}=\frac{z_{1}+z_{2}+\cdots+z_{n}}{n}
\end{aligned}
$$

Equation 3.1

Equation 3.2

Equation 3.3
$X_{c}, Y_{c}$ and $Z_{c}$ define the three dimensional coordinates of the marker cluster centroid with $x_{n}, y_{n}$ and $z_{n}$ defining the positions of an individual marker. $n$ is the number of markers in a marker cluster. The centroid is defined as: Centroid $=<X_{c}, Y_{c}, Z_{c}>$.

The three marker clusters assessed during this project were located in the T4, T8 and L1 vertebra. The migration of these marker clusters is determined using the implementation of the following matrix equations published by Laende (2006) [29]. They were reproduced here with permission. The equation script was modified to reflect the use in the spine.

## Variables:

$$
\begin{aligned}
& {\left[P_{\text {Time }}^{\text {Vertebra }}\right]_{\text {Coordinate System }}} \\
& {\left[T_{\text {Time to Time }}^{\text {Vertebra }}\right]_{\text {Coordinate System }}} \\
& \text { Pose Matrix for a marker } \\
& \text { cluster } \\
& \text { Transformation Matrix. This } \\
& \text { represents the rotational } \\
& \text { transformation of a Pose } \\
& \text { Matrix between Time } 1 \text { and } \\
& \text { Time 2. It is in the form: } \\
& {[R]=\left[\begin{array}{ccc}
\cos \beta & 0 & \sin \beta \\
0 & 1 & 0 \\
\sin \beta & 0 & \cos \beta
\end{array}\right]\left[\begin{array}{ccc}
\cos \gamma & -\sin \gamma & 0 \\
\sin \gamma & \cos \gamma & 0 \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & \cos \alpha & -\sin \alpha \\
0 & \sin \alpha & \cos \alpha
\end{array}\right]} \\
& {\left[M M_{\text {Time,Corrected }}^{\text {Vertebra }}\right]_{\text {Coordinate System }}} \\
& \text { Rotational Matrix where } \alpha \text { is } \\
& \text { rotation about the } \mathrm{x} \text {-axis, } \beta \text { is } \\
& \text { about the } y \text {-axis and } \gamma \text { is about } \\
& \text { the } \mathrm{z} \text {-axis. } \\
& \text { Where: Vertebra }= \\
& \text { Time }= \\
& \text { Coordinate System }= \\
& \text { Corrected }= \\
& \text { Shifted }= \\
& \text { T4, T8, or L1 vertebrae. The example shown here is of } \\
& \text { the } \mathrm{T} 8 \text { vertebra measured in reference to the L1 } \\
& \text { vertebra. } \\
& \text { Reference exam (1) or follow-up exam (2) } \\
& \text { RSA Coordinate System (G) } \\
& \text { Origin vertebra transformation applied to remove } \\
& \text { global misalignment between exams. } \\
& \text { Moved to origin of coordinate system }
\end{aligned}
$$

1) Determine the time 1-2 transformation for the reference marker cluster.

$$
\left[T_{21}^{L 1}\right]_{G}=\left[P_{2}^{L 1}\right]_{G}\left[P_{1}^{L 1}\right]_{G}^{-1}
$$

Equation 3.4

2) Apply the time 1-2 transformation to the migratory vertebral marker cluster to bring the time 2 cluster into alignment with time 1.

$$
\left[M M_{2, \text { corrected }}^{T 8}\right]_{G}=\left[T_{21}^{L 1}\right]_{G}\left[M M_{2}^{T 8}\right]_{G}
$$

Equation 3.5

3) Translate the centroid of the reference marker cluster and migratory marker clusters to the global origin.
$\left[M_{2, \text { corrected }, \text { shifted }}^{T 8}\right]_{G}=\left[M M_{2, \text { corrected }}^{T 8}\right]_{G}-$ Centroid $_{1}^{T 8}$
Equation 3.6

$$
\left[M M_{1, \text { shifted }}^{T 8}\right]_{G}=\left[M M_{1}^{T 8}\right]_{G}-\text { Centroid }_{1}^{T 8}
$$

Equation 3.7
4) Determine the transformation of the corrected migratory marker cluster between time 1 and time 2. This transformation is the measured migration with the rotation in the order Y, Z, X.

$$
\left[T_{12}^{T 8}\right]_{G}=\left[P_{1, \text {,hif feed }}^{T 8}\right]_{G}\left[P_{2, \text { corrected.shifted }]_{G}^{T 8}}^{T_{1}^{1}}\right.
$$



The order used to calculate the rotational displacements of the migratory vertebrae can have a significant impact on the results obtained. In the matrix equations above, the order of rotations is $\mathrm{Y}, \mathrm{Z}, \mathrm{X}$ which is common for this style of calculations.

### 3.2.5 Simulation Precision Validation

To determine the precision validity of the simulated RSA environment a parallel precision study was undertaken. In clinical research situations, RSA system precision is calculated using double exams. These exams are taken at a single time point and are assumed to have no migration associated within them. In phantom model situations, the unaltered model can be imaged several times without having to worry about the adverse
effects of radiation dosages, a limiting factor in clinical research. Protocols for assessing precision using phantom models are well defined in the literature. Madanat et al (2005, 2007), Bragdon et al (2002), Önsten et al (2001), and Allen et al (2004) recommend the repositioning of the phantom model within the RSA environment with no displacement induced within the phantom model [26], [34], [59], [60], [63]. The study was conducted identically on both a phantom and simulated model to compare their respective precisions and assess their congruency. The testing process is summarized in Figure 3.14.


Figure 3.14: Process flow chart of the parallel simulation precision validation. Green Path - Physical Model Testing, Blue Path - Simulated Model Testing

### 3.2.5.1 Phantom Model

The phantom model was constructed using the simulated vertebral models previously constructed as described in Section 3.2.1.1. These models were modified to include guide holes for the pedicle screws and for the insertion of the RSA markers. See Figure 3.15 for an example of a modified vertebral model. The holes created for the RSA markers create a marker placement profile identical to that of the simulated marker placement profile as shown in Section 3.2.1.2.3.


Figure 3.15: Modified T8 vertebral model. Red cylinder indicated the guide hole for the placement of the \#2 RSA marker.

Physical constructs of the three vertebral models (T4, T8 and L1) were created using the Dalhousie University Mechanical Engineering Department's rapid prototyper. This machine creates accurate, three-dimensional plastic replicas of the CAD drawings. These physical models were identical replicas of those used in all computer simulations. The dimensions for these phantom models can be found in Section 3.2.1.1.

Into each of the vertebral models, seven 1 mm tantalum RSA markers were implanted into each vertebral model using the marker guide holes shown in Figure 3.15.

The phantom model was assembled using standard spinal fusion pedicle screw implants and instrumentation (DePuy Expedium 5.5mm System; DePuy Spine; Raynham, MA) with the help of Dr. Waleed Kishta, a Pediatric Orthopaedic Fellow at the IWK Health Centre. Six monoaxial pedicle screws and two 5.5 mm Cobalt-Chrome fixation rods were used to form the scoliotic and kyphotic curve of the phantom model. The pedicle screws used are listed in Table 3.8.

Table 3.8: Pedicle screw sizes used in the simulated spinal model

| Vertebra | Screw Length (mm) | Diameter (mm) |
| :---: | :---: | :---: |
| T4 | 25 | 4.35 |
| T8 | 40 | 4.35 |
| L1 | 40 | 6.00 |

The spinal dimensions of the phantom model were modified from the original simulated fusion model to compensate for the limited field of view associated with the physical RSA system. The new phantom model now allows for the phantom to fit within the RSA diagnostic imaging area allowing for the simulation validation to be carried out using the Caudal Origin Style. The nominal dimensions of the physical model are $80 \%$ of the full sized simulated model shown in Figure 3.16 and listed in Table 3.9. The use of a scaled model is expected to impact the precision results obtained from the assessment of the two RSA environments. This impact will not be apparent in the simulation validation assessment as both the physical and simulated models are both scaled to $80 \%$ of the full size length. No analysis between a scaled and full sized phantom was conducted in this thesis.


Figure 3.16: Nominal dimensions and Coordinate System of the Phantom Spinal Model.

Table 3.9: Nominal dimensions of the phantom model compared to those of the full-size simulated spinal model.

| Locations | Full-Size Simulated Model |  | Phantom Model |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Translation <br> $(\mathrm{mm})$ | Rotation $(\mathrm{deg})$ | Translation <br> $(\mathrm{mm})$ | Rotation <br> $(\mathrm{deg})$ |
|  | X | 0.0 | 10 | 0.0 | 10 |
| T4 | Y | 267.0 | 0 | 213.6 | 0 |
|  | Z | 0.0 | -10 | 0.0 | -10 |
|  | X | -15.0 | 0 | -12.0 | 0 |
|  | Y | 156.5 | 0 | 152.2 | -5 |
|  | Z | -15.0 | 0 | -12.0 | 0 |
| L1 | X | 0.0 | -10 | 0.0 | -10 |
|  | Y | 0.0 | 0 | 0.0 | 0 |
|  | Z | 0.0 | 10 | 0.0 | 10 |

Due to the nature of the surgical techniques, the dimensions of the phantom spine were best approximated at the time of assembly. The completed phantom model mounted to its Plexiglas support backing is shown in Figure 3.17.


Figure 3.17: Phantom model on its Plexiglas backing. The dots on the vertebral models indicate the locations of the implanted RSA markers. The Spinal Coordinate System is shown.

To identify the locations of each of the twenty-one implanted RSA markers the assembled phantom model was imaged with a Toshiba Aquilion CT scanner (Toshiba America Medical Systems; Tustin, California). During this CT imaging the phantom model was placed on a level examination surface and aligned so that the Y -axis of the phantom model was approximately in line with the long axis of the CT scanner. A sample image slice of the T 8 vertebral model is shown in Figure 3.18. In this image the markers number 3,6 and 7 can be seen along with the plastic vertebral model, the implanted pedicle screws, the fixation rods, the Plexiglas backing and the top surface of the examination table. The marker location data recorded from this CT scan is shown in Table 3.10.


Figure 3.18: A slice from the CT scan performed on the assembled phantom model showing the T8 vertebral model and implanted components. View is from the bottom of the vertebra.

Table 3.10: Locations of the RSA markers as determined from the assembled phantom CT scan. Locations are described in the Spinal Coordinate System. The L1 marker \#2 position was used as the reference point.

| Vertebra | Marker \# | Marker Location | $X$ | $\boldsymbol{Y}$ | Z |
| :---: | :---: | :---: | :---: | :---: | :---: |
| T4 | 1 | Left Transverse Process | 30.07 | 227.75 | -48.67 |
|  | 2 | Spinous Process | 1.93 | 212.75 | -60.70 |
|  | 3 | Right Transverse Process | -21.45 | 233.75 | -48.90 |
|  | 4 | Left Lamina | 7.37 | 224.75 | -48.90 |
|  | 5 | Right Lamina | -1.48 | 224.75 | -48.90 |
|  | 6 | Left Pedicle Screw Hole | 6.69 | 218.75 | -18.25 |
|  | 7 | Right Pedicle Screw Hole | 1.25 | 220.25 | -17.57 |
| T8 | 1 | Left Transverse Process | 25.76 | 137.75 | -68.19 |
|  | 2 | Spinous Process | -1.93 | 116.75 | -69.10 |
|  | 3 | Right Transverse Process | -29.63 | 134.75 | -61.61 |
|  | 4 | Left Lamina | 3.74 | 131.75 | -64.11 |
|  | 5 | Right Lamina | -7.61 | 130.25 | -62.75 |
|  | 6 | Left Pedicle Screw Hole | 6.24 | 134.75 | -27.33 |
|  | 7 | Right Pedicle Screw Hole | -0.12 | 134.75 | -25.97 |
| L1 | 1 | Left Transverse Process | 34.84 | 11.75 | -45.72 |
|  | 2 | Spinous Process | 1.25 | -6.25 | -55.25 |
|  | 3 | Right Transverse Process | -30.99 | 14.75 | -45.95 |
|  | 4 | Left Lamina | 8.06 | 5.75 | -42.54 |
|  | 5 | Right Lamina | -4.88 | 5.75 | -42.54 |
|  | 6 | Left Pedicle Screw Hole | 6.47 | 26.75 | 8.99 |
|  | 7 | Right Pedicle Screw Hole | 1.02 | 26.75 | 6.03 |

The marker locations recorded from the CT scan were used to develop an identical computer simulation of the marker distribution. The three dimensional marker locations were utilized directly in Solid Edge creating the single, twenty-one marker assembly shown in Figure 3.19.


Figure 3.19: Simulated Model Marker Distribution. From top to bottom: T4 marker cluster, T8 marker cluster, and L1 marker cluster located at the Spinal Coordinate System origin.

The position and orientations of the vertebral models and fusion implants were approximated to closely match the orientations of the three marker clusters. The use of an approximated placement of the vertebral models and AIS implants was deemed acceptable since the exact locations of the vertebral models and implants are unimportant in traditional marker based RS assessment past their role in marker occlusion. Assessment of the resultant images shows that marker occlusion between the physical and simulated images are preserved, for an example see Figure 3.20. The physical phantom model was imaged using x-ray energies of 90 KV for 10 ms .


Figure 3.20: Comparison of Physical (Left) and Simulated (Right) images of the L1 vertebral models. Marker occlusion and spinal model placement is almost identical between the image pair. The simulated image has been colour inverted to provide comparison with the phantom image.

For the computer simulation the CAD model of the $4.35 \times 40 \mathrm{~mm}$ monoaxial pedicle screw implanted into the T8 phantom model vertebrae was unavailable. The $4.35 \times 30 \mathrm{~mm}$ screw model was used in the computer simulation instead. A test image set was taken to assess the effect of this substitution and it was shown that there were no changes in marker occlusion.

### 3.2.5.2 Precision Movement Imaging

To test the system precision and to validate the simulation process, both the physical phantom and simulated model were manipulated in an identical fashion. Both were repositioned as a single rigid unit within the RSA environment with respect to the RSA Coordinate System as defined by the calibration box. No intervertebral movement was induced during all precision imaging. The movements discussed below are described as a single process, applying to both the physical and simulated models except where expressly stated.

The physical model was placed in a supine position on a level examination table at the approximate center of the RSA imaging volume in accordance with the patient placement protocol. The vertical $(\mathrm{Y})$ axis of the model was aligned parallel with the Y -
axis of the RSA calibration box. This arrangement aligns the Spinal Coordinate System with the global RSA Coordinate System. After initial placement, a test image was produced to confirm placement and marker clarity. This positioning was used as the "Reference Position".

To assess the precision of the RSA system and the validity of the simulated environment, sixteen independent migrations were used. The models were moved globally within the RSA environment in three independent movement scenarios. In each case the migration induced was global migration of the spinal model with no intervertebral movement induced. The first of these was that a 10 mm translation in all six cardinal directions. An example of this movement is shown in Figure 3.21.


Figure 3.21: Translational Precision Movement. A) Reference Position, B) Global precision movement of the spine model -10 mm along the $X$ axis.

The second movement scenario was a rotation of the model was $\pm 6^{\circ}$ about all three principle global axes. An example of this movement is shown in Figure 3.22.


Figure 3.22: Rotational Precision Movement. A) Reference Position B) Global precision movement of the spine model - $6^{\circ}$ about the $Z$ axis.

The third movement scenario was one simulating a patient undergoing a combination of rotational displacements. In this scenario, the model was rotated about the Y-axis $\pm 6^{\circ}$ and then $\pm 6^{\circ}$ about the Z-axis. In each of the three scenarios, each examined movement was independent of one another. The model returned to the reference position between each migration scenario. The movements for the three movement scenarios are summarized in Table 3.11.

Table 3.11: Global movements of the fusion model. Each movement scenario was completed independent of the other two.

| Movement | Translation (mm) | Rotation (deg) | Combination Rotation (deg) |
| :---: | :---: | :---: | :---: |
| $\mathbf{0}$ | Reference | Reference | Reference |
| $\mathbf{1}$ | $10+X$ | $6+X$ | $6+Y, 6+Z$ |
| $\mathbf{2}$ | $10+Y$ | $6+Y$ | $6+Y, 6-Z$ |
| $\mathbf{3}$ | $10+Z$ | $6+Z$ | $6-Y, 6+Z$ |
| $\mathbf{4}$ | $10-X$ | $6-X$ | $6-Y, 6-Z$ |
| $\mathbf{5}$ | $10-Y$ | $6-Y$ | Reference 2 |
| $\mathbf{6}$ | $10-Z$ | $6-Z$ |  |
| $\mathbf{7}$ | Reference 2 | Reference 2 |  |

All rotational movements were conducted about a point in the center of the bottom of the Plexiglas backing used to secure the phantom model, Figure 3.23. This point was mirrored in the simulated CAD model as $<1.99,116.75,-82.63>\mathrm{mm}$ in the Spinal Coordinate System. This position of the rotational center was selected to centralize the rotation, keeping the spine centered in the available RSA imaging area. A full definition of this phantom precision rotational coordinate system is described in Appendix B. All Translational movements were along the cardinal axes of the RSA Coordinate System.


Figure 3.23: Etched phantom precision rotation center.

At the end of the movements conducted, the phantom model was returned to the zero reference position and another image set was produced, referred to as "Reference 2" in Table 3.11. This second reference image set was not produced for the simulated model due to the precise nature of the simulation process. This second simulated reference image would be identical to that of the first reference image taken. Therefore the "Reference 2" in Table 3.11 for the simulated precision assessment was a repeat of the original reference image for the simulated model assessment.

### 3.2.5.3 Simulation Precision Validation

Since no intervertebral movements were introduced in either model during the precision assessment imaging, any intervertebral migrations measured using the RSA calculations are an assessment of the system precision. A total of eighteen image sets were produced for the assessment of the precision for the physical RSA environment, while seventeen were produced for the assessment of the simulated environment. This discrepancy was due to the additional 'Reference 2' image set taken during the physical study.

The assessment of the precision was conducted in the same manner as that performed by Madanat et al (2005, 2007), Bragdon et al (2002), Önsten et al (2001), and Allen et al (2004) [26], [34], [59], [60], [63]. When the exams were evaluated using the MB-RSA software, each model repositioning was assessed with respect to the previous model position described in Table 3.11. In this case each repositioning of the models acted as both a migrating scene with respect to the previous model position, and a reference scene with respect to the subsequent model position. For example from Table 3.11, for the translational movement scenario: image set 0 forms the reference scene for
images set 1. Image set 1 then forms the reference scene for image set 2 and so on. This created nineteen data points for the migrations of the T4 and T8 vertebrae for both the physical and simulated models.

Any translational or rotational migrations calculated represent the error within the RSA system. This error is normally based on three main factors: the radiographic positioning and technique, the marker placement, and the migration calculation process which is influenced by the origin style used. Between both the physical phantom and simulated model testing, the marker placement and origin styles were kept constant removing them as sources of error. This left only the radiographic technique as a significant source of error between the real world physical model and its simulated counterpart.

Madanat et al (2005) utilized a simple and effective means of determining system precision shown in Equation 3.9 [60].

$$
P=y \times S D
$$

Equation 3.9
where $S D$ is the standard deviation of the migration dataset ( $\Delta \mathrm{X}, \Delta \mathrm{Y}, \Delta \mathrm{Z}, \Delta \mathrm{Rx}$, $\Delta \mathrm{Ry}, \Delta \mathrm{Rz}, \Delta \mathrm{MTPM})$ and $y$ is the $95 \%$ confidence interval. For nineteen data points $y$ is equal to 2.09 as defined from the critical values of a student $t$-test with nineteen degrees of freedom at an $\alpha$ of 0.05 . The calculations for the precisions can be found in Appendix E, Section E.2.

To compare the precisions of the physical and simulated model, an assessment of their variances was undertaken. Each of the migration datasets ( $\Delta \mathrm{X}, \Delta \mathrm{Y}, \Delta \mathrm{Z}, \Delta \mathrm{Rx}, \Delta \mathrm{Ry}$, $\Delta \mathrm{Rz}, \triangle \mathrm{MTPM})$ for both models were tested for equal variance.

The method used to compare the variances is dependent on the distribution of the two assessed datasets. The distribution of each dataset was analyzed using an AndersonDarling test in Minitab 16. A p-value generated from this test greater than 0.05 indicated that the data was normally distributed. The results of the distribution analysis determined the statistical test used to assess the variance difference. If both compared datasets were normally distributed, an F-Test was used to compare their variance. In dataset pairs where one or both of the sets are non-parametrically distributed the Levene's Test was used. For either of these tests a p-value greater than 0.05 indicated that there is no statistical difference between the two datasets and that the simulated environment mirrored that of the physical RSA system.

### 3.3 Simulation Precision Validation Results

### 3.3.1 Image Simulation

To assess the settings of the image simulation process, the reference images of both the physical and simulated phantom were assessed. The assessment looked at the image intensities, contrast, SNR and CNR of the two image sets. The image intensities were recorded as 8 -bit grey-scale values from 0 to 255 where 0 is black and 255 is white.

### 3.3.1.1 Physical Phantom Imaging

The left and right images produced at the Halifax RSA suite produced two images with unique background intensities and were analysed separately. These images, having been created using a physical RSA system displayed image noise. Figure 3.24 shows the Regions of Interest (ROI) used to assess the image properties. The positions of the ROIs for the assessed can be found in Table 3.12.

Table 3.12: Regions of Interest for the Physical Phantom image assessment.

|  |  | Background Region | Calibration Box Marker | Bone Region | Implanted Bone Marker |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Left Image | Start Pixel | 300, 750 | 464, 673 | 1415, 1223 | 1393, 1247 |
|  | End Pixel | 649, 999 | 469, 677 | 1466, 1278 | 1400, 1252 |
|  | Dimensions (Pixels) | $350 \times 250$ | 6x5 | 52x56 | $8 \times 6$ |
| Right <br> Image | Start Pixel | 1600, 750 | 1773, 684 | 757, 1191 | 743, 1215 |
|  | End Pixel | 1949, 999 | 1778, 687 | 830, 1272 | 750, 1221 |
|  | Dimensions (Pixels) | 350x250 | $6 \times 4$ | 74x82 | $8 \times 7$ |



Figure 3.24: Physical Phantom Reference Image Pair with assessed Regions of Interest. Region A: Image Background. Region B: Bone. Marker C: Calibration Box Marker. Marker D: Bone Implanted Marker

From the assessment of the ROI-A in the images the background noise of the image was calculated as 16.85 for the left image and 10.50 for the right image. The mean signal intensities, marker contrast, SNR and CNRs for the physical phantom images are reported in Table 3.13.

Table 3.13: Physical Image Properties.

|  |  | Left Image | Right Image |
| :---: | :---: | :---: | :---: |
| Background Noise ( $\sigma$ ) |  | 16.85 | 10.50 |
| Mean <br> Signal Strength | Background ROI (A) | 98.83 | 36.92 |
|  | Bone ROI (B) | 161.96 | 56.85 |
|  | Calibration Box Marker (C) | 244.77 | 212.83 |
|  | Bone Marker (D) | 246.65 | 222.50 |
| Contrast | Calibration Box Marker | 145.93 | 175.91 |
|  | Bone Marker | 84.68 | 165.65 |
| Noise <br> Ratios | SNR | 5.86 | 3.52 |
|  | CNR <br> (Calibration Box) | 8.66 | 16.75 |
|  | CNR (Bone) | 5.03 | 15.77 |

### 3.3.1.2 Simulated Phantom Imaging

The simulated phantom images were assessed likewise. In the case of the simulated images, the left and right image had identical background intensities, therefore only the left image was assessed.

Table 3.14: Regions of Interest in the Simulate Reference Image

|  | Start Pixel | End Pixel | Dimensions |
| :---: | :---: | :---: | :---: |
| Background | 750,300 | 999,649 | $250 \times 350$ |
| Calibration Box | 673,420 | 677,424 | $5 \times 5$ |
| Marker | 1167,1615 | 1190,1634 | $24 \times 20$ |
| Bone Segment | 1175,1643 | 1179,1647 | $5 \times 5$ |
| In Bone Marker |  |  |  |



Figure 3.25: Simulated Phantom Left Reference Image with assessed Regions of Interest. Region A: Image Background. Region B: Bone. Marker C: Calibration Box Marker. Marker D: Bone Implanted Marker. The image colour has been inverted to be compared to the physical phantom image pair.

Due to the perfection of the signal source in the simulated image, the assessment of the ROI-A yielded a result of 0 for the image background noise. The mean signal intensities, marker contrast, SNR and CNRs for the physical phantom images are reported in Table 3.15.

Table 3.15: Simulated Image Properties

|  |  | Simulated Image |
| :--- | :---: | :---: |
| Background Noise ( $\sigma$ ) |  | 0.0 |
| Mean | Background ROI (A) | 100.73 |
| Signal | Bone ROI (B) | 114.01 |
| Strength | Calibration Box | 219.32 |
|  | Marker (C) | 194.08 |
| Contrast | Cane Marker (D) | 118.59 |
|  | Marker | 80.07 |
| Noise | Bone Marker | $\infty$ |
| Ratios | CNR (Calibration Box) | $\infty$ |
|  | CNR (Bone) | $\infty$ |

### 3.3.2 Precision Results

To delineate the precision of the T 4 measurement and T 8 migration measurement the terms superior precision and inferior precision are used. The superior precision pertains to the assessment of the T4 migration in reference to the L1 vertebral marker cluster while the inferior precision pertains to the assessment of the T8 migration, also in reference to the L1 marker cluster. Due to their large size, the data created and the precision calculations are not included here. They are, however, included in this thesis, located in Appendix E, Section E.2.

The resultant superior precision calculated for the phantom and simulated models are shown in Table 3.16 and graphically shown in Figure 3.26.

Table 3.16: Superior Precisions generated by the Phantom and Simulated model assessments

|  | $\mathbf{X}(\mathrm{mm})$ | $\mathrm{Y}(\mathrm{mm})$ | $\mathrm{Z}(\mathrm{mm})$ | $\mathrm{Rx}(\mathrm{deg})$ | $\mathrm{Ry}(\mathrm{deg})$ | $\mathrm{Rz}(\mathrm{deg})$ | $\mathrm{MTPM}(\mathrm{mm})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Phantom | 0.2438 | 0.0553 | 0.2001 | 0.3706 | 0.4554 | 0.1382 | 0.2185 |
| Simulated | 0.2725 | 0.0488 | 0.2640 | 0.4112 | 0.3810 | 0.2460 | 0.2461 |



Figure 3.26: Calculated Superior Precision

The inferior precisions calculated for the phantom and simulated spinal models are shown in Table 3.17 and graphically shown in Figure 3.27.

Table 3.17: Inferior Precisions generated by the Phantom and Simulated model assessments

|  | $\mathrm{X}(\mathrm{mm})$ | $\mathrm{Y}(\mathrm{mm})$ | $\mathrm{Z}(\mathrm{mm})$ | $\mathrm{Rx}(\mathrm{deg})$ | $\mathrm{Ry}(\mathrm{deg})$ | $\mathrm{Rz}(\mathrm{deg})$ | $\mathrm{MTPM}(\mathrm{mm})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Phantom | 0.1319 | 0.0544 | 0.1490 | 0.2987 | 0.2902 | 0.1766 | 0.1147 |
| Simulated | 0.1963 | 0.0429 | 0.1175 | 0.4192 | 0.4697 | 0.1892 | 0.1630 |



Figure 3.27: Calculated Inferior Precision.

### 3.3.3 Precision Comparison

The data from the two spinal models were compared to assess the validity of the simulated RSA environment. Each directional precision was assessed independently for their variance agreement. To do this the distribution of the datasets is required.

### 3.3.3.1 Dataset Distribution

Each of the twenty-eight datasets (there were seven directions assessed for each migratory vertebra and two migratory vertebrae for each of the two assessed models) was analyzed using an Anderson-Darling test in Minitab 16 to check their distribution. Resultant p-values greater than 0.05 indicated that a dataset was normally distributed. The
results from the assessment of the superior and inferior precision datasets are summarized in Table 3.18. As it can be seen the majority of the data recorded was normally distributed.

Table 3.18: Distribution of the precision datasets.

| Assessed | Superior Aspect |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Direction | Phantom |  | Simulated |  |
|  | p- value | Normalcy | p- value | Normalcy |
| X | 0.034 | Non-Parametric | 0.216 | Normal |
| Y | 0.078 | Normal | 0.700 | Normal |
| Z | 0.477 | Normal | 0.608 | Normal |
| Rx | 0.714 | Normal | 0.545 | Normal |
| Ry | 0.423 | Normal | 0.497 | Normal |
| Rz | 0.723 | Normal | 0.008 | Non-Parametric |
| MTPM | $<0.005$ | Non-Parametric | 0.893 | Normal |
|  | $\quad$ Inferior Aspect |  |  |  |
|  | Phantom |  |  |  |
| X | 0.093 | Normalcy | p- value | Normalcy |
| Y | 0.959 | Normal | 0.061 | Normal |
| Z | 0.928 | Normal | 0.257 | Normal |
| Rx | 0.806 | Normal | 0.522 | Normal |
| Ry | 0.814 | Normal | 0.406 | Normal |
| Rz | 0.424 | Normal | 0.046 | Non-Parametric |
| MTPM | $<0.005$ | Non-Parametric | 0.524 | Normal |

### 3.3.3.2 Variance Assessment

An example of the graphical output for a test of equal variance, the analysis of the inferior X rotation is shown in Figure 3.28.


Figure 3.28: Test for equal variance of the $\mathbf{R x}$ direction for the inferior aspect.
In this assessment, both of the two datasets are normally distributed and therefore the F-Test was used. With a p-value of 0.160 this assessment shows that there was no statistical difference between the phantom and simulated models in their X rotational assessment. A full summary of all variance assessment results can be found in Table 3.19.

Table 3.19: Summary of the results of the assessment of equal variance between the physical and simulated models.

| Assessed <br> Direction | Superior Aspect |  |  | Inferior Aspect |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Statistical | p- value | Statistical | Statistical |  |  |
|  | Test | p-value | Statistical <br> Difference |  |  |  |
| $\mathbf{X}$ | Test | Levene's | 0.739 | No | F-Test | 0.100 |
| Y | F-Test | 0.597 | No | F-Test | 0.324 | No |
| $\mathbf{Z}$ | F-Test | 0.250 | No | F-Test | 0.322 | No |
| Rx | F-Test | 0.663 | No | F-Test | 0.160 | No |
| Ry | F-Test | 0.457 | No | Levene's | 0.211 | No |
| Rz | Levene's | 0.297 | No | F-Test | 0.773 | No |
| MTPM | Levene's | 0.431 | No | Levene's | 0.209 | No |

From Table 3.19 it can be seen that there is no statistical difference between any of the RSA precision datasets of the physical and simulated models.

### 3.4 Simulation Precision Validation Discussion

The use of a simulated RSA assessment has been previously used by Madanat et al (2006). They found that in the assessment of distal radius fractures, "... a computer simulation model can be accurately used to replace phantom models in the simulation of RSA studies" [59]. Their use of a computer simulated model and POV-Ray ray-tracing showed "very high correlation" between the simulated movements and the RSA measurement output [59]. This assessment ascertained that a simulated RSA environment provides measurement accuracy comparable to that of physical RSA systems. The article concluded that the use of simulated RSA assessments proved an opportunity for accurate creation of complex movements without the errors associated with the use of micrometers. It was also stated that the use of simulated RSA exams provide a vehicle for the further development of model based RSA. They further concluded that the use of simulated RSA exams can provide fast and cost-effective means for the performing of RSA studies compared to the associated costs of using of physical radiographs and phantoms [59].

The use of a simulated RSA environment has been previously used at this institution by Francis (2009) [27]. He concluded that the simulated environment provided an adequate vehicle for the assessment of the use of RSA in the assessment of the success of spinal fusions. This project used his foundation to further the project goal with the object of assessing the validation of the use of the simulated RSA Environment.

From the foundation work, significant alterations were made to the simulation process to try and create a more realistic x-ray simulation. The impact of these changes on the realism of the simulation remained unknown without a side-by-side comparison study.

One of the most significant impacts of the process improvements was the change in the spatial resolution of the simulated images. The material attenuation method creates a change in the visualization of object edges, enhancing simulation realism. An example of this change is shown in Figure 3.29. With the surface attenuation technique, the photon signal is at either a full and unobstructed strength, or attenuated to a material's contrast strength. However, the material attenuation technique creates a shadow effect where the signal is partially attenuated, like the light grey areas on the right in Figure 3.29. This creates an edge blurring effect. Due to the angle of the x-ray tube to the image detection plate, the shadow effect is not symmetric for the objects. This is standard in RSA exams.


Figure 3.29: Simulated Photon Attenuation Techniques. Both markers shown are the \#1 marker of the L 1 marker cluster and were placed a similar distance from the image detectors during simulated imaging.

The edge blurring created by the material attenuation technique is essentially an application of the edge spread function which causes objects to lose definition, impacting special resolution. Due to the intrinsic magnification factor created through the use of the diverging photon rays emitted from the x-ray foci, projections cast by objects in the field of view are enlarged; loosing definition at their edges the further they are from the image detectors [56]. This effect is shown in Figure 3.30.


Figure 3.30: Magnification Blurring. A) Fiducial marker located close to the image detectors showing well defined marker edges. B) Marker \#1 located in the T4 vertebra shows much more edge blurring, obscuring the marker edge definition. The image was taken from a section of the left image of the superior spine section's reference exam.

The further an object is from the image detector, the greater the blurring. This is why the projections of the fiducial markers [Figure 3.30 A ] have a much more defined outline than those of the rigid body markers [Figure 3.30 B ]. This simple factor, not seen with the surface attenuation technique, adds realism to the simulation previously overlooked. Neither the point spread nor edge spread functions have been defined for the computer simulated RSA set-up.

The first objective of this thesis was to conduct a comparative side-by-side precision assessment of the physical and simulated RSA environments. This comparison found no statistical difference between the any of the recorded precisions of the two environments. The lack of statistical difference validates the use of the simulated RSA process in research performed on the use of RSA in the assessment of multi-level spinal fusion success.

### 3.4.1 Spinal Fusion Precision Comparison

The precision produced by both the physical and simulated phantom models underperformed those reported in the literature. All precision values reported in other RSA applications were on the order of hundredths to thousandths of a millimetre and tenths to hundredths of a degree. The precision recorded during the simulation validation process was on the order of tenths of a millimetre for translational precision and tenths of a degree for the rotational precision. It was expected that this thesis would cover the most precise modeling situation before adding on additional complexities and sources of error much like the Allen et al (2004) study looked at three levels of RSA modeling (Plexiglas, Sawbones and In Vivo modeling) [63].

The poor precision results presented in this thesis are expected to be due to the large measurement vectors used in the assessment of multilevel spinal fusions. In other applications, like those in the knee, hip and single level spinal fusions, the measurement vectors are limited [1], [2], [26], [28], [34], [59-61], [63]. The reduced length in measurement vectors lowers the error associated with misalignment of the origin marker cluster. In a preliminary experiment conducted after the conclusion of the thesis data collection, simulated single level spinal fusions showed greatly improved precision responses.

### 3.4.2 Limitations

Although improvements were made over previous simulation work, there remain several limitations within the simulated RSA environment.

### 3.4.2.1 Anatomical Information

The anatomical information used to construct the CAD models used in the RSA simulation was adapted from two publications by Panjabi et al (1991, 1992) [67], [68]. The published measurements were average anatomical measurements taken from healthy adult donor vertebrae. At the standard age at which spinal fusions are often performed for scoliosis patients, the skeleton is matured reaching its adult proportions. Although there is little size discrepancy between the average vertebrae and patient vertebrae, there can be significant individual anatomical variation, especially when examining a patient with scoliosis.

During the conversion from average anatomical measurements to CAD models small anatomical structures were discarded. Examples of discarded structures are the neuroforamen and the facet joints. These structures are not modeled due their meaninglessness in RS assessment or their removal in the surgical setting.

The loss of boney anatomical structures and measurements was not deemed to significantly impact the validity of the use of the vertebral models. RSA does not use the anatomical structures themselves for reference points, therefore the alterations made to create the CAD models of the simulated vertebrae are of little consequence. With the vast difference in the x-ray attenuation properties of the materials, the tantalum markers and ASI implants are clearly recognizable, no matter the anatomical structures simulated.

### 3.4.2.1.1 Soft Tissue Envelope

Currently the simulation does not contain a soft tissue envelope. The absence of soft tissue decreases the realism of the simulation as soft tissue interacts with the projected x-rays. The opacity caused by the presence of soft tissue negatively impacts the image clarity and marker visibility, as well as creating tissue induced x-ray scatting which increases image noise characteristics. The presence of a soft tissue envelope would decrease the marker contrast, decreasing the contrast to noise ratio.

The scope of the phantom models produced during this thesis was limited to 'dry' phantoms to limit the sources of error. Currently the images produced without a soft tissue envelope are overly accurate and precise, representing the best case scenario for RS assessment of multi-level spinal fusion success. Future work will inevitably involve the addition of a soft tissue envelope as RS assessment of spinal fusions progresses from computer simulation toward clinical application.

### 3.4.2.2 Model Scaling

The use of an $80 \%$ scale model to conduct the simulation validation objective of this thesis was done to ensure that the model comfortably fits within the available imaging area when utilizing the traditional Caudal Origin Style. The utilization of the scaled phantoms is akin to the selection of a smaller patient or patient with a shorter fusion length to undergo RS assessment. The vertebral models used in the construction of the scaled phantoms are full size representations, having not undergone size reduction. This provides spatially larger maker clusters than would be present in a smaller sized patient.

The use of a scaled model has a potential impact on the recorded precision of the RSA system. The precision impact of this scaling was not categorized during the course of this thesis but is expected to have a linear effect. As well the utilization of the spatially larger marker clusters decreases the misalignment in matching the cluster's orientation, improving system precision over the use of marker clusters sized to the anatomical proportions of a smaller patient.

The use of scaling is not expected to have any effect on the conclusions constructed by this thesis as the use of scaled simulated and physical phantom models were segregated from the use of the full sized simulated phantoms. Therefore the compared results between the physical and simulated RSA environment were conducted on identical constructs and are directly comparable.

### 3.4.2.3 Image Rendering

The last of the simulation limitations is the material attenuation properties. The coefficients used in the simulations were approximated from images during from a single phantom study. It was not the focus of this thesis to recreate the RSA environment exactly, and as such the approximation of the material attenuation factors was deemed satisfactory. A comparison of the original simulation, the upgraded simulation and an image of a phantom model can be found in Figure 3.31.


Figure 3.31: A comparison of T4 vertebrae showing the x-ray attenuation techniques. A) Simulated RSA image using the surface attenuation technique. B) Simulated RSA image using the material attenuation technique. C) RSA image of a phantom model of the spine.

Another limitation is the lack of signal noise present in the images produced. The simulation is "perfect" in that there is no detector noise, signal loss, or other image degradations present in the simulation. Previous work tried to introduce background noise to the images through the use of photo manipulation but this was not done with this simulation procedure. This lack of signal noise is expected to cause the simulation to be overly acute in selecting the RSA markers and allowing for reduced rigid body error and higher marker cluster accuracy. Due to the previously demonstrated acuity in a physical phantom study, the absence of noise in not expected to greatly impact system accuracy and precision but further research should be conducted.

### 3.4.3 Conclusion

In both qualitative and quantitative measures, the simulated RSA environment accurately emulates the physical RSA environment of the Halifax Infirmary's RSA Suite. The simulated RSA environment has undergone a parallel comparison with the physical counterpart and has been shown to replicate its performance with no statistically significant differences in the system precisions. The RSA simulation process continues to pass validation assessments and continues to demonstrate adequate validation for the use in research into the use of RSA in multilevel spinal fusion success assessment.

# Chapter 4- Thesis Objective \#2: Assessment of Novel RSA Origin Styles Used for Spinal Fusion Success Analysis 

### 4.1 Introduction

Work by Francis (2009) found physical size limitations effecting the use of the Halifax Infirmary's RSA suite in the assessment of the success of spinal fusions [27]. He found that the length of his average sized phantom model did not adequately fit within the constraints of the diagnostic imaging area. To compensate for this limitation, the simulated environment was adjusted to fit the simulated spinal model. Adjustments to the physical RSA set-up were not feasible so alternative solutions for the spine length were required.

To compensate for the limited imaging length, two new migrational measurement origin styles were created. These two origin styles section the fused spine into two discreet sections imaged in two separate RSA exams. By using two RSA image sets the available imaging area was effectively doubled. The definitions of the novel origin styles, the Apex and Dual Origin Styles, are described in Sections 4.1.1.2 and 4.1.1.3.

The purpose of this second thesis objective is to investigate the implications of the new origin styles on the accuracy and precision of the use of RSA in the assessment of spinal fusion success. The accuracy and precision are dependent on the components of the RSA set-up, including the migration origin style. To be deemed a valid method of assessing the success of spinal fusions, the performance of the new origin styles must
match or exceed the performance of the traditionally used Caudal Origin Style. The Caudal Origin Style represented the benchmark used in this thesis. The process for the testing of the three origin styles is shown in Figure 4.1.


Figure 4.1: Process flow chart of the testing of the three origin styles. Green Path - Caudal Origin Style, Red Path Apex Origin Style, Blue Path - Dual Origin Style

### 4.1.1 RSA Origin Styles

Three origin styles were examined for their impact on accuracy and precision. The Caudal Origin Style was assessed as a legacy style used in previous project work and throughout the literature. The Apex and Dual Origin Styles, created to compensate for the limited RSA imaging field of view, are novel to this thesis alone.

### 4.1.1.1 Caudal Origin Style

The Caudal Origin Style, simply put, uses the marker cluster at the inferior end of the scoliotic curve as the inter-vertebral migration origin. This origin style was used in previous project work and has been used in the literature, most notably in the study by Pape et al (2002) where the translational Limits of Clinical Significance were defined [1].

In this thesis the Caudal Origin Style compares all movement of the investigated model to the location of the L1 vertebra, Figure 4.2 using a coordinate style defined at the spinal origin. A full definition of the Caudal Coordinate System can be found in Appendix B. This style necessitates that all rigid body marker clusters be fully captured by a single RSA exam image pair.


Figure 4.2: The Caudal Origin Style and Caudal Coordinate System. The orange pentagon is the migration origin located at the $L 1$ vertebra. The green triangles are the migrating rigid bodies, the T4 and T8 vertebrae. The blue and red arrows are the superior and inferior linear measurement vectors respectively.

The origin style allows for the single exam assessment of all motion within the fusion, a characteristic not found in the succeeding origin styles. This origin style potentially has the lowest patient radiological dose using only one RSA image set. To achieve proper patient placement allowing for the entire fusion length to be imaged, additional image pairs that may be required. This could negatively impact the low dosage characteristics of this origin style.

Fusion failure localization is achievable using the Caudal Origin Style but this is not as intuitive as the localization found with the other origin styles. Migration of both the T4 and T8 marker clusters must be assessed simultaneously to determine failure localization. To determine if a failure is located in the superior section of the spine, the inferior (T8) migration must be subtracted from the T4 migration. Failure in the inferior
section of the spine is identified by solely assessing the migration of the T8 vertebra with respect to the L 1 origin.

In this thesis the simulated patient was placed in a supine position, rather than the prone position used in the previous project analysis [27]. This alteration was done to match current clinical placement positioning, which is more comfortable for the patient. There was no significant difference observed in image quality or RSA applicability between the two patient placement options during preliminary work done for this thesis.

To image the entire spine model during the assessment of the Caudal Origin Style, the origin of the spine model was placed at the point $\langle 420,30,450\rangle \mathrm{mm}$ in the RSA Coordinate System. The model was aligned so that the Spinal Coordinate System aligned with the RSA Coordinate System. This position was defined as the model's reference position for the Caudal Origin Style.

### 4.1.1.1.1 Caudal Origin Style Limitations

This origin style has limitations which precludes it from use in the local clinical setting. The Caudal Origin Style requires that the full length of the spine fit with the area of the image detectors. The image detectors available at the Halifax Infirmary severely limit the length of fusion that can be assessed using the caudal origin style. The maximum fusion length that can be assessed is approximately 300 mm . This restrictive length would prohibit the use of RSA on a large portion of the patient pool.

The use of the Caudal Origin Style will not be the origin style used during future clinical applications of RS assessment of spinal fusion success at this center. The size limitations are equipment dependent, therefore other equipment may allow for larger
fusion lengths to be assessed using the Caudal Origin Style. The Caudal Origin Style has been previously used by Francis (2009) and in other published literature [1], [2], [27]. Although it will not be used clinically at this center in the future, the Caudal Origin Style has been included in this thesis to provide a benchmark for the new, alternate migration assessment techniques proposed.

### 4.1.1.2 Apex Origin Style

The Apex Origin Style is one that utilizes the vertebra located at the apex of the scoliotic curve as the migration origin, Figure 4.3. A full definition of the Apex Coordinate System used in this origin style can be found in Appendix B.


Figure 4.3: The Apex Origin Style and associated Apex Coordinate System. The orange pentagon is the migration origin located at the $\mathbf{T 8}$ vertebra. The green triangles are the migrating rigid bodies, the $T 4$ and L1 vertebrae. The blue and red arrows are the superior and inferior linear measurement vectors respectively. The green and purple rectangles represent the superior and inferior RSA exam areas respectively.

Having the migration origin in the center of the fusion allows for the sectioning of the spine into two image sets that are analyzed separately in two separate RSA exams. This sectioning of the spine into two image sets relies on the use of vertebra located at the apex of the scoliotic curve. The T8 vertebra is present in both image sets, which gives both exams a common reference marker cluster. A comparison between the image sets produced from the Caudal and Apex Origin Styles can be seen in Figure 4.4. The positions of the spine origin within the RSA Coordinate system for the two image pairs were: $<420,-46,560>\mathrm{mm}$ for the image pair of the superior section of the spine and $<420,85,560>\mathrm{mm}$ for the image pair capturing the inferior section of the spine. As with the Caudal Origin Style, the spine was orientated so that the Spinal Coordinate System aligned with the RSA Coordinate System.


Figure 4.4: Comparison of the image sets required for the Caudal Origin Style (A) and Apex Origin Style (B). The T8 vertebra is present on both image sets of (B) allowing it to be the migration origin. Each image is has the same dimensions ( $2208 \times 2688$ pixels covering $353 \times 430 \mathrm{~mm}$ ).

Sectioning the fusion into superior and inferior halves effectively doubles the length of the diagnostic imaging area. This removes the size limitation placed on patients by the Caudal Origin Style. As can be seen in Figure 4.4 (B), the phantom model now fits
comfortably within the diagnostic imaging area. Conversely with the Caudal Origin Style, any global movement in the inferior direction would cause the L1 vertebra to be pushed partially outside the image area, degrading RSA performance. Superior movement in the Caudal Origin Style similarly impacts the visibility of the markers within the T4 vertebra.

The use of the Apex Origin Style allows for the easy localization of fusion failure. A failure in either the superior or the inferior section of the fusion would only appear in the corresponding RSA exam while the other fusion section exam would show no movement. The use of the Apex Origin Style will also reduce the distance between the origin and the T4 vertebral marker cluster, reducing misalignment error and hopefully improving system precision.

As with most improvements, this new origin style is not without drawbacks. The most significant of these drawbacks is the increased radiological dose experienced by the patient over the caudal benchmark. An increase in the number of image sets increases the effective dose accordingly. Precise patient placement must be achieved to satisfy the requirement that the apex vertebral marker cluster fully appear within both RSA image sets, which leads to the potential use of additional image sets to achieve proper patient placement, further increasing patient effective dose.

With the use of additional RSA exams the use of technician and equipment time is similarly affected. However, this is not a major increase in resource usage and is not a significant concern.

### 4.1.1.3 Dual Origin Style

The Dual Origin Style is the second origin style developed for this thesis. This origin style, like the Apex Origin Style, sections the fusion into a superior and inferior aspect with the apex marker cluster common to both image sets. The Dual Origin Style uses the same superior and inferior RSA image sets as the Apex Origin Style. This means it shares many of the advantages and disadvantages associated with the Apex Origin Style. As with the Apex Origin Style, the use of the Dual Origin Style increases the diagnostically important imaging area as well as increasing patient experienced radiation dose over the Caudal Origin Style benchmark.

The Dual Origin Style differs from the Apex Origin Style by using the marker clusters at both the superior and inferior ends of the fusion as the migration origin (Figure 4.5), instead of using the apex marker cluster. Unlike the other two origin styles, this technique uses two coordinate systems; one for each RSA image pair. The origin for the superior and inferior coordinate system is located at the T4 and L1 vertebral origin respectively. A full definition of these coordinate systems can be found in Appendix B.


Figure 4.5: The Dual Origin Style and Dual Coordinate Systems. The orange pentagons are the migration origins located at the $T 4$ and $L 1$ vertebrae. The green triangles are the migrating rigid body, the $T 8$ vertebra. The blue and red arrows are the superior and inferior linear measurement vectors respectively. The green and purple rectangles represent the superior and inferior RSA exam areas respectively.

The migration measurement is inward toward the apex of the curve with the superior and inferior migration measured independently of one another. In this respect, like the Apex Origin Style, the localization of fusion failure is self-evident as displacements in either the superior or the inferior sections of the spine.

Lastly, the use of this origin technique reduces the possibility of the migration origin undergoing rotational displacement. The T4 and L1 vertebrae are unlikely to rotate as they need to maintain alignment with the native spine. The rotation of the T8 (curve apex) vertebra has, in large rotations, led to the occlusion of rigid body RSA markers. The reduction in the visibility of origin markers reduces matching marker pairs which can impact the misalignment error, reducing precision of the Apex Origin Style. The use of the Dual Origin Style alleviates this complication.

### 4.2 Origin Style Assessment Methodology

### 4.2.1 Accuracy Assessment

The validation of the accuracy of the developed origin styles was conducted through manipulations to the simulated phantom model. The T4 and T8 vertebrae were adjusted to create displacements used to assess the translational and rotational accuracy.

### 4.2.1.1 Translational Accuracy

Studies conducted by Madanat et al (2005, 2007), Önsten et al (2001), Wilson (2007), and Laende et al (2009) used a Prediction Interval (PI) method to determine system accuracy from a range of implemented displacements [28], [34], [59-61]. Directional accuracies in these studies were determined to be half the width of the average PI. Prediction Intervals are a statistical method of estimating, within a set confidence, an interval in which future data points will fall.

The Prediction Interval method uses collected data to determine a range in which future values are expected with $95 \%$ confidence. The calculation is similar to Confidence Intervals (CI) except that a confidence interval estimates the distribution of a true population. The difference in the determination of the PI and the CI for a set of normally distributed data is graphically shown in Figure 4.6. The accuracy of an RSA system is determined for a direction by taking the $1 / 2$ width of the average prediction interval for the assessed direction.


Figure 4.6: Example showing the $\mathbf{9 5 \%}$ Prediction Interval in blue versus $\mathbf{9 5 \%}$ Confidence Interval in red. The dataset is a normally distributed set of random variables generated in Microsoft Excel 2007®.

The translational displacements used to assess accuracy were selected to represent the range of movements found in failed fusions in several RSA studies. In a study of the cervical spine, Lee et al detected motions of 0.35 to 35 mm while Johnsson et al observed motions of 0.4 to 10 mm in a study focused on the lumbar spine [8], [9]. The protocol used for the assessment of the translational accuracies of the three origin styles is the use of ten displacements covering a range of -20 to 20 mm along all three of the principal axes. Each direction was investigated independently from all other movements. Figure 4.7 shows a graphical representation of the implemented displacements.


Figure 4.7: Induced displacements used to assess system translational accuracy.
To assess translational accuracy, failures of both the superior and inferior sections of the fusion were independently simulated. To simulate a failure in the superior section of the spine, the T 4 vertebra was moved in relation to the rest of the spine, Figure 4.8. Simulating a failure in the inferior section of the spine, the T4 and T8 vertebrae were moved, as a solid unit, with respect to the L1 vertebra, Figure 4.9. The induced displacements used for the assessment of the accuracy displacement are summarized in Table 4.1. The repeated translational movements were induced in all three principal directions ( $\mathrm{X}, \mathrm{Y}$, and Z ) of the Spinal Coordinate System. Each migration was independently induced and was measured using the three developed RSA origin styles.


Figure 4.8: Superior Fusion Failure Translational Accuracy Movement A) Reference Position. B) -X direction migration movements of the $T 4$ vertebral model simulating a superior fusion failure. Migration range from 0.5 mm to 20 mm .


Figure 4.9: Inferior Fusion Failure Translational Accuracy Movement A) Reference Position. B) -X direction migration movements of the T4 and T8 vertebral models simulating an inferior fusion failure. Migration range from 0.5 mm to 20 mm

Table 4.1: Manipulations used to assess translational accuracy of one cardinal direction. Migrations are in relation to the Spinal Coordinate System.

| Migration | Superior Failure |  | Inferior Failure |  |
| :---: | :---: | :---: | :---: | :---: |
| Scene \# | T4 migration | T8 migration | T4 migration | T8 migration |
|  | $(\mathrm{mm})$ | $(\mathrm{mm})$ | $(\mathrm{mm})$ | $(\mathrm{mm})$ |
| $\mathbf{1}$ | 20 | 0 | 20 | 20 |
| $\mathbf{2}$ | 10 | 0 | 10 | 10 |
| $\mathbf{3}$ | 5 | 0 | 5 | 5 |
| $\mathbf{4}$ | 1 | 0 | 1 | 1 |
| $\mathbf{5}$ | 0.5 | 0 | 0.5 | 0.5 |
| $\mathbf{6}$ | -0.5 | 0 | -0.5 | -0.5 |
| $\mathbf{7}$ | -1 | 0 | -1 | -1 |
| $\mathbf{8}$ | -5 | 0 | -5 | -5 |
| $\mathbf{9}$ | -10 | 0 | -10 | -10 |
| $\mathbf{1 0}$ | -20 | 0 | -20 | -20 |

The thresholds used as the translational Limits of Clinical Significance 0.3, 0.5, and 0.7 mm in the transverse (X), vertical (Y), or sagittal (Z) spinal axes, respectively as defined by Pape et al (2002) [1].

### 4.2.1.2 Rotational Accuracy

Rotational accuracy has not been assessed in many RSA studies performed on spinal fusions in the literature and as a result does not have a defined rotational accuracy testing protocol. Johnsson et al (2002) determined that the limit of clinical significance for rotational movements in the spine was $2.0^{\circ}, 0.5^{\circ}$, and $0.9^{\circ}$ about the transverse (X), vertical (Y), or sagittal (Z) spinal axes respectively [2]. Although not in the spine, Madanat et al (2005 and 2007) and Laende et al (2009) used the same PI protocol to assess the rotational accuracy as with the translational accuracy assessment protocol [5961].

To simulate a rotational failure of the fusion, rotational displacements were induced in the T 8 vertebra. The vertebra was rotated around the centroid of the marker
cluster, Figure 4.10. The centroid of the T8 marker cluster is located at the point $<0.14$, 10.07, $-25.21>\mathrm{mm}$ in the T8 Vertebral Coordinate System. For a full definition of the rotational coordinate system see Appendix B. The use of the marker cluster centroid as the rotational origin limited the induced displacement to a purely rotational means, as opposed to a rotational and translational displacement pair found when rotating around the T8 Vertebral Coordinate System, whose origin was not located at the marker cluster centroid.


Figure 4.10: Rotational origin of the T8 vertebra located at the centroid of the marker cluster.
An example of a $-10^{\circ}$ rotation around the Z axis is shown in Figure 4.11 with a summary of the eight displacements that were induced around all three principal axes shown in Table 4.2.

Table 4.2: Rotations induced during rotational accuracy assessment.

| Migration Scene \# | T8 Rotation (deg) |
| :---: | :---: |
| $\mathbf{1}$ | 10 |
| $\mathbf{2}$ | 6 |
| $\mathbf{3}$ | 3 |
| $\mathbf{4}$ | 1 |
| $\mathbf{5}$ | -1 |
| $\mathbf{6}$ | -3 |
| $\mathbf{7}$ | -6 |
| $\mathbf{8}$ | -10 |



Figure 4.11: Rotational Accuracy Movement A) Reference Position B) Movement of the T8 vertebral model simulating a $10^{\circ}$ rotational failure about the $Z$ axis.

All rotations induced on the T8 vertebrae were conducted independently of one another. Only one rotation about one axis was completed in each case. This eliminated concerns over the order of rotations applied. If a combination rotation is applied to the vertebra, the order of rotation becomes significant, that is an X rotation followed by a Y rotation is different than a Y rotation followed by an X rotation. The measurement of this
rotational displacement also poses sources of error. The measurement of a series of combination rotations can produce a situation of crosstalk between the assessed rotational axes, which can impact the results if the measurement technique follows a different order of rotational assessment than was used to apply the rotations.

The choice to not conduct combination rotation was made to limit the sources of measurement errors and examine the best possible system rotational accuracy scenario.

### 4.2.1.2.1 Apex Rotation Calculations

Calculations conducted using the MB-RSA program produced erroneous translational migrations of the T4 and L1 vertebrae when assessing the rotational displacements of the T8 vertebrae using the Apex Origin Style. The MB-RSA software does not create local coordinate systems of the individual marker clusters but assesses all migrations by matching the migration scene with the reference scene and examining the migrations with respect to the global RSA environment. This means that the entire migrating scene was rotated to match the position of the T 8 origin in the reference scene, producing a situation where both the T4 and L1 vertebrae have been moved. An example of this scene rotation is shown in Figure 4.12. Local coordinate systems can be created for manufactured implants, such as tibial components of artificial knees, but the process is impractical for patient specific, rigid body marker clusters implanted into the bone.


Figure 4.12: Alignment of the Migration and Reference scenes in MB-RSA. Red marker clusters are the Reference Scene. Green marker clusters are the migration scene of $\mathbf{1 0}^{\mathbf{0}}$ rotation of the $\mathbf{T 8}$ cluster about the Z -axis.

To use a local coordinate system located at the T8 vertebra, post processing was required. A MatLab program, found in Appendix D Section D.2.3, was used to calculate the rotational displacements for the Apex Origin Style using a local coordinate system. For the T 8 vertebral marker cluster, a local coordinate system was defined by the MatLab program. This program used the marker locations originally determined by the MB-RSA software. The core function used in this program was developed by E. Laende and has been reproduced with permission.

This sort of post processing will be required for all clinical RSA exams performed on the spine. The post processing was not necessary during this study because the migration origins were not rotated with the exception of the Apex Origin as discussed above.

### 4.2.1.3 Accuracy Statistical Assessment

Each of the simulated models for the translational and rotational fusion failures were used to create a RSA image pair using the image simulation process previously described. These "migrating scenes" for each origin style were compared to the corresponding "reference scene" to generate each data point assessed.

Each origin style, for both translation and rotation, was assessed for its absolute accuracy, confirming that it was measuring the induced displacements to within the acceptable Limits of Clinical Significance. This assessment was accomplished through the application of Bland-Altman (BA) plots. These plots allow for the visual evaluation of datasets, comparing the agreement between the measured values and those of the induced displacement. They were originally developed by Bland and Altman in 1986 and have achieved significant usage within the medical research community [4]. Each origin style was a unique "measurement technique" to compare with the known, induced displacement. Each data point, representing a unique accuracy migration, equate to a separate "patient" as described by the original Bland-Altman paper. This necessitates the use of three individual BA plots for the assessment of the accuracy of each direction (one for each origin style assessed).

Since the analysis contained a reference value for one of the measurement techniques, the expected outcome (the X -axis value of the BA plot) was not an average of the two measurement techniques but the true induced displacement value. The use of this technique over that of an average reference value was discussed by Krouwer et al (2008) [71].

For a measured dataset to agree with the true implemented values, the limits of agreement of the BA plots must fall within the Limits of Clinical Significance. The limits of agreement, $L A$, are defined by Equation 4.1, where SD is the standard deviation. The mean in this equation is in reference to the mean error of the measured dataset. The limits of agreement represent a $95 \%$ confidence limit around the mean.

$$
L A=M e a n \pm 1.96 \times S D
$$

Equation 4.1

The results of the BA plots were assessed against the translational and rotational Limits of Clinical Significance as determined by Pape et al (2002) and Johnsson et al (2002) respectively [1], [2]. The Limits of Clinical Significance are summarized in Table 4.3. In graphical analysis, Limits of Clinical Significance have been abbreviated to LoCS.

Table 4.3: Translational and Rotational Limits of Clinical Significance from Pape et al (2002) and Johnsson et al (2002) [1], [2].

|  | $\mathbf{X}$ | $\mathbf{Y}$ | $\mathbf{Z}$ |
| :---: | :---: | :---: | :---: |
| Translational (mm) [1] | 0.3000 | 0.5000 | 0.7000 |
| Rotational (deg) [2] | 2.0000 | 0.5000 | 0.9000 |

### 4.2.2 Precision Assessment Methodology

The methods used to assess the precision of the three origin styles were similar to those used to assess simulation validity, Sections 3.2.5.2 and 3.2.5.3

To test the system precision of the three origin styles, the simulated phantom model was repositioned, as a unit, within the CAD environment with respect to the RSA Coordinate System defined by the calibration box. There was no intervertebral movement induced and as such any migration measured is erroneous and a measure of system precision. Models for all three origin styles underwent two sets of global movement. The first was that the spine model was translated 10 mm in all six cardinal directions, an example of this is shown in Figure 4.13. The second movement was that the spine model was rotated $\pm 10^{\circ}$ about all three principle global axes, shown in Figure 4.14. The manipulations used to assess system precision are summarized in Table 4.4.


Figure 4.13: Translational Precision Movement. A) Reference Position, B) Global movement of the spine model $\mathbf{- 1 0 m m}$ along the X -axis


Figure 4.14: Rotational Precision Movement. A) Reference Position, B) Global movement of the spine model $-10^{\circ}$ about the Z -axis.

Table 4.4: Global movements used to assess system precision. Each scene was assessed using the previous as the migration reference.

| Scene \# | Global Translation (mm) | Global Rotation (deg) |
| :---: | :---: | :---: |
| $\mathbf{0}$ | Reference | Reference |
| $\mathbf{1}$ | 10 X | 10 X |
| $\mathbf{2}$ | -10 X | -10 X |
| $\mathbf{3}$ | 10 Y | 10 Y |
| $\mathbf{4}$ | -10 Y | -10 Y |
| $\mathbf{5}$ | 10 Z | 10 Z |
| $\mathbf{6}$ | -10 Z | -10 Z |
| $\mathbf{7}$ | Reference | Reference |

The rotational center for the precision assessment was a point adjacent to the T8 vertebra, half-way along the length of the curve. This point was not the origin of the T8 vertebra, but a point in line with the Y -axis of the spine model defined as $<0.0,156.5$, $0.0>\mathrm{mm}$ in the Spinal Coordinate System. The full definition of this simulated model rotational coordinate system can be found in Appendix B. The position of the rotational
center was selected to centralize the rotation, keeping the spine centered in the available RSA imaging area.

When the exams were evaluated using the MB-RSA software, each model repositioning was assessed with respect to the previous position. Each repositioning of the phantom model acted as both a migrating scene with respect to the previous position and a reference scene with respect to the subsequent position.

Since there were no intervertebral displacements induced, any translational or rotational migrations calculated represent the error within the RSA system. This error is normally based on three main factors: the radiographic positioning and technique; the marker placement; and the migration calculation process, the latter of which is influenced by the origin style used. Since this is a computer simulated study, the radiographic positioning, technique and marker placement are constants, leaving only the migration calculation as the variable source of system error.

Statistical analysis and comparison of the precision of the three origin styles is identical to that used to assess the validity of the simulated RSA environment.

This statistical analysis once again uses the equation used by Madanat et al (2005) [60], reprinted as Equation 4.2, to assess system precision.

$$
\begin{equation*}
P=y \times S D \tag{Equation 4.2}
\end{equation*}
$$

where $S D$ is the standard deviation of the migration dataset ( $\Delta \mathrm{X}, \Delta \mathrm{Y}, \Delta \mathrm{Z}, \Delta \mathrm{Rx}$, $\Delta \mathrm{Ry}, \Delta \mathrm{Rz}, \Delta \mathrm{MTPM})$ and $y$ is the $95 \%$ confidence interval. In this assessment only fourteen data points were created, so $y$ is equal to 2.14 as defined from the critical values of a student t test with fourteen degrees of freedom at an $\alpha$ of 0.05 . Since precision is an
assessment of the error inherent in the RSA system and origin style, it should be as close to zero as possible.

### 4.2.2.1 Precision Statistical Assessment

To compare the precisions of the three origin styles, an assessment of their variances was undertaken. Each of the seven migration datasets ( $\Delta \mathrm{X}, \Delta \mathrm{Y}, \Delta \mathrm{Z}, \Delta \mathrm{Rx}, \Delta \mathrm{Ry}$, $\Delta \mathrm{Rz}, \Delta \mathrm{MTPM})$ for each origin style was tested for equal variance.

The method used to compare the variances is dependent on the distribution of the datasets. Again, the distributions of the datasets for all three origin styles were assessed using the Anderson-Darling test in Minitab 16. If one or more of the dataset groups were non-parametrically distributed then the Levene's test was used to compare the three variances. If all datasets were normally distributed, the Bartlett's test was used. In both tests a p-value above 0.05 indicated no statistical differences. If a significant difference was found, a second equal variance test was performed between the datasets of the Apex and Dual Origin Styles to determine if either of them was displaying a significant difference from the other.

### 4.3 Origin Style Assessment Results

### 4.3.1 Accuracy Assessment Results

For the assessment of the RSA system accuracy, migration was generated by comparing the simulated RSA exams of the Reference Scene and the various Migrating Scenes. This was done to assess both the translational and rotational accuracies.

### 4.3.1.1 Translational Accuracy

To assess translational accuracy, failure of both the superior and inferior sections of the fusion was simulated with the T 4 and T 8 vertebrae moved in all principle directions with respect to the L1 vertebra. The data collected for each principle direction and for each origin style was separated into a superior and inferior set. The sets are defined in Table 4.5.

Table 4.5: Superior and inferior migration sets used in the three origin styles.

| Origin | Superior Set |  | Inferior Set |  |
| :---: | :---: | :---: | :---: | :---: |
| Style | Migrating Vertebra | Origin Vertebra | Migrating Vertebra | Origin Vertebra |
| Caudal | T4 | L1 | T8 | L1 |
| Apex | T4 | T8 | L1 | T8 |
| Dual | T8 | T4 | T8 | L1 |

Data was not collected for migration sets that were not undergoing induced migration. For example, when using the Apex Origin Style, the superior dataset was not measured when an inferior fusion failure was simulated. The practice of not recording and assessing the non-migratory data was developed to avoid repeatedly assessing perfect zero movement data, which would skew results.

The migration data recorded for each principal direction was collected into a format as shown in Table 4.6. Due to the large quantity of data, it cannot all be in included in the body of this report. All data analyzed for the creation of the conclusions of this thesis can be found in the appendices. The collected migration data for the accuracy assessment of the three origin styles is collected in Appendix E, Section E.3.

Table 4.6: Migration data recorded for the Superior aspect of the Caudal Origin Style undergoing a simulated failure of the superior section of the spine. Simulated failure is in the $X$ direction.

| Displacements | $\mathbf{X}(\mathbf{m m})$ | $\mathbf{Y}(\mathbf{m m})$ | $\mathbf{Z}(\mathbf{m m})$ | $\mathbf{R x}(\mathrm{deg})$ | $R y(d e g)$ | $R z(d e g)$ | MTPM <br> (mm) |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $\mathbf{0} . \mathbf{5}$ | 0.4925 | -0.0197 | 0.2016 | 0.0442 | -0.0051 | 0.0182 | 0.5697 |
|  | -0.5210 | 0.0026 | 0.0480 | 0.0155 | -0.0218 | 0.0281 | 0.5419 |
| $\mathbf{1}$ | 0.9803 | -0.0005 | 0.1183 | 0.0448 | -0.0086 | 0.0002 | 1.0094 |
|  | -1.0417 | -0.0144 | 0.2770 | 0.0625 | -0.0467 | 0.0355 | 1.1384 |
| $\mathbf{5}$ | 5.0276 | -0.0056 | 0.0426 | 0.0525 | 0.0798 | 0.0184 | 5.1832 |
|  | -4.9921 | 0.0025 | 0.0303 | 0.0121 | 0.0061 | -0.0015 | 4.9996 |
| $\mathbf{1 0}$ | 10.0019 | 0.0152 | 0.0845 | 0.0706 | 0.1133 | 0.0109 | 10.1155 |
|  | -9.9839 | -0.0081 | 0.0990 | 0.0229 | 0.0275 | 0.0059 | 10.0120 |
| $\mathbf{2 0}$ | 20.0235 | -0.0143 | 0.1165 | 0.0881 | 0.0472 | 0.0225 | 20.1579 |
|  | -20.0596 | -0.0159 | 0.1554 | 0.0506 | -0.0243 | 0.0323 | 20.0848 |

Prediction interval assessment was used to calculate the accuracy of the simulated RSA origin styles. All prediction intervals were calculated using Minitab 16. The accuracy of an RSA system is determined for a direction by taking the $1 / 2$ width of the average prediction interval for the assessed direction. A calculation of the accuracy produced by the Caudal Origin Style for the X direction is shown in Table 4.7.

Table 4.7: Accuracy in the $X$ Direction calculated for the Caudal Origin Style. Error in the $X$ direction is $\pm 0.0444 \mathrm{~mm}$.

| Failure <br> Examined | Data |  | Prediction Interval |  |  |  | Accuracy <br> Half Width (mm) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Displacement (mm) | Measured (mm) | Lower <br> Limit | Upper Limit | Width | Average Width (mm) |  |
| Superior <br> (T4) | 0.5000 | 0.4925 | 0.4348 | 0.5522 | 0.1174 | 0.1057 | 0.0528 |
|  | -0.5000 | -0.5210 | -0.5667 | -0.4493 | 0.1174 |  |  |
|  | 1.0000 | 0.9803 | 0.9356 | 1.0530 | 0.1174 |  |  |
|  | -1.0000 | -1.0417 | -1.0675 | -0.9501 | 0.1174 |  |  |
|  | 5.0000 | 5.0276 | 4.9412 | 5.0599 | 0.1187 |  |  |
|  | -5.0000 | -4.9921 | -5.0744 | -4.9557 | 0.1187 |  |  |
|  | 10.0000 | 10.0019 | 9.9472 | 10.0696 | 0.1224 |  |  |
|  | -10.0000 | -9.9839 | -10.0841 | -9.9617 | 0.1224 |  |  |
|  | 20.0000 | 20.0235 | 19.9560 | 20.0921 | 0.1362 |  |  |
|  | -20.0000 | -20.0596 | -20.1066 | -19.9705 | 0.1362 |  |  |
| Superior (T8) | 0.5000 | 0.4814 | 0.4177 | 0.5298 | 0.1121 |  |  |
|  | -0.5000 | -0.5233 | -0.5847 | -0.4726 | 0.1121 |  |  |
|  | 1.0000 | 0.9771 | 0.9189 | 1.0310 | 0.1121 |  |  |
|  | -1.0000 | -1.0577 | -1.0860 | -0.9738 | 0.1121 |  |  |
|  | 5.0000 | 5.0022 | 4.9279 | 5.0412 | 0.1133 |  |  |
|  | -5.0000 | -5.0565 | -5.0961 | -4.9829 | 0.1133 |  |  |
|  | 10.0000 | 9.9811 | 9.9382 | 10.0550 | 0.1168 |  |  |
|  | -10.0000 | -10.0048 | -10.1099 | -9.9931 | 0.1168 |  |  |
|  | 20.0000 | 20.0214 | 19.9556 | 20.0856 | 0.1300 |  |  |
|  | -20.0000 | -20.0957 | -20.1406 | -20.0106 | 0.1300 |  |  |
| Inferior (T4) | 0.5000 | 0.4884 | 0.4542 | 0.5288 | 0.0746 |  |  |
|  | -0.5000 | -0.5005 | -0.5467 | -0.4721 | 0.0746 |  |  |
|  | 1.0000 | 0.9909 | 0.9546 | 1.0292 | 0.0746 |  |  |
|  | -1.0000 | -1.0206 | -1.0472 | -0.9726 | 0.0746 |  |  |
|  | 5.0000 | 5.0040 | 4.9578 | 5.0331 | 0.0754 |  |  |
|  | -5.0000 | -5.0072 | -5.0511 | -4.9757 | 0.0754 |  |  |
|  | 10.0000 | 9.9829 | 9.9610 | 10.0387 | 0.0777 |  |  |
|  | -10.0000 | -9.9889 | -10.0567 | -9.9789 | 0.0777 |  |  |
|  | 20.0000 | 20.0094 | 19.9655 | 20.0519 | 0.0865 |  |  |
|  | -20.0000 | -20.0481 | -20.0699 | -19.9834 | 0.0865 |  |  |

Using this prediction interval method, the data for each origin style was assessed for accuracy in the three translational degrees of freedom. The remainder of these calculations can be found in Appendix E, Section E.4. The results of the accuracy calculations are displayed in Table 4.8.

Table 4.8: Translational accuracies of the three principle directions of the three origin styles compared to the Limits of Clinical Significance. Accuracies are in mm.

| Origin Style | Principle Direction |  |  |
| :---: | :---: | :---: | :---: |
| X | Y | Z |  |
| Limits of Clinical Significance | 0.3000 | 0.5000 | 0.7000 |
| Caudal Technique | 0.0528 | 0.0234 | 0.2363 |
| Apex Technique | 0.1501 | 0.0238 | 0.1145 |
| Dual Technique | 0.0677 | 0.0207 | 0.1100 |

From Table 4.8 it can be seen that all calculated RSA system translational accuracies come in under the thresholds set by the Limits of Clinical Significance. Figure
4.15 displays a comparison of the three origin styles for each translational direction.


Figure 4.15: Comparison of the translational accuracies of the three origin techniques compared to the Limits of Clinical Significance.

### 4.3.1.2 Rotational Accuracy

For the assessment of the rotational accuracy, the T8 vertebra was repeatedly rotated about the centroid of the T8 marker cluster, independently of the other vertebrae. The vertebra was rotated to various angles to garner a large enough population size to determine the accuracies of the various origin styles. Rotations were induced around all three principal axes. The rotational measurements were assessed in the identical manner to those of the translational accuracy assessments.

In the current clinical environment, variability of $5^{\circ}$ has been defined as acceptable when measuring the deformity of the spine on standard bi-planar x-rays.[20] The use of RSA is expected to be more accurate than this current diagnostic tool, providing significantly improved diagnostic information. Johnsson et al have defined the Rotational Limits of Clinical Significance as $2.0^{\circ}, 0.5^{\circ}$ and $0.9^{\circ}$ about the transverse (X), vertical $(\mathrm{Y})$, or sagittal ( Z ) spinal axes respectively.

To calculate the rotational accuracies for the three origin styles, prediction intervals were once again used. These calculations, found in Appendix E, Section E.4, resulted in the rotational accuracies presented in Table 4.9 with a graphical comparison on the three origin styles is shown in Figure 4.16.

Table 4.9: Calculated rotational accuracies of the three origin styles. All accuracies are in degrees.

| Origin Style | Principle Direction |  |  |
| :---: | :---: | :---: | :---: |
|  | X | Y | Z |
| Limits of Clinical Significance | 2.0000 | 0.5000 | 0.9000 |
| Caudal Technique | 0.0504 | 0.0725 | 0.0414 |
| Apex Technique | 0.0949 | 0.1315 | 0.1386 |
| Dual Technique | 0.0945 | 0.1371 | 0.1385 |



Figure 4.16: Comparison of the rotational accuracies of the three origin techniques.
The differences between the three origin styles for rotational accuracy assessment are negligible when compared to the Limits of Clinical Significance. Removing the overwhelming columns representing the Limits of Clinical Significance Figure 4.16 becomes Figure 4.17. Here it is still shown that the variance between the three origin styles is still minor.


Figure 4.17: Comparison of the rotational accuracies of the three origin styles without the Limits of Clinical Significance indicators.

### 4.3.1.3 Migrational Measurement Assessment

The measured movement was assessed to determine if the three origin styles were adequately registering the migrations induced in the simulated model. This was accomplished through the application of Bland-Altman (BA) plots. Due to the high number of BA plots analyzed, only a sample is provided here for assessment. All BA plots and their analysis can be found in Appendix F, Section F.2.

The following graphs, Figure 4.18, Figure 4.19, and Figure 4.20, are the BA plots created to examine the ability of the three origin styles to accurately measure the displacement induced within the simulated phantom model. The limits of agreement (ULA - Upper Limit of Agreement, LLA - Lower Limit of Agreement) are represented by the two red lines. All displacements in the three figures are in the X direction.


Figure 4.18: Bland-Altman plot showing the accuracy of the Caudal Origin Technique in the $X$ direction. Green Line: Mean, -0.01. Red Lines: Upper and Lower Limits of Agreement, 0.04 and $\mathbf{- 0 . 0 7}$ respectively. These limits contain the limits of $\mathbf{9 5 \%}$ of data. Black data points: Values falling within the limits of agreement. Red data point: Value falling outside the limit of agreement. Limits of Clinical Significance are shown as the maximum and minimum of the ordinate axis.


Figure 4.19: Bland-Altman plot showing the accuracy of the Apex Origin Technique in the $X$ direction. Green Line: Mean, $\mathbf{0 . 0 3}$. Red Lines: Upper and Lower Limits of Agreement, 0.14 and -0.09 respectively. These limits contain the limits of $\mathbf{9 5 \%}$ of data. Black data points: Values falling within the limits of agreement. Red data point: Value falling outside the limit of agreement. Limits of Clinical Significance are shown as the maximum and minimum of the ordinate axis.


Figure 4.20: Bland-Altman plot showing the accuracy of the Dual Origin Technique in the $X$ direction. Green Line: Mean, -0.02. Red Lines: Upper and Lower Limits of Agreement, 0.06 and $\mathbf{- 0 . 1 1}$ respectively. These limits contain the limits of $\mathbf{9 5 \%}$ of data. Black data points: Values falling within the limits of agreement. Red data points: Value falling outside the limit of agreement. Limits of Clinical Significance are shown as the maximum and minimum of the ordinate axis.

For a measurement to agree with the true value on a Bland-Altman plot, the limits of agreement must remain within the Limits of Clinical Significance [61]. For all BA plots presented in this thesis, the limits of the ordinate axis represent the Limits of Clinical Significance; in this sample case 0.300 mm as determined by Pape et al (2002) [1]. Figure 4.18, Figure 4.19, and Figure 4.20 all show that each of the three origin styles adequately measured the displacement induced in the simulated model. Therefore there is no significant difference between the measured and true migration values. This is also true for both the Y and Z translational migration and all rotational accuracies. These results are shown in the compressed BA plots, Figure 4.21 and Figure 4.22. These compressed plots show only the Upper and Lower Limits of Agreement (ULA and LLA respectively) for agreement comparison purposes.


Figure 4.21: Comparison of the Translational Accuracy Bland-Altman plots Limits of Agreement.


Figure 4.22: Comparison of the Rotational Accuracy Bland-Altman plots Limits of Agreement.

Figures showing the full BA plots with mean and ULA/LLA data are included in Appendix F, Section F.2.

None of the BA plots showed average errors of zero for the three origin styles. This represents a bias of these measurement techniques. The associated bias of the three origin styles are shown in Table 4.10.

Table 4.10: Measurement Bias of the three origin styles.

|  | $\mathbf{X}(\mathrm{mm})$ | $\mathbf{Y}(\mathrm{mm})$ | $\mathbf{Z}(\mathrm{mm})$ | $\mathbf{R x}(\mathrm{deg})$ | Ry (deg) | Rz (deg) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Caudal | -0.0146 | -0.0022 | 0.1289 | 0.0332 | 0.0031 | -0.0120 |
| Apex | 0.0275 | 0.0027 | -0.0095 | -0.0537 | 0.0065 | 0.0110 |
| Dual | -0.0241 | 0.0024 | 0.1024 | 0.0544 | -0.0051 | -0.0119 |

The significant portion of these biases correspond to minor errors which, when compared to their associated Limits of Clinical Significance do not pose a significant concern. As shown in Table 4.11, only two of the eighteen biases exhibit errors which are more than $10 \%$ of their Limit of Clinical Significance.

Table 4.11: Bias Error Percentage of respective Limit of Clinical Significance

|  | X (mm) | Y (mm) | Z (mm) | Rx (deg) | Ry (deg) | Rz (deg) |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Caudal | $-4.86 \%$ | $-0.43 \%$ | $18.42 \%$ | $1.66 \%$ | $0.62 \%$ | $-1.33 \%$ |
| Apex | $9.16 \%$ | $0.54 \%$ | $-1.36 \%$ | $-2.69 \%$ | $1.29 \%$ | $1.23 \%$ |
| Dual | $-8.02 \%$ | $0.49 \%$ | $14.62 \%$ | $2.72 \%$ | $-1.01 \%$ | $-1.32 \%$ |

Although these two cases exhibit large percentage bias errors, their respective limits of agreement are well within the 0.7 mm Limit of Clinical Significance for the Z translational migration. All biases recorded in this study fall well within the acceptable limits for measurement error in a full fused spine section.

### 4.3.2 Precision Assessment Results

During the assessment of system precision, each Scene was compared to the previous Scene, resulting in the generation of seven samples for each of the two global displacement types, totalling fourteen data points used for the assessment of the precision of the RSA system. Two of the Z rotation precision exams for the Caudal Origin Style caused the L1 vertebra to be located outside of the available imaging area, excluding these exams from use in the caudal precision assessment. Therefore only twelve data points are used in the caudal precision assessment.

Each model was assessed for both superior and inferior precision. The superior precision aspect is a precision assessment of the migration analysis capturing the T4 vertebra. The inferior precision aspect is the precision assessment of the migration analysis capturing the L1 vertebra. The vertebrae compared in the assessment of the separate aspects for each origin technique is expressed in Table 4.12.

Table 4.12: Migrating and origin vertebrae of the two aspects of precision for each origin style.

| Origin Style | Superior |  | Inferior |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Migrating | Origin | Migrating | Origin |
|  | Vertebra | Vertebra | Vertebra | Vertebra |
| Caudal | T4 | L1 | T8 | L1 |
| Apex | T4 | T8 | L1 | T8 |
| Dual | T8 | T4 | T8 | L1 |

The unprocessed migration data for the fourteen precision exams can be found in Appendix E, Section E.5.

### 4.3.2.1 Precision Calculation

For a set of fourteen sample points, as collected in this project, $y$ is equal to 2.14. For twelve data points, this value is increased to 2.18 . For both spine section aspect and all three origin styles, precision was calculated for the translational and rotational migrations as well as for the Maximum Total Point Motion (MTPM). The calculation results for the superior aspect is shown in Table 4.13 and displayed graphically in Figure 4.23.

Table 4.13: Precision data for the Superior Aspect.

|  | $\mathrm{X}(\mathrm{mm})$ | $\mathrm{Y}(\mathrm{mm})$ | $\mathrm{Z}(\mathrm{mm})$ | $\mathrm{Rx}(\mathrm{deg})$ | $\mathrm{Ry}(\mathrm{deg})$ | $\mathrm{Rz}(\mathrm{deg})$ | $\mathrm{MTPM}(\mathrm{mm})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Caudal | 0.2804 | 0.0950 | 0.3963 | 0.2208 | 0.1539 | 0.1539 | 0.2813 |
| Apex | 0.1979 | 0.0434 | 0.1681 | 0.1414 | 0.1770 | 0.2028 | 0.2944 |
| Dual | 0.3344 | 0.0905 | 0.2828 | 0.1414 | 0.1771 | 0.2027 | 0.3083 |



Figure 4.23: Graphical display of the precision of the superior aspect of the three origin styles.
For further assessment of the precisions of the superior aspect of the spine, variance comparisons were undertaken. The outcomes to these tests are laid out in Section 4.3.2.2.2.

The calculation results for the inferior aspect is shown in Table 4.14 and displayed graphically in Figure 4.24.

Table 4.14: Precision Outcomes for the Inferior Aspect.

|  | $\mathrm{X}(\mathrm{mm})$ | $\mathrm{Y}(\mathrm{mm})$ | $\mathrm{Z}(\mathrm{mm})$ | $\mathrm{Rx}(\mathrm{deg})$ | $\mathrm{Ry}(\mathrm{deg})$ | $\mathrm{Rz}(\mathrm{deg})$ | $\mathrm{MTPM}(\mathrm{mm})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Caudal | 0.1807 | 0.0625 | 0.2300 | 0.1622 | 0.1430 | 0.0778 | 0.1767 |
| Apex | 0.3657 | 0.0577 | 0.3043 | 0.2307 | 0.2554 | 0.1744 | 0.3177 |
| Dual | 0.1378 | 0.0762 | 0.4819 | 0.2307 | 0.2554 | 0.1744 | 0.4029 |



Figure 4.24: Graphical display of the precision of the inferior aspect for the three origin styles
Results from the comparisons of directional variances are reported in Section 4.3.2.2.2.

### 4.3.2.2 Precision Comparison

For evaluation of the precision for the different origin styles, each direction was independently compared. Precision is a measure of the variance of the measurements and as such the comparisons of the precisions were done by assessing the variance present in the datasets. The first step to this process is the determining the distribution of the datasets.

### 4.3.2.2.1 Dataset Distribution

Each of the forty-two datasets were analyzed using an Anderson-Darling test to check for a normal distribution with p-values greater than 0.050 indicating a normal distribution. Figure 4.25 shows an example of the results of a normally distributed dataset subjected to this test.


Figure 4.25: Probability Plot for the precision results of the superior aspect of the Apex Origin Style. $p>0.050$ indicates normal distribution.

Figure 4.26 shows an example of the results of a non-parametric distributed dataset subjected to the Anderson-Darling test.


Figure 4.26: Probability Plot for the precision results of the inferior aspect of the Caudal Origin Style. $\mathbf{p}<\mathbf{0 . 0 5 0}$ indicates non-parametric distribution.

Due to the large number of probability plots, they could not be displayed here in the body of this thesis with the remainder of the plots located in Appendix F, Section F.3.1. A summary of the results of distribution assessment are displayed in Table 4.15 and Table 4.16.

Table 4.15: Assessment of the normalcy of the superior precision datasets for each principal direction. $p$-value $>\mathbf{0 . 0 5 0}$ is an indicator of a normal distribution.

| Assessed Direction | Origin Style |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Caudal |  | Apex |  | Dual |  |
|  | $p$-value | Distribution | $p$-value | Distribution | $p$-value | Distribution |
| X | 0.014 | NonParametric | 0.589 | Normal | 0.932 | Normal |
| Y | 0.700 | Normal | 0.117 | Normal | 0.790 | Normal |
| Z | 0.906 | Normal | 0.486 | Normal | 0.772 | Normal |
| Rx | 0.332 | Normal | 0.596 | Normal | 0.602 | Normal |
| Ry | 0.027 | NonParametric | 0.785 | Normal | 0.778 | Normal |
| Rz | 0.483 | Normal | 0.944 | Normal | 0.944 | Normal |
| MTPM | 0.699 | Normal | 0.473 | Normal | 0.418 | Normal |

Table 4.16: Assessment of the normalcy of the inferior precicion datasets for each principal direction. $p$-value $>0.050$ is and indicator of a normal distribution.

| Assessed Direction | Origin Style |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Caudal |  | Apex |  | Dual |  |
|  | p -value | Distribution | p-value | Distribution | p-value | Distribution |
| X | <0.005 | NonParametric | 0.142 | Normal | 0.943 | Normal |
| Y | 0.367 | Normal | 0.430 | Normal | 0.014 | NonParametric |
| Z | 0.761 | Normal | 0.008 | NonParametric | 0.525 | Normal |
| Rx | 0.124 | Normal | 0.816 | Normal | 0.820 | Normal |
| Ry | 0.097 | Normal | 0.772 | Normal | 0.771 | Normal |
| Rz | 0.523 | Normal | 0.299 | Normal | 0.290 | Normal |
| MTPM | 0.278 | Normal | <0.005 | NonParametric | 0.013 | Normal |

The necessity to determine whether a dataset is normally distributed or not is that distribution determines the statistical test required to compare the variances. For a set to be compared using parametric analysis, all three datasets must have normal distribution. In this case, the Bartlett test is utilized. If any or all the datasets are non-parametric, a Levene's test is used to assess the statistical differences.

### 4.3.2.2.2 Variance Comparison

In order to statistically assess the differences between the three origin styles, an assessment of the variances of the precision data was assessed for each of the fourteen precision conditions. Figure 4.27 is an example of one of these variance tests.


Figure 4.27: Example of one of the ten variance comparisons with no statistical difference. Not all datasets were normally distributed, so the Levene's Test is used. With a p-value of greater than $\mathbf{0 . 0 5 0}$, no significant statistical difference between the three methods was indicated.

In this plot of the precision variance for X direction of the superior aspect, not all data is normally distributed so the Levene's test was used. The reported p-value of the test is 0.199 , above the 0.050 threshold showing that there are no statistical differences between the variances of all three origin styles. This is the standard outcome, occurring in ten of the fourteen conditions tested. A summary of the outcomes can be found in Table
4.17.

Table 4.17: Summary of the statistical outcome of the precision comparison tests.

| Assessed <br> Direction |  | Superior Aspect |  | Inferior Aspect |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Statistical | p-value | Statistical <br> Difference | Statistical |  |  |
| Test |  |  |  |  |  |  |$\quad$ p-value | Statistical |
| :---: |
| D | Levene's

Four of the variance test conditions showed that there was a statistical difference between the three origin styles. Two conditions were all part of the superior aspect of the precision assessment, directions Y and Z , and two were part of the inferior aspect, directions X and Ry. The plots of these four conditions are shown in Figure 4.28, Figure 4.30, Figure 4.31, and Figure 4.33.


Figure 4.28: Variance comparison showing statistical difference present in the $Y$ direction for the superior aspect of the spine precision. All datasets were shown to be normally distributed; therefore the p-value reported by the Bartlett test was used. A value of 0.022 shows a significant difference in the variance between the caudal and dual origin precision datasets.

The results shown in Figure 4.28 indicate that there is a difference between the Apex Origin Style and the other two. This difference is further explored in Figure 4.29, which examines the relationship solely between the Apex and Dual Origin Styles.


Figure 4.29: Comparison of the Superior Y Precision of the Apex and Dual Origin Styles. Since both datasets are normally distributed, the F-test is used. This test indicates that there is a statistical difference between the Apex and Dual Origin Styles for the precision in the Y direction.

This test shows that there is a statistical difference between the two origin styles with the Apex Origin Style demonstrating the least variance of the pair. There was no statistical difference between the Caudal and Dual Origin Styles.


Figure 4.30: Variance comparison showing statistical difference present in the $\mathbf{Z}$ direction for the superior aspect of the spine precision. All datasets were shown to be normally distributed; therefore the Bartlett test reported p-value was used. A value of 0.019 shows a significant difference in the variance between datasets.

Figure 4.30 shows that there is a statistical difference between the Caudal and Apex Origin Styles in the $Z$ direction of the superior aspect of the spine. However, further analysis did not demonstrate a statistical difference between the Apex and Dual Origin Styles.


Figure 4.31: Variance comparison showing statistical difference present in the $X$ direction for the superior aspect of the spine precision. All datasets were not normally distributed; therefore the Levene's test reported p-value was used. A value of 0.005 shows a significant difference in the variance between datasets.

Figure 4.31 shows that there is a statistical difference between the three origin styles. Further analysis did demonstrate a difference between the Apex and Dual Origin Styles with the Dual Origin Style demonstrating less variance then the Apex counterpart, Figure 4.32.


Figure 4.32: Comparison of the Inferior X Precision of the Apex and Dual Origin Styles. Since both datasets are normally distributed, the F-test was used. This test indicates that there was a statistical difference between the Apex and Dual Origin Styles for the precision in the Y direction.


Figure 4.33: Variance comparison showing statistical difference present in the Ry direction for the superior aspect of the spine precision. All datasets were shown to be normally distributed; therefore the Bartlett test reported p-value was used. A value of 0.004 shows a significant difference in the variance between datasets.

Figure 4.33 shows that there is a statistical difference between the Caudal Origin Style and novel origin styles. Further analysis demonstrated no difference between the Apex and Dual Origin Styles. In fact, there were no differences between the variances of the Apex and Dual Origin Styles with respect to any of their rotational precisions. All additional variance comparison graphs can be found in Appendix F, Section F.3.2.

### 4.4 Origin Style Assessment Discussion

This thesis objective set out to examine the impact of RSA origin style on the accuracy and precision associated with the assessment of success of spinal fusions performed for the treatment of Adolescent Idiopathic Scoliosis. The three origin styles examined were the established Caudal Origin Style and two new origin styles: the Apex Origin Style and the Dual Origin Style. Due to physical constraints at the Halifax Infirmary RSA suite the use of the Caudal Origin Style cannot be carried into clinical usage due to the limited imaging area, Figure 4.34 . The phantom model, even when optimally placed, barely fits within the imaging area.


Figure 4.34: X-ray images comprising the reference exam for the Caudal Origin Style. As shown the length of the image barely contains the phantom model length.

The new origin styles remove the size limitation by using two exams in conjunction to capture intervertebral migration. Both new origin styles use the same image sets, an example of which can be seen in Figure 4.35. For this phantom model the
common vertebra found in both image pairs is the T8 vertebra located at the apex of the simulated scoliotic curve.


Figure 4.35: X-ray image sets comprising the reference exams for the Apex and Dual Origin Styles. A) Image pair of the superior section of the spine containing the T4 and T8 vertebrae. B) Image pair of the inferior section of the spine containing the $\mathbf{T 8}$ and L 1 vertebrae.

The assessment of the impact of origin style was accomplished by analyzing the results of simulated RSA exams performed on a computer simulated phantom model of a right thoracic curve surgically corrected to $20^{\circ}$. Figure 4.36 shows the fully assembled computer simulation of the spine.


Figure 4.36: A posterior-anterior view of the simulated spine assembly showing the residual $20^{\circ}$ right main thoracic curve.

### 4.4.1 Origin Style Assessment

Traditionally, migration assessment has been performed using a Caudal Origin Technique where the vertebra at the inferior end of the curve is used as the migration origin. This technique was not feasible at our institution, requiring the need for alternate origin techniques. The new techniques introduced were the Apex and Dual Origin Styles. With the Apex Origin Style, the apex vertebra of the scoliotic curve was used as migration origin. In the Dual Origin Style the superior and inferior vertebrae are used as a pair of migration origins. A summary of the three origin styles can be seen in Figure 4.37.


Figure 4.37: Comparison of the three examined origin styles where the pentagons indicate the migration origin vertebrae and triangles the migrating vertebrae. A) Caudal Origin Style. B) Apex Origin Style. C) Dual Origin Style.

### 4.4.1.1 Translational Accuracy

The system accuracy for all six degrees of freedom was assessed with very promising results, shown in Table 4.8 for translational and Table 4.9 for rotational accuracies. All origin styles, in all directions, demonstrated high accuracies, measuring the induced displacements within the Limits of Clinical Significance. Although the origin styles all fell within the Limits of Clinical Significance, the more accurate the system, the higher its diagnostic value will be.

There is no significant difference between the three origin styles with respect to the measurement of true translational migration. Both the Apex and Dual Origin Styles consistently maintain high accuracies in all three cardinal directions. Neither of the two novel origin styles have any directional accuracy worse than 0.1750 mm . The Caudal Origin Style, while maintaining the required accuracy below the level of clinical significance, does not perform as well as the new styles with respect to the Z migrational accuracy. In all three origin styles the Z translational accuracy produced the highest results. This is due to the out of plane nature of the measurement. Off-planer RSA systems consistently produce lower accuracies in the out of plane direction. As this is a known limitation patient orientation can be adjusted so that the direction requiring the least accuracy is aligned so that it is out of the image plane. In the case of spinal fusion this direction is along the patient's PA axis.

Figure 4.38 shows an assessment of the total translational accuracy for the three origin styles. This data was created by a vector addition of the $\mathrm{X}, \mathrm{Y}$, and Z directional accuracies produced by the origin styles. The Apex and Dual Origin Styles both show improvement over the conventional Caudal Origin Style. The accuracy improvement is
ultimately dwarfed by the accuracy level of all origin styles compared to the total limit of clinical significance.


Figure 4.38: Vector addition of the translational accuracies for the three origin styles compared with the total vector for the translational Limits of Clinical Significance.

The improvement in translational accuracy is mostly due to the fact that the $Z$ displacement accuracy in the Caudal Origin Style is worse than displayed in the other two origin styles. This discrepancy is due to the large distance between the migration origin located at the L1 and the T4 vertebra and when measuring the displacement of the T4 vertebra. When the origin to migration vertebra distance is lessened, using the T 8 vertebra as a means to measure displacement in the superior section of the spine (as with the Apex and Dual Origin Styles), the accuracy of the measurement improves. This improvement is an example of the change in the factors that influence the misalignment error.

### 4.4.1.2 Rotational Accuracy

The use of standard bi-planar x-rays are subject to a $5^{\circ}$ variability in the assessment of vertebral rotation [20]. The assessment of the rotational accuracies of the three origin styles found over tenfold improvement over the current clinically available diagnostic information.

The Caudal Origin Style demonstrates consistently higher rotational accuracies than the Apex or Dual Origin Styles. The cause for this increased rotational accuracy is unknown but due to the extremely high rotational accuracies recorded for all three origin styles the variations between rotational accuracies are not significant. All origin styles are more than adequate at measuring rotational displacement, producing accuracies under $0.2000^{\circ}$.

Interestingly the limits of agreement for the rotational accuracies of the Apex and Dual Origin Style are the inverse of one another. For example, in the rotational X direction, the Apex Upper Limit of Agreement is $0.04^{\circ}$ while the Lower Limit of Agreement is $-0.15^{\circ}$ with a mean of $-0.05^{\circ}$. The Dual Origin Style on the other hand shows a ULA of $0.15^{\circ}$, an LLA of $-0.04^{\circ}$ and a mean of $0.05^{\circ}$. This inverse of the BA plots is due to the negative correlation in the measurements. A positive rotation measured using the Apex Origin Style is measured as a negative rotation in the using the Dual Origin style. This is due to the opposite nature of the origin-migration vertebrae for each measurement. Since the graphs are identically inverted this is a good indicator of the repeatability of the measurement. The errors recorded from both measurement directions are not different enough to change the results of the BA plots.

The differences between the accuracies of the three origin styles in their assessment of rotational migration are inconsequential compared to the associated Limits of Clinical Significance. The choice of any origin style would suitably provide rotational measurements of the vertebral rotation.

### 4.4.1.3 Precision

The results of the precision assessment show that RSA precision underperforms other RSA precisions reported in the literature [26], [30], [34], [60], [63]. The precision results can be found in Table 4.13 for the superior aspect and Table 4.14 for the inferior aspect, both of which are found in Section 4.3.2.1. This decrease in system precision is due to the relationship of the misalignment error and the large vector lengths used in the calculation of migration within the spinal fusion [27]. Other RSA studies of spinal fusions have focused on measuring migration in single level fusions or arthroplasty implant migration [1], [32], [37], [43], [46], [47], [49], [60]. In these cases the vector lengths between the migratory and origin components were a fraction of the distances examined in this thesis, producing much more precise measurement pairs.

There were four statistically significant differences found when the variations of the origin style precisions were assessed. Two of the cases just showed statistically significant differences between the Caudal Origin Style and the novel origin styles. The two remaining cases showed statistically significant differences between the Apex and Dual Origin Styles. In both cases where the Apex and Dual Origin Styles were statistically different, the origin style that used a larger marker cluster as the migration origin demonstrated a higher precision. That is, the Dual Origin Style had less variance
when assessing inferior X precision and the Apex Origin Style showed less variance when assessing the superior Y precision.

The precision measurements of the three origin techniques show that much of the precision is not statistically different between the three origin styles. The precision assessment alone was unable to determine a "best" technique for clinical application.

Of the precision results recorded during this thesis objective, eight of the forty-two had translational precisions greater than 0.3000 mm . Two of these were recorded for the X directional precision, which is larger than the acceptable level of clinical significance. This indicates that the current origin styles and marker implantation protocol create migration measurement vectors (the distance between the centroids of the reference and migratory marker clusters) that are too large to provide the necessary level of system precision. The reduction of these measurement vectors can reduce the misalignment error associated with RSA migrational measurement and improve system precision [27]. In all other applications of RSA the measurement vectors are very small, existing between adjacent vertebrae, bone fracture elements or arthroplasty implants and the surrounding bone [1], [26], [28], [34], [50], [59-61], [63]. These small distances create a higher system precision which was not demonstrated in this study.

The advantages of vector reduction are shown in the comparison of the Caudal Origin Style precision results with those of the simulated model from Thesis Objective \#1. In both the superior and inferior aspects of the spine the $80 \%$ scale simulated model of the spine used in Thesis Objective $\# 1$ demonstrated higher precision in the Y and Z directions. An improvement in the X direction was only demonstrated in the superior
aspect of the spine. The $Z$ direction showed most significant change with each precision improving by over 0.1 mm . It is expected that the creation of a simulated model that would assess the migration of adjacent vertebrae would produce precision values congruent with those published in single level fusion studies. Future work should be conducted to assess methods to reduce the length of the measurement vectors and mitigate the low system precision.

### 4.4.2 Origin Style Selection

This thesis objective was to assess the effect of the origin style on the accuracy and precision of the RSA assessment for determination of the success of spinal fusions performed during scoliosis treatment and determine which of the two novel origin styles should be used for future clinical research and diagnostic assessment. The three origin styles assessed were the Caudal Origin Style, the Apex Origin style, and the Dual Origin Style. Each of the origin styles were compared to a set of primary and secondary characteristics. These characteristics were a measure to determine their clinical applicability and ultimately select the most ideal origin style candidate to advance into further research.

Due to the physical limitations of the RSA setup, the future use of the Caudal Origin Style at this institution is not possible. It was used as a benchmark to which the other two origin styles were assessed. The primary comparison characteristics were the assessment of the accuracy and precision of the origin styles. All three of the origin styles maintained accuracies below the Limits of Clinical Significance.

The Apex and Dual Origin Styles outperformed the caudal benchmark with respect to overall translational accuracy. The Caudal Origin Style, due to its measure of the T4 vertebra in reference to the L1 origin, performed poorly in the Z-direction while the other two showed improvement over this benchmark.

In the rotational accuracy, the Apex and Dual Origin Styles were nearly identical in their outcomes, displaying identical accuracies to the nearest $0.01^{\circ}$. These results were slightly worse than the corresponding Caudal Origin Style results, but still over an order of magnitude better than what is currently available by bi-planar x-rays [20].

The assessment of the precision produced variable results. In the superior aspect of the spine, the Apex Origin Style produced translational precision that was consistently better than the other two origin styles. The inferior aspect of the spine showed no clear indicator of a "best" origin style. In both aspects, the Apex and Dual Origin Styles had identical rotational precisions. The assessment of the precision did not clearly indicate a "best" selection between the Apex and Dual Origin Styles for future clinical application. In fact, the precision may suggest the usage of a hybrid origin style where the spine is sectioned into a superior and inferior section but the caudal rigid body marker cluster in both image sets be used as the migration origin.

Along with the quantitative results, the three origin styles also underwent a more subjective assessment. Expected patient radiological dose, diagnostic imaging area, and the industrial expense of performing the RSA exam were assessed to logistically determine the best origin style to proceed toward clinical application.

All Origin styles performed similarly in their ease of use for migration analysis with the Apex and Dual Origin Styles requiring slightly more RSA technician time for assessment.

### 4.4.2.1 Patient Radiological Risk

The Apex and Dual Origin Styles provide the potential for almost doubling the available imaging area with the drawback of increased patient radiological dose. To assess the different dose characteristics of the two imaging techniques, an estimate of the effective dose given to an average patient was created.

For this assessment the full spine image was assumed to cover the length from the T4 to L1 vertebrae with the effective dose calculated for all organs anterior to this region. For the multi-image exams the patient effective dose was calculated for two regions: T1 to T 10 for the superior image area and from T 6 to L 2 for the inferior image area. These regions cover much of the central torso, containing several major organs. The organs affected by each imaging area and their associated tissue weighting factor can be found in Table 4.18. It was assumed that the x-ray energies used to produce the full spine, superior and inferior images were identical ( $X$ remains constant).

Table 4.18: Effective Dose Tissue Weighting Factors. "Remaining Tissue" indicates that this organ makes up part of the Remaining Tissue Weighting Factor. The weighting factors were originally published in IRCP report 103 (2007) and were republished in The Essential Physics of Medical Imaging ( ${ }^{\text {rd }}$ Edition) (2012) [54]

| Organ | Weighting Factor (Wt) |  |  |
| :---: | :---: | :---: | :---: |
|  | Full Spine Image Area | Superior Image Area | Inferior Image Area |
| Thyroid | Not in Image Area | 0.04 | Not in Image Area |
| Lungs | 0.12 | 0.12 | 0.12 |
| Heart | Remaining Tissue | Remaining Tissue | Remaining Tissue |
| Breasts | 0.12 | 0.12 | 0.12 |
| Esophagus | 0.04 | 0.04 | 0.04 |
| Stomach | 0.12 | 0.12 | 0.12 |
| Small Intestine | Not in Image Area | Not in Image Area | Remaining Tissue |
| Colon | 0.12 | Not in Image Area | 0.12 |
| Liver | 0.04 | 0.04 | 0.04 |
| Gall Bladder | Remaining Tissue | Not in Image Area | Remaining Tissue |
| Pancreas | Remaining Tissue | Not in Image Area | Remaining Tissue |
| Adrenal Glands | Remaining Tissue | Not in Image Area | Remaining Tissue |
| Kidneys | Remaining Tissue | Not in Image Area | Remaining Tissue |
| Lymph Nodes | Remaining Tissue | Remaining Tissue | Remaining Tissue |
| Spleen | Remaining Tissue | Remaining Tissue | Remaining Tissue |
| Muscles | Remaining Tissue | Remaining Tissue | Remaining Tissue |
| Ribs and Vertebrae | 0.01 | 0.01 | 0.01 |
| Red Bone Marrow | 0.12 | 0.12 | 0.12 |
| Skin | 0.01 | 0.01 | 0.01 |
| Remaining Tissues | 0.12 | 0.12 | 0.12 |
| Image Area Total | 0.82 | 0.74 | 0.82 |
| Origin Style Total | 1.64 |  |  |

The use of the Apex or Dual Origin Styles causes the patient to experience an effective dose of 1.9 times as much as if they were subjected to a single image pair during the Caudal Origin Style.

From the assessment of both the quantitative and qualitative characteristics, this thesis has concluded that the use of either the Apex or Dual Origin Styles are equally applicable for further research and potential diagnostic implementation.

### 4.4.3 Limitations

Several assumptions and simplifications were made to assess of the various origin styles. These alterations induced several known limitations to the scope of the thesis work. The limitations, although impacting the project scope, should not negatively impact the validity of the conclusions made.

The conclusions drawn from this thesis are only applicable for the assessment of scoliotic curves of the 1AN Lenke classification of comparable size and severity [3]. The complex nature of the three-dimensional deformity and correction of scoliosis provides a lot of inter-patient variability that could severely impact the accuracy and precision results reported in this thesis.

The length of the fusions required varies among the patient population, easily changing the distances between the marked vertebrae. With larger distances, the misalignment issue would have a greater impact on system precision [27]. A smaller fusion would bring the marked vertebrae closer together improving system precision.

This thesis only assessed a single curve structure. The compound curve deformity may require additionally marked vertebrae to adequately assess the migrations within the spinal fusion, adding to vertebral marking and migration assessment complexity.

With these variations in curve structure and spine size, marker occlusion becomes a significant issue. Even within single curve structures, small alterations of vertebral
orientation or implant positioning could greatly impact the marker occlusion problem, decreasing marker visibility. The creation of patient or curve classification specific marker placement protocols should be assessed to create RSA marker systems that are adequate at assessing intervertebral migration.

### 4.4.4 Conclusion

The results from this objective found that the use of any of the three origin styles tested was successful at accurately measuring the migration induced in the simulated spinal model. With no significant differences between the two origin styles the use of either the Apex or Dual Origin Style are equally applicable for future clinical research and potential diagnostic implantation. Steps should be taken to decrease the length of the inter-cluster measurement vectors to increase system precision.

## Chapter 5- Discussion

### 5.1 Thesis Impact

The research conducted for the basis of this thesis has the potential for a significant impact on the Radiostereometric Analysis (RSA) body of research.

### 5.1.1 RSA Research

This thesis has validated precision component of a simulation RSA environment which can be used to create x-ray images used in RS analysis. The expanded use of the simulation process could have a significant impact on RSA research for all RSA applications. The use of simulated x-ray images provides economical, ethical and a superior method of assessing RSA performance.

Simulated RSA studies can be performed without specialist personnel or equipment, requiring less time and resources to conduct than the use of physical radiographs. Radiographic imaging equipment is not tied up for research with simulated x-rays, allowing it to maintain its clinical diagnostic assessment duties. With the exception of the phantom model study, the entirety of the research performed during this project has been performed independently on a commercially available notebook computer. After the initial vertebral model construction, each RSA image pair took approximately 25 minutes to complete, during periods of peak image simulation periods. Images were rendered automatically outside of work hours, allowing for over 50 individual images to be created per day during peak periods. Along with being inexpensive, simulated RSA exams have no possibility of radiological exposure to
personnel or patients. Therefore, large in-depth studies can be conducted with zero risk to equipment, personnel, or subjects.

A simulated model provides a superior method for assessing RSA system accuracy. Displacements induced in physical phantom models have error associated with them proportional to the methods used to implement the motion. Micrometers are commonly used to induce displacement in phantom models. The highly accurate nature of RSA creates a situation where the migration inducing and measuring techniques have similar accuracies so that the use of RSA may just be recording the error associated with the induced displacement. The simulation process eliminates this source of error. The displacements induced in the simulated phantom models are "perfect" with no error associated with the measurement. When subsequently measured with RSA software, all errors recorded are inherent to the RSA process alone.

The use of simulated RSA studies also allows for the implementation of complex movements that would be impractical or impossible to simulate with traditional phantom models. Although complex movements were not used during this study, the addition of vertebral rotation to a translational migration would not create any additional complications. To perform the same action on a traditional phantom would require the addition of another micrometer as well as increased marker obstruction concern [59]. For this reason, this thesis agrees with the sentiments expressed by Madanat et al (2007) that the use of simulated RSA research makes the assessment of complex moments possible [59].

### 5.1.2 Spinal Fusion Assessment

Along with validation of the simulation process, the use of RSA in the assessment of spinal fusion success was also analyzed. This study concludes that either the Apex or the Dual Origin Styles are equally valuable for future clinical research and implementation. RSA provides a unique opportunity to acquire highly accurate migrational measurement data at the initial postoperative assessment level. Patients can undergo RSA assessment similar to the current standard radiological assessment regime, receiving a lower effective radiological dose while increasing the output of diagnostically useful migration information. This increase in highly accurate measurements will provide faster clinical response and reduce the use of CT scans on questionable pseudoarthrosis.

Results of the translational movements of the model spines indicate that the length between the marker clusters is creating a situation of poor precision. As stated by Francis (2009), as the length of measurement vectors increase the effects of the misalignment error increase [27]. During the research completed for this thesis, the use of three marked vertebrae to measure the intervertebral displacements resulted in low precision due to misalignment error. Investigation into the reduction of this effect should be conducted.

It is of this researcher's opinion that research into the use of RSA in the assessment of spinal fusion success should continue toward the point of clinical application.

### 5.1.2.1 Marker Placement

During the course of this project a marker placement protocol adapted from the previous project work conducted by Francis (2009) was used [27]. As such the placement protocol was expected to maintain the same level of marker dispersion in the vertebrae and marker visibility in the normal, reference position (the "Reference Scene"). The marker placement protocol was also expected to undergo all migrations (the "Migrating Scenes") associated with the accuracy and precision testing without significant detriment to marker visibility.

As mentioned previously, the markers were placed in the bone, mimicking the level of placement accuracy available to a surgeon during surgery. This intentional inaccuracy provided optimization opportunities with the marker placement protocol. This was done first by placing the markers, then simulating an image set and examining the marker visibility. If a marker was obscured then it was moved to a different location. In one example, marker \#6 in the T4 vertebra was moved deeper into the vertebral body, near the anterior edge of the vertebra, from its original position, close to the right screw tip. This allowed the marker to become visible to the left of the fixation rod as shown in Figure 5.1. This kind of optimization would not be available post-operatively if a marker is found to be occluded. Using pre-operative computer simulation, a similar trial-anderror approach could be undertaken on a case-by-case basis to provide surgeons locations for safe, visible positions to implant the markers.


Figure 5.1: T4 Vertebra with marker movement A) Marker \#6 occluded by fixation rod B) Marker moved anteriorly to allow for visibility.

The placement optimization resulted in very high visibility of the seven implanted markers in each vertebra. In both the T4 and T8 models, all seven markers were visible during reference conditions. The screw placement and global position of the L1 vertebrae occluded L1 marker \#7 from view. Although this occlusion was not able to be corrected, work done by Madanat et al (2005) found that the minimum number of markers required to adequately define the position of a marker cluster with high accuracy is four visible markers [60].

During all translational accuracy and precision exams, all markers visible in the reference scene remained visible. Unfortunately, during rotational accuracy and precision movements, not all markers were visible. In a few of the assessments for the rotational precision of Caudal Origin Style the number of visible markers in a rigid body fell to four, however, this is still within the acceptable threshold for rigid body positioning. In a clinical setting, in these cases, the patient would have to be repositioned for better visibility and the x-rays would have to be recaptured.

With the high visibility of the markers and the wide spread of the markers inside the vertebra, the condition numbers of the three vertebral marker clusters were well below the threshold of 100 . The condition numbers recorded from the reference image sets were: T4: 18.5, T8: 19.7, and L1: 19.8. In all but four extreme cases, the condition number of all marker models remained under 45 .

Some of the extreme movements induced in the simulated model caused the marker clusters to extend out of the range of the imaging area when using the Caudal Origin Style. A total of eight exams were afflicted, three for the accuracy assessment and five for the precision assessment. The three accuracy assessment exams affected were both the superior and inferior +20 mm Y failure, where the T 4 vertebral cluster was partially outside the imaging area, and the -20 mm X failure where one of the matched markers of the T8 vertebra was not accessible. With the +20 mm Y failure movements, only three markers of the T4 marker cluster remained matched. While this is below the four marker threshold, the good condition number of 34.4 indicated that it was acceptable to proceed with the use of these exams as part of the accuracy assessment.

The loss of markers outside the imaging area was most profound with the movements induced for the assessment of system precision. Of the five exams affected, four were used for rotational precision assessment. The translational precision exam with negative Y movement exhibited the loss of one marker of the L1 vertebra outside the imaging area. The rotational precision exams were the most affected by the limited imaging area. Rotations around both the X and Z axes caused the L 1 vertebra to be positioned partially outside the imaging area. With the X rotation, four L 1 markers remained in the image set while Z and - X rotations saw three L 1 markers still matched.

Unfortunately, only two of the markers matched in the Z rotated precision assessment were also matched in the preceding and subsequent exams, the Y and -X rotations respectively. This precludes the precision Z rotation exam from being used in the assessment of system precision.

The -Z rotation caused the L 1 vertebra to be extended so far outside the imaging area that only two matched markers remained in the image. This is not enough for a determination of the migration origin so this exam was also removed from precision assessment.

All other thresholds required for an adequate marker placement protocol were upheld.

### 5.2 Limitations

With all research, especially phantom studies, limitations on research outcomes are imposed. The following limitations limit the scope of the presented results and do not negatively impact the conclusions made. The results of this study are only applicable to main thoracic scoliotic curves corrected to $20^{\circ}$ which correspond to a 1 AN Lenke curve classification. Different deformity structures can be created using the simulation process but will result in different intervertebral distances, vertebral marking requirements, and marker occlusion. These curve variations should be assessed before clinical implantation of RSA as a method to assess spinal fusion success.

### 5.2.1 Simulation Limitations

As stated previously, the image simulation procedure is limited in its photorealism. The most significant of the realism inaccuracies is the absence of image noise and the accuracy of material contrast. The material attenuation coefficients used to create the image contrast were created as a best match scenario to a radiograph taken at the Halifax Infirmary RSA suite in 2010 of a phantom spinal fusion model. Therefore the coefficients used do not correlate precisely to actual anatomical material absorption characteristics. This approximation was found to create adequate image contrast and was deemed acceptable.

The second photorealism inaccuracy was the absence of image noise. The signal-to-noise ratio of the simulated images approached infinity. This allows the simulated images to have higher spatial resolution than a physical x-ray. Previous work tried to compensate for this by adding in a background taken from a blank section of a physical x -
ray as well as adding a gaussian noise blur [27]. These measures were implemented as a best-match scenario to physical x-rays. They were deemed as unnecessary as the physical RSA system could provide spatial resolution to distinguish two touching markers. With this resolution present in a physical RSA system, the absence of image noise in the simulated system would provide little advantage.

### 5.3 Future Work

Due to the limitations of the RSA simulation, several research avenues exist for future research. To fully validate the RSA simulation, all avenues may require exploration to advance the simulation and to bring the assessment of spinal fusion success using RSA to the level of clinical applicability.

### 5.3.1 Image Simulation Improvements

Testing should be performed to quantify the x-ray attenuation factors of the various materials encountered during an RSA exam. The current simulated attenuation factors were set to mimic the factors found in a single phantom study. These factors were sufficient enough to differentiate the various materials present in the simulated environment but are not photorealistic. Future studies conducted on the effects of tissue simulants and implant materials would allow for quantification of attenuation characteristics at various x-ray energies and durations. The quantification would create better attenuation coefficients for the simulation process and the ability to vary the simulated x -ray strength administered during the exam.

Along with the quantification of material attenuation properties signal noise could also be quantified and incorporated into the simulation process. The addition of noise should be conducted after an assessment of physical system noise has been undertaken. The noise added to the simulated environment should be correlated with that of the physical environment to ensure that it possesses not only similar amplitude but also the same characteristics in pattern and in the frequency domain. By undertaking this vital step, the noise in the simulation will generate an identical impact on the rendered image
as its real world counterpart. Therefore the image realism can be maintained while additionally allowing for the simulation of image improvement scenarios without having to progress to physical phantoms and clinical equipment.

The improvement of the simulation process would be a great advancement for the research conducted in x-ray and RSA imaging. The use of these simulations could eventually trickle back to the clinical environment allowing for technicians to assess x-ray energy setups for individual patients before subjecting the patients to any extraneous radiological dosage.

### 5.3.2 Complete Simulation Validation

This thesis completed one of three aspects for complete simulation validation. A precision validation study confirmed that the simulated environment reproduces the same level of systemic errors as the physical RSA environment. Previous work by Madanat et al (2007) and Francis (2009) concluded that the simulation produces accurate simulations of real world counterparts [27], [59].

What remains is the assessment of the system responsiveness. To complete this assay, this researcher recommends the implementation of a parallel measurement accuracy assessment. In this study a phantom model containing migrational staging could be assessed using the physical RSA environment while a simulated phantom undergoes identical intervertebral migrations. The results from the two parallel streams should then be assessed to confirm that the results from the simulated environment reflect those of the physical RSA system.

### 5.3.3 Patient Specific Anatomical Information

Using this research as a foundation, future research should focus on the creation of patient specific simulations. The use of simulated phantom models leads to the simple, efficient and cost effective means of altering the shape of examined spinal deformities. Utilizing a complete spine model and a full complement of correction implants, a wide range of corrections could be simulated and their RSA applicability examined. This would be a vehicle for the creation of patient specific marker placement protocols, selection of surgical implants, and possible assistance in surgical planning processes. The use of patient specific anatomical information would ensure that each simulation would be tailored to the individual surgical case. Utilizing this information marker placement protocols could be customized so that all implanted markers would be visible postoperatively.

Another benefit to the use of patient specific simulations is the reduction in surgical overhead. Using a simulation based pre-operative planning processes, the required implant hardware could be selected and ordered on a case-by-case basis which would eliminate the necessity for each hospital to order and maintain a full set of implant pedicle screw and fixation rod options.

To create patient specific spinal models, several methods were examined during initial project research. The easiest of these methods is the creation of three dimensional models from pre-operative CT scans. However these scans would subject patients to high doses of radiation eliminating the radiological advantage of using RSA. The use of preoperative CT scans should be avoided for the sole use of model construction, but they
remain a viable source of anatomical information for those already undergoing the scans for other clinical reasons.

The second option for the acquisition of patient anatomical information is taking measurements from traditional bi-planer x-rays. These are part of the standard presurgical work-up and could provide adequate accuracy for gross placement of the modeled vertebrae. However, the use of bi-planer x-rays would not be adequate for the precise modeling of individual vertebral structures [72], [73].

The final and most intriguing method would be the use of Magnetic Resonance Imaging (MRI) to develop the simulated models. There were several articles found in the literature discussing the creation of models of the lumbar spine, however, it was outside the scope of this project to develop a method of acquiring anatomical information of the vertebral structures of the thoracic and lumbar spine at the IWK Health Centre [74], [75]. The use of MR imaging remains intriguing due to the safety factor associate with the method. MR imaging is non-destructive and does not subject the patient to any radiological risk.

All of these methods remain as options for further research in creating precise, patient specific anatomical models of the spine for use in later simulations.

### 5.3.4 Vertebral Marking Protocols

Current work used a placement protocol where three vertebrae are marked to determine the intervertebral migration. The superior and inferior ends of the curve as well as the curve apex were marked. This was seen as the minimum number of levels which would adequately report fusion movement. Therefore, it provided a balance between acquiring spatial information and patient safety.

This study has found that the system precision currently precludes the use of RSA to evaluate spinal fusion success. Future research should focus on the mitigation of this precision effect by limiting the distance between the marked vertebrae. This will require the use of additional marked vertebrae. This researcher suggests that moving to a system where four or five vertebrae are marked would limit the inter-cluster distances so that the required system precision is achieved.

Along with the additional marking of vertebrae, a hybrid origin style should be assessed. This new origin style should combine the use of a spatially larger origin marker cluster, the segmental analysis of the Apex and Dual Origin Styles, and the standard migrational orientation of the Caudal Origin Style. This technique would be a Sectional Origin Style. Here each marked vertebrae would act as both a migrational vertebrae for the adjacent inferior marker cluster and a migration origin for the adjacent superior marker cluster. An example of this proposed Sectional Origin Style is shown in Figure 5.2.


Figure 5.2: Sectional Origin Style. Orange Pentagon: Inferior Vertebra, Red Square: Apex Vertebra, Green Triangle: Superior Vertebra, Blue Squares: Intermediate Marked Vertebrae. Arrow colour corresponds with measurement origin vertebrae. Coordinate systems of origin vertebrae shown.

In addition to the investigation of the increase of marked vertebrae, an investigation in marker redundancy should be undertaken. The current marking protocol was developed by Francis (2009) and contains 7 markers per vertebra [27]. It was not in the scope of this thesis to assess the marking protocol past the adjustment to the use of anatomical landmarks in marker placement. Valstar et al (2005) recommend the use of 69 well placed markers in a rigid body to compensate for marker occlusion and marker loosening [5]. Using the impact on CN as a guide for marker importance, the markers which are expected to create the lowest CN are the markers in the Transverse Processes, the Spinous Process and the markers down the pedicle screw holes in the vertebral body. The least important markers are those in the lamina in that they would have the least effect on marker cluster distribution and potentially the least impact on CN . This researcher does not recommend reducing the number of markers in the vertebrae below five markers.

### 5.4 Summary and Conclusion

This thesis used simulated Radiostereometric Analysis (RSA) exams for research for its use in spinal fusions and assessed the impact of the RSA origin style on the system accuracy and precision. This research was conducted on a spinal fusion conducted on a simulated ten segment $20^{\circ}$ right thoracic scoliotic curve extending from the T 4 to L 1 vertebrae. A parallel precision assessment study was undertaken to validate the systemic errors present within the simulated RSA environment as part of a continual validation of the simulated RSA exams.

Several advances were made to the simulation process to make it more realistic. The most significant of these advances was the use of material attenuation factors to create the required radio-opacity of the simulated materials. This is an upgrade from the surface attenuation method used in previous simulations. These advancements were put to the test in a parallel phantom/simulated model validation study. This study concluded that the simulated RSA environment replicates the physical system present at the Halifax Infirmary and that the simulated RSA environment has been validated for use in RSA research.

The work completed in this thesis found that all origin styles examined preformed adequately, producing measurements that were accurate within the Limits of Clinical Significance. No statistically significant data was produced in the assessment of the two introduced and novel origin styles with both measuring the induced migrations within the respective Limits of Clinical Significance. The system precision was ineffective to produce a definite ruling on the "best" origin style with all of them producing similar
precision results. These precision results currently preclude the use of RSA in the assessment of spinal fusions. Future research into alternative curve marking protocols and origin styles should improve system precision to adequate levels.

In conclusion this thesis has shown that RSA should continue to be pursued as a future method for use clinically in the assessment of spinal fusion, replacing the current use of bi-planar x-rays. Furthermore, this thesis has also created and assessed two new measurement styles, enabling RSA measurement to be used on patients whose spines are too long to fit within the diagnostic area of the current RSA equipment. Patient or curve classification specific simulations should be undertaken to develop new vertebral marking protocols, leading the way for clinical application of RSA in spinal fusion success assessment.

## Bibliography

[1] D. Pape et al., "Lumbosacral stability of consolidated anteroposterior fusion after instrumentation removal determined by roentgen stereophotogrammetric analysis and direct surgical exploration," Spine, vol. 27, no. 3, pp. 269-74, Feb. 2002.
[2] R. Johnsson, B. Strömqvist, and P. Aspenberg, "Randomized radiostereometric study comparing osteogenic protein-1 (BMP-7) and autograft bone in human noninstrumented posterolateral lumbar fusion: 2002 Volvo Award in clinical studies.," Spine, vol. 27, no. 23, pp. 2654-61, Dec. 2002.
[3] L. G. Lenke et al., "Adolescent idiopathic scoliosis: a new classification to determine extent of spinal arthrodesis.," The Journal of bone and joint surgery. American volume, vol. 83-A, no. 8, pp. 1169-81, Aug. 2001.
[4] J. M. Bland and D. G. Altman, "Statistical methods for assessing agreement between two methods of clinical measurement.," Lancet, vol. 1, no. 8476, pp. 30710, Feb. 1986.
[5] E. R. Valstar, R. Gill, L. Ryd, G. Flivik, N. Börlin, and J. Kärrholm, "Guidelines for standardization of radiostereometry (RSA) of implants.," Acta orthopaedica, vol. 76, no. 4, pp. 563-72, Aug. 2005.
[6] S. Strandring and H. Gray, Gray's Anatomy: the Anatomical Basis of Clinical Practice, 40th, Anni. Churchill Livingstone/Elsevier, 2008, p. 1551.
[7] A. P. Schnuerer, Basic Anatomy and Pathology of the Spine, Second. Medtronic Sofamor Danek, 2003, p. 168.
[8] R. L. Drake, W. Vogl, A. W. M. Mitchell, and H. Gray, Gray's Anatomy for Students, 2nd ed. Churchill Livingstone/Elsevier, 2009, p. 1103.
[9] W. A. N. Dorland, Dorland's Pocket Medical Dictionary, 28th ed. Philadelphia: Elsevier Saunders, 2009.
[10] J. A. Herring, Tachdjian's Pediatric Orthopaedics, vols 1-3, 3rd ed., vol. 288, no. 6. W.B. Saunders Company, 2001, p. 2950.
[11] W. W. Lovell, R. B. Winter, R. T. Morrissy, and S. L. Weinstein, Lovell and Winter's pediatric orthopaedics, Fifth., vol. 1. Philadelphia: Lippincott Williams \& Wilkins, 2001, p. 1600.
[12] S. L. Weinstein, The Pediatric Spine: Principles and Practice, 1st ed., vol. 1. New York: Raven Press Ltd., 1994, p. 1959.
[13] L. A. Karol, "Effectiveness of bracing in male patients with idiopathic scoliosis," Spine, vol. 26, no. 18, pp. 2001-2005, Sep. 2001.
[14] D. E. Katz, B. S. Richards, R. H. Browne, and J. A. Herring, "A comparison between the Boston brace and the Charleston bending brace in adolescent idiopathic scoliosis.," Spine, vol. 22, no. 12, pp. 1302-1312, Jun. 1997.
[15] A. S. Hilibrand and T. S. Dina, "The use of diagnostic imaging to assess spinal arthrodesis.," The Orthopedic clinics of North America, vol. 29, no. 4, p. 591, 1998.
[16] E. R. G. Santos, D. G. Goss, R. K. Morcom, and R. D. Fraser, "Radiologic assessment of interbody fusion using carbon fiber cages," Spine, vol. 28, no. 10, pp. 997-1001, May 2003.
[17] P. Lang, N. Chafetz, H. K. Genant, and J. M. Morris, "Lumbar spinal fusion. Assessment of functional stability with magnetic resonance imaging.," Spine, vol. 15, no. 6, pp. 581-588, Jun. 1990.
[18] L. K. Cannada, S. C. Scherping, J. U. Yoo, P. K. Jones, and S. E. Emery, "Pseudoarthrosis of the cervical spine: a comparison of radiographic diagnostic measures," Spine, vol. 28, no. 1, pp. 46-51, Jan. 2003.
[19] W. Frobin, P. Brinckmann, G. Leivseth, M. Biggemann, and O. Reikerås, "Precision measurement of segmental motion from flexion-extension radiographs of the lumbar spine.," Clinical biomechanics (Bristol, Avon), vol. 11, no. 8, pp. 457-465, Dec. 1996.
[20] G. C. Lam, D. L. Hill, L. H. Le, J. V. Raso, and E. H. Lou, "Vertebral rotation measurement: a summary and comparison of common radiographic and CT methods.," Scoliosis, vol. 3, p. 16, Jan. 2008.
[21] W. Huda, J. V. Atherton, D. E. Ware, and W. A. Cumming, "An approach for the estimation of effective radiation dose at CT in pediatric patients.," Radiology, vol. 203, no. 2, pp. 417-22, May 1997.
[22] A. E. Brodsky, E. S. Kovalsky, and M. A. Khalil, "Correlation of radiologic assessment of lumbar spine fusions with surgical exploration," Spine, vol. 16, no. 6S, p. S261, 1991.
[23] G. Selvik, "Roentgen stereophotogrammetric analysis.," Acta radiologica (Stockholm, Sweden : 1987), vol. 31, no. 2, pp. 113-26, Mar. 1990.
[24] G. Selvik, "Roentgen stereophotogrammetry. A method for the study of the kinematics of the skeletal system.," Acta orthopaedica Scandinavica. Supplementum, vol. 232, pp. 1-51, Jan. 1989.
[25] J. Kärrholm, "Roentgen stereophotogrammetry. Review of orthopedic applications.," Acta orthopaedica Scandinavica, vol. 60, no. 4, pp. 491-503, Aug. 1989.
[26] C. R. Bragdon et al., "Experimental assessment of precision and accuracy of radiostereometric analysis for the determination of polyethylene wear in a total hip replacement model," Journal of Orthopaedic Research, vol. 20, no. 4, pp. 688695, 2002.
[27] A. Francis, "Simulation of a Standardized Bead Placement Protocol for Radiostereometric Analysis of Thoracic Spinal Fusion," Dalhousie University, 2009.
[28] D. Wilson, "Radiostereometric Analysis of Migration and Inducible Displacement of a Novel Porous Biomaterial used in Total Knee Arthroplasty," Dalhousie University, 2007.
[29] E. Laende, "Radiostereometric analysis of migration and inducible displacement for the evaluation of total knee replacement fixation," Dalhousie University, 2006.
[30] L. Ryd, "Micromotion in knee arthroplasty," Acta Orthopaedica, vol. 57, no. s220, pp. 3-80, Jan. 1986.
[31] J. W. Fong, "Model-Based Radiostereometric Analysis of an Uncemented MobileBearing Total Ankle Arthroplasty System," Dalhousie University, 2010.
[32] L. Ryd, A. Lindstrand, R. Rosenquist, and G. Selvik, "Tibial component fixation in knee arthroplasty," Clinical orthopaedics and related research, vol. 213, p. 141, 1986.
[33] L. Ryd et al., "Roentgen stereophotogrammetric analysis as a predictor of mechanical loosening of knee prostheses.," The Journal of bone and joint surgery. British volume, vol. 77, no. 3, pp. 377-83, May 1995.
[34] I. Onsten, A. Berzins, S. Shott, and D. R. Sumner, "Accuracy and precision of radiostereometric analysis in the measurement of THR femoral component translations: human and canine in vitro models," Journal of Orthopaedic Research, vol. 19, no. 6, pp. 1162-1167, Nov. 2001.
[35] P. Axelsson, R. Johnsson, and B. Strömqvist, "Effect of lumbar orthosis on intervertebral mobility. A roentgen stereophotogrammetric analysis.," Spine, vol. 17, no. 6, pp. 678-81, Jun. 1992.
[36] R. Johnsson, B. Strömqvist, P. Axelsson, and G. Selvik, "Influence of spinal immobilization on consolidation of posterolateral lumbosacral fusion. A roentgen stereophotogrammetric and radiographic analysis.," Spine, vol. 17, no. 1, pp. 1621, Jan. 1992.
[37] P. Axelsson and B. S. Karlsson, "Intervertebral mobility in the progressive degenerative process. A radiostereometric analysis," European Spine Journal, vol. 13, no. 6, pp. 567-572, Oct. 2004.
[38] T. H. Olsson, G. Selvik, and S. Willner, "Kinematic analysis of spinal fusions.," Investigative radiology, vol. 11, no. 3, pp. 202-209, 1976.
[39] G. Gunnarsson, P. Axelsson, R. Johnsson, and B. Strömqvist, "A method to evaluate the in vivo behaviour of lumbar spine implants.," European spine journal : official publication of the European Spine Society, the European Spinal Deformity Society, and the European Section of the Cervical Spine Research Society, vol. 9, no. 3, pp. 230-234, Jun. 2000.
[40] P. Axelsson and B. S. Karlsson, "Standardized provocation of lumbar spine mobility: three methods compared by radiostereometric analysis," Spine, vol. 30, no. 7, pp. 792-7, Apr. 2005.
[41] K. Greene-Donnelly, K. Ogden, N. Ordway, M. Roskopf, and J. Calabrese, "SU-GG-I-60: Effective Dose to Patients Undergoing Radiostereometric Analysis of the Lumbar Spine," Medical Physics, vol. 35, no. 6, p. 2656, 2008.
[42] R. Johnsson, P. Axelsson, and B. Strömqvist, "Posterolateral lumbar fusion using facet joint fixation with biodegradable rods: a pilot study.," European spine journal: official publication of the European Spine Society, the European Spinal Deformity Society, and the European Section of the Cervical Spine Research Society, vol. 6, no. 2, pp. 144-148, Jan. 1997.
[43] R. Johnsson, G. Selvik, B. Strömqvist, and G. Sundén, "Mobility of the lower lumbar spine after posterolateral fusion determined by roentgen stereophotogrammetric analysis.," Spine, vol. 15, no. 5, pp. 347-50, May 1990.
[44] G. Leivseth, P. Brinckmann, W. Frobin, R. Johnsson, and B. Strömqvist, "Assessment of sagittal plane segmental motion in the lumbar spine: a comparison between distortion-compensated and stereophotogrammetric roentgen analysis," Spine, vol. 23, no. 23, p. 2648, 1998.
[45] B. Zoëga, J. Kärrholm, and B. Lind, "Mobility provocation radiostereometry in anterior cervical spine fusions.," European spine journal, vol. 12, no. 6, pp. 631-6, Dec. 2003.
[46] P. Axelsson, R. Johnsson, and B. Strömqvist, "Mechanics of the External Fixation Test in the Lumbar Spine: A Roentgen stereogrammetric analysis," Imaging, vol. 21, no. 3, pp. 330-333, 1996.
[47] R. Johnsson, P. Axelsson, G. Gunnarsson, and B. Strömqvist, "Stability of lumbar fusion with transpedicular fixation determined by roentgen stereophotogrammetric analysis.," Spine, vol. 24, no. 7, pp. 687-690, Apr. 1999.
[48] S. Lee, K. G. Harris, V. K. Goel, and C. R. Clark, "Spinal motion after cervical fusion. In vivo assessment with roentgen stereophotogrammetry.," Spine, vol. 19, no. 20, pp. 2336-42, Oct. 1994.
[49] G. Leivseth, F. Kolstad, O. P. Nygaard, B. Zoëga, W. Frobin, and P. Brinckmann, "Comparing precision of distortion-compensated and stereophotogrammetric Roentgen analysis when monitoring fusion in the cervical spine," European spine journal, vol. 15, no. 6, pp. 774-779, Jun. 2006.
[50] D. Pape, F. Adam, E. Fritsch, K. Müller, and D. Kohn, "Primary lumbosacral stability after open posterior and endoscopic anterior fusion with interbody implants: a roentgen stereophotogrammetric analysis," Spine, vol. 25, no. 19, pp. 2514-2518, Oct. 2000.
[51] G. Selvik, P. Alberius, and A. S. Aronson, "A roentgen stereophotogrammetric system. Construction, calibration and technical accuracy.," Acta radiologica: diagnosis, vol. 24, no. 4, pp. 343-52, Jan. 1983.
[52] B. L. Kaptein, E. R. Valstar, B. C. Stoel, P. M. Rozing, and J. H. C. Reiber, "A new type of model-based Roentgen stereophotogrammetric analysis for solving the occluded marker problem.," Journal of biomechanics, vol. 38, no. 11, pp. 2330-4, Nov. 2005.
[53] L. Ryd, X. Yuan, and H. Löfgren, "Methods for determining the accuracy of radiostereometric analysis (RSA)," Acta orthopaedica Scandinavica, vol. 71, no. 4, pp. 403-8, Aug. 2000.
[54] Jerrold T. Bushberg, J. A. Seibert, E. M. Leidholdt Jr., and J. M. Boone, The Essential Physics of Medical Imaging, 3rd ed. Philadelphia: Lippincott Williams \& Wilkins, 2012.
[55] C. Guy and D. Ffytche, An Introduction to the Principles of Medical Imaging. London: Imperial Collage Press, 2005, p. 374.
[56] J. T. Bushberg, J. A. Seibert, E. M. Leidholdt Jr., and J. M. Boone, The Essential Physics of Medical Imaging, 2nd ed. Lippincott Williams \& Wilkins, 2001, p. 933.
[57] Medis specials bv., "Model-based RSA 3.2 Software User Manual." p. 80, 2008.
[58] "Merriam-Webster Online Dictionary." [Online]. Available: http://www.merriamwebster.com/dictionary/accuracy. [Accessed: 04-Mar-2012].
[59] R. Madanat, N. Moritz, and H. T. Aro, "Three-dimensional computer simulation of radiostereometric analysis (RSA) in distal radius fractures.," Journal of biomechanics, vol. 40, no. 8, pp. 1855-61, Jan. 2007.
[60] R. Madanat, T. J. Mäkinen, N. Moritz, K. T. Mattila, and H. T. Aro, "Accuracy and precision of radiostereometric analysis in the measurement of three-dimensional micromotion in a fracture model of the distal radius," Journal of orthopaedic research, vol. 23, no. 2, pp. 481-488, Mar. 2005.
[61] E. K. Laende, K. J. Deluzio, A. W. Hennigar, and M. J. Dunbar, "Implementation and validation of an implant-based coordinate system for RSA migration calculation.," Journal of biomechanics, vol. 42, no. 14, pp. 2387-93, Oct. 2009.
[62] T. J. Mäkinen, J. K. Koort, K. T. Mattila, and H. T. Aro, "Precision measurements of the RSA method using a phantom model of hip prosthesis.," Journal of biomechanics, vol. 37, no. 4, pp. 487-493, Apr. 2004.
[63] M. J. Allen, S. M. Hartmann, J. M. Sacks, J. Calabrese, and P. R. Brown, "Technical feasibility and precision of radiostereometric analysis as an outcome measure in canine cemented total hip replacement," Journal of orthopaedic science, vol. 9, no. 1, pp. 66-75, Jan. 2004.
[64] P. Axelsson, R. Johnsson, and B. Strömqvist, "Adjacent segment hypermobility after lumbar spine fusion: no association with progressive degeneration of the segment 5 years after surgery," Acta orthopaedica, vol. 78, no. 6, pp. 834-839, Dec. 2007.
[65] I. Söderkvist and P.-Å. Wedin, "Determining the movements of the skeleton using well-configured markers.," Journal of biomechanics, vol. 26, no. 12, pp. 1473-7, Dec. 1993.
[66] D. P. Breglia, "Generation of a 3-D Parametric Solid Model of the Human Spine Using Anthropomorphic Parameters," Ohio University, 2006.
[67] M. M. Panjabi et al., "Thoracic human vertebrae. Quantitative three-dimensional anatomy.," Spine, vol. 16, no. 8, pp. 888-901, Aug. 1991.
[68] M. M. Panjabi et al., "Human lumbar vertebrae. Quantitative three-dimensional anatomy.," Spine, vol. 17, no. 3, pp. 299-306, Mar. 1992.
[69] Canon, "Digital Radiography: CXDI-50C User's Manual," Group. p. 36, 2008.
[70] B. L. Kaptein, E. R. Valstar, B. C. Stoel, P. M. Rozing, and J. H. C. Reiber, "Evaluation of three pose estimation algorithms for model-based roentgen stereophotogrammetric analysis.," Proceedings of the Institution of Mechanical Engineers. Part H, Journal of engineering in medicine, vol. 218, no. 4, pp. 231-8, Jan. 2004.
[71] J. S. Krouwer, "Why Bland-Altman plots should use X , not $(\mathrm{Y}+\mathrm{X}) / 2$ when X is a reference method.," Statistics in medicine, vol. 27, no. 5, pp. 778-80, Feb. 2008.
[72] R. Dumas et al., "A semi-automated method using interpolation and optimisation for the 3D reconstruction of the spine from bi-planar radiography: a precision and accuracy study," Medical \& biological engineering \& computing, vol. 46, no. 1, pp. 85-92, Jan. 2008.
[73] L. Humbert, J. A. de Guise, B. Aubert, B. Godbout, and W. Skalli, "3D reconstruction of the spine from biplanar X-rays using parametric models based on transversal and longitudinal inferences.," Medical engineering \& physics, vol. 31, no. 6, pp. 681-687, Jul. 2009.
[74] C. L. Hoad, a L. Martel, R. Kerslake, and M. Grevitt, "A 3D MRI sequence for computer assisted surgery of the lumbar spine.," Physics in medicine and biology, vol. 46, no. 8, pp. N213-20, Aug. 2001.
[75] C. L. Hoad and A. L. Martel, "Segmentation of MR images for computer-assisted surgery of the lumbar spine.," Physics in medicine and biology, vol. 47, no. 19, pp. 3503-17, Oct. 2002.

## Appendix A - CAD Drawings





## Appendix B - Thesis Coordinate Systems

Throughout this thesis there have been eight distinct coordinate systems used. These systems, along with several specialized systems, are defined in this appendix.

## B. 1 Vertebral Coordinate Systems

Each vertebral model has its own, distinct coordinate system that was used for model construction, rigid body marker placement and for model placement in the larger spinal model. The origin for each coordinate system is the center of the inferior end plate of the vertebral body. For each vertebra the three axes are orientated so that the positive X-axis is left, positive Y -axis is superior and the positive Z -axis is anterior. The three coordinate systems are shown in Figure B.1.


Figure B.1: Vertebral Coordinate Systems. A) T4 Coordinate System, B) T8 Coordinate System, C) L1 Coordinate System

## B. 2 T8 Rotational Coordinate System

To create accuracy migrations that produce only rotational migrations in MB-RSA the origin of the migration origin for the T 8 vertebral model had to be translated to the centroid of the marker cluster. The centroid of the T8 marker cluster is located at $<0.14$, 10.07, $-25.21>\mathrm{mm}$ in the T8 Vertebral Coordinate System. The orientation of the T8 Rotational Coordinate System is in line with the spinal coordinate system with: X - Left, Y - Superior, Z - Anterior of the patient. The T8 Rotational Coordinate System is shown in Figure B.2.


Figure B.2: T8 Rotational Coordinate System.

## B. 3 Spinal Coordinate System

The Spinal Coordinate System pertains to the coordinate system of the full simulated spine model. It describes the placement of the three vertebral models and is used to define the migrations associated with the accuracy assessment present in this thesis. The position of the Spinal Coordinate System origin and axis alignment is shown in Figure B.3. The axes are orientated so that the X -axis is positive to the left, the Y -axis is positive in the superior direction and the Z -axis is positive anteriorly. The origin of this coordinate system was located as the origin of the L1 Vertebral Coordinate System.


Figure B.3: Spinal Coordinate System

## B.3.1 Precision Movement Coordinate Systems

The rotations used during precision assessments required a centralized rotation origin to keep the marker clusters of the superior and inferior vertebral models within the RSA diagnostic imaging volume. Without these translated coordinate systems the spine model would move outside of the image, making migration analysis impossible.

## B.3.1.1 Phantom Model Precision Coordinate System

The phantom model precision coordinate system was defined to provide an easily identifiable reference for translations and rotations undertaken during the phantom model precision assessment. The location of the coordinate system origin was also designed to keep the phantom model centered within the RSA diagnostic imaging area during the $6^{\circ}$ precision rotations. This coordinate system has the same orientation as that of the Spinal Coordinate System with the X -axis pointing left, the Y -axis pointing superiorly and the Z axis pointing anteriorly. The location of the translated coordinate system origin was nominally defined as $<1.99,116.75,-82.63>\mathrm{mm}$ in the Spinal Coordinate System. The translated coordinate system origin is shown in Figure B.4. This coordinate system was used for the all rotational movements of the simulation validation procedure.


Figure B.4: Location of the translated origin used for the rotational precision assessment of the phantom spinal model.

## B.3.1.2 Simulated Model Precision Coordinate System

The simulated model precision coordinate system was defined to keep the spinal model centered within the RSA diagnostic imaging area during the $10^{\circ}$ rotations undertaken to assess the rotational accuracy of the three origin styles. This coordinate system has the same orientation as that of the Spinal Coordinate System with the X -axis pointing left, the Y -axis pointing superiorly and the Z -axis pointing anteriorly. The location of the translated coordinate system origin was defined as $<0.0,156.5,0.0\rangle \mathrm{mm}$ in the Spinal Coordinate System. The translated coordinate system origin is shown in Figure B.5.


Figure B.5: Location of the translated origin used for the rotational precision assessment of the simulated spinal model.

## B. 4 RSA Origin Style Coordinate Systems

The measurement of the intervertebral manipulations of the spine was conducted using three distinct coordinate systems passed on the origin style used. These coordinate systems were defined by the MB-RSA software and patient orientation. With the patient placed so that the Spinal Coordinate System native to the spine model aligns with the global RSA Coordinate System the subsequent origin style coordinate systems are also aligned with the Spinal Coordinate System. The locations of the origins to these coordinate systems are located at the centroid of their respective marker clusters.

## B.4.1 Caudal Coordinate System

The Caudal Coordinate System was used to define intervertebral migrations when using the Caudal Origin Style. This coordinate system has a single origin located at the centroid of the L1 migration origin marker cluster. The orientation of the Caudal Coordinate System aligns with that of the Spinal Coordinate System with the X -axis pointing left, the Y -axis pointing in a superior direction and the Z -axis pointing anteriorly as shown in Figure B.6. Since this coordinate system and associated origin style both use the L1 vertebra as the migration origin all recorded measurements match the migrations induced using the Spinal Coordinate System.


Figure B.6: The Caudal Coordinate System. The origin of this coordinate system is located at the centroid of the $L 1$ marker cluster.

## B.4.2 Apex Coordinate System

The Apex Coordinate System was used to define intervertebral migrations when using the Apex Origin Style. This coordinate system has a single origin located at the centroid of the T 8 migration origin marker cluster. The orientation of the Apex Coordinate System aligns with that of the Spinal Coordinate System with the X-axis pointing left, the Y -axis pointing in a superior direction and the Z -axis pointing anteriorly as shown in Figure B.7. Due to the inversion of the migratory and origin vertebra the measurement of the migration of the L 1 vertebra with respect to the T 8 vertebra will be subsequently inverted from the induced migrations of the T 8 vertebra.


Figure B.7: Apex Coordinate System. The origin of this coordinate system is located at the centroid of the T8 marker cluster.

## B.4.3 Dual Coordinate System

The Dual Coordinate System was used to define intervertebral migrations when using the Dual Origin Style. Unlike the other two origin styles, this coordinate system contains two sub-coordinate systems: the superior and inferior coordinate systems. This is due to the use of two migration origins. The origin for each sub-coordinate system is located at the centroid of the marker clusters that make up the two migration origins. The superior origin is located at the centroid of the T4 vertebra while the inferior origin is located at the centroid of the L1 vertebra. The alignments of the two coordinate systems both parallel the directions of the Spinal Coordinate System where the X -axis is left, the Y-axis is superior and the Z -axis is anterior as shown in Figure B.8. The superior coordinate system, due to the reversal of the migratory and origin vertebrae will record the migrations of the T8 vertebra opposite than what was inputted using the Spinal Coordinate System.


Figure B.8: The Superior and Inferior Coordinate Systems which make up the Dual Coordinate System.

## B. 5 RSA Coordinate System

The RSA Coordinate System is the global coordinate system defining the overall diagnostic area. The coordinate system is defined by the calibration box native to the Halifax RSA Suite and the MB-RSA software. The origin of this coordinate system is the lower left marker of the fiducial plane with the fiducial plane forming the $\mathrm{X}-\mathrm{Y}$ plane of the system. The Z axis protrudes out of the image plane, creating the RSA diagnostic space. The RSA Coordinate System is shown in both Figure B. 9 and Figure B.10. The RSA Coordinate System is used to locate the x-ray sources and rigid body markers implanted into the spine model. These locations are used to calculate intervertebral migrations.


Figure B.9: Front view of the RSA Coordinate System. The yellow grids indicate the positions of the markers in the fiducial plane while the green grids show the positions of the markers in the control plane. The green circles on the image are the projected positions of the control markers. The images are blank simulations of the calibration box with the colours inverted.


Figure B.10: Bottom view of the RSA Coordinate System. The black planes are the images with the yellow fiducial markers shown. The green planes are the locations of the control markers with the red lines showing the projection lines of the control makers running from the x-ray sources to the images. The images are blank simulations of the calibration box with the colours inverted.

# Appendix C - Simulation Process 

## C. 1 Programs Used:

SolidEdge with Synchronous Technology 2 (Siemens, Germany)<br>Rhinoceros - Service Release 8 (McNeel North America, USA)<br>POV-Ray 3.7 (Beta Release) (Persistence of Vision Raytracer Pty. Ltd.)

## C. 2 RSA Setup

* Note: coordinate systems shown in the following images are the coordinate systems used in the Solid Edge software, not the anatomically defined systems described in Appendix B.

SolidEdge - Construct a calibration box stand-in for the CAD environment using dimensions specified for the RSA system to be simulated. Ensure that the calibration box is oriented so that the bottom right corner is located at the CAD environment origin as shown in Figure C.1. The Z axis should point up and the Y should point toward the front of the calibration box. This alignment is due to the left hand coordinate system used by POV-Ray. The green area shown in Figure C. 1 is the volume that will appear on both image plates.


Figure C.1: Calibration box (orange) and imaging area (green) in the CAD environment.
POV-Ray - Construct a simulated calibration box using the marker locations and size as specified by the layout in the physical calibration box. The X coordinate of each marker must be of the must be entered as:

$$
x_{P O V}=L_{n o m}-x_{C B}
$$

where $x_{P O V}$ is the x coordinate in POV-Ray, $x_{C B}$ is the x coordinate in the calibration box and $L_{\text {nom }}$ is the nominal length of the calibration box in the x-direction. Both the Y and Z coordinates stay the same. This process allows for the matching of the CAD and RSA right hand coordinate system with the left hand system used by POV-Ray.

## C. 3 Model Construction and Placement



Build all required models in Solid Edge. For the spine simulations this consisted of 38 separate models: 3 vertebrae, 6 pedicle screws, 6 set screws, 2 fixation rods, and 21 implanted tantalum markers. Assemble all components into a single assembly. The origin of this assembly should be in a desirable location for later placement in the RSA environment (planes shown in Figure C.2).

Figure C.2: Image of the fully assembled spine model.

## C. 4 Placement in the RSA Environment

In the CAD RSA environment, place three orthogonal reference planes in the desired location of the model origin [Figure C.3].


Figure C.3: Planes used to locate model to be imaged.

Import simulated model and mate model origin planes with placement planes, example shown in Figure C.4.


Figure C.4: Simulated model located within RSA environment.

## C. 5 File Conversion

Before saving the Solid Edge assembly file, delete all parts you do not wish to render. This is generally the calibration box and imaging area. Save the assembly file as a STEP Document (.stp or .step file extension). Open the .stp file in Rhinoceros SR8 and save the file as a .pov file in a separate empty folder. Use a single letter as a filename. Throughout this project "A.pov" was used. When asked, select the "Create separate .INC file for each object" option. A separate file will be created for each component of the simulated model (each Solid Edge part). When prompted, slide the indicator to the "more polygons" setting so that the largest number of polygons will be used to create the components.

## C. 6 POV-Ray Processing

Open the .pov file in POV-Ray and replace the following:

```
// POV-Ray file generated from Rhinoceros.
camera {
    perspective
    location <784.987, 593.639, -199.165>
    right <1.15471, 1.19804e-17, 0.666652>
    up <-0.249996, 0.866024, 0.433018>
    direction <-0.433002, -0.500003, 0.750004>
    angle 35.9886
    /*
    // to get an image that's the same as the viewport in Rhino,
    // uncomment this section and render with command line options (alt+c):
    // +w348 +h327
    right <603.198, 6.25835e-15, 348.246>
    up <-163.642, 566.88, 283.444>
    direction <-0.433002, -0.500003, 0.750004>
    */
    look_at <424.516, 177.392, 425.206>
}
background { color rgb <0.627451, 0.627451, 0.627451> }
global_settings { ambient_light color rgb <0, 0, 0> }
// default light
light_source { <300513, 346699, -519358> color rgb <1,1,1> }
```

With:

```
#version 3.6;
global_settings {max_trace_level 256}
#include "colors.inc"
#include "RSAMaterials2.inc"
//Calibration Box
#include "CalBox.inc"
//Camera Locatoins
    background {color Black}
    camera {
        perspective
// location < 100, 175,633> // Right Image
// look_at <100, 175, -20> // Right Image
        location < <745, 175,633> // Left Image
        look_at <745, 175, -20> // Left Image
        right <.814,0,0>
        up <0,1,0>
        angle 30
}
```

```
// X-Ray Tubes
```

```
light_source {
```

light_source {
// <1024, 175, 1580> // Right Image
// <1024, 175, 1580> // Right Image
<-179, 175, 1580> // Left Image
<-179, 175, 1580> // Left Image
color <1,1,1>
color <1,1,1>
// area_light <2.6, 0, -1.5>, <0, 3, 0>, 5,5 // Right Image
// area_light <2.6, 0, -1.5>, <0, 3, 0>, 5,5 // Right Image
area_light <-2.6, 0, -1.5>, <0, 3, 0>, 5,5 // Left Image
area_light <-2.6, 0, -1.5>, <0, 3, 0>, 5,5 // Left Image
adaptive 1
adaptive 1
}
}
// X-Ray Plates
// X-Ray Plates
//Left Image Plate
//Left Image Plate
box {
box {
<-75,-41,-20>
<-75,-41,-20>
<275,391,-21>
<275,391,-21>
pigment {color < 1,1,1>}
pigment {color < 1,1,1>}
}
}
//Right Image Plate
//Right Image Plate
box{
box{
<570,-41,-20>
<570,-41,-20>
<920,391,-21>
<920,391,-21>
pigment {color < 1,1,1>}
pigment {color < 1,1,1>}
}

```
    }
```

This code recreates the RSA environment with the x-ray foci located 1.6 m above the detectors at an angle of $30^{\circ}$.

Each object code needs to be converted from:

```
// (#2911) Right Rod (Object1)
#declare Object1Material = material {
texture {
    pigment { color rgbf <1, 1, 1, 0> }
    finish { ambient 1 diffuse 1 }
    }
}
#declare Object1 = object {
    #include "A.inc"
}
object { Object1 material { Object1Material }}
```

To:
// (\#3169) Right Rod (Object1)
\#declare Object1 = object \{ \#include "A1.inc"
\}
object \{ Object1 material \{ CoCr \}no_image \}

When converting the object code to the required format, the object materials are specified. The materials and their call functions are:

| Material | Call Function |
| :---: | :---: |
| Bone | Bone |
| Cobalt-Chrome | CoCr |
| Titanium | Ti |
| Tantalum | Tant |

To produce a left and right image the file will have to be rendered twice. Once with the "//Right Image" tagged lines activated and once with the "//Left Image" tagged lines.

## C. 7 RS Assessment

Process the image pair as with any other RSA exam making sure to check the "Black on White" box when detecting markers on the calibration tab.

## Appendix D - Programming Code

## D. 1 POV-Ray Code

The POV-Ray code shown here is for the left image of the image pair. For the right image the lines tagged "//Right Image" need to be activated while the "//Left Image" tagged lines, deactivated. The calibration box coding contains proprietary information on marker placement and is not included in this thesis.

## D.1.1 RSA Image Code

```
#version 3.6;
global_settings {max_trace_level 256}
#include "colors.inc"
#include "RSAMaterials2.inc"
//Calibration Box
#include "CalBox.inc"
//Camera Locatoins
    background {color Black}
    camera {
        perspective
// location < 100, 175,633> // Right Image
// look_at <100, 175, -20> // Right Image
        location <745, 175,633> // Left Image
        look_at <745, 175, -20> // Left Image
        right <.814,0,0>
        up <0,1,0>
        angle 30
    }
// X-Ray Tubes
light_source {
// <1024, 175, 1580> // Right Image
    <-179, 175, 1580> // Left Image
    color <1,1,1>
// area_light <2.6,0, -1.5>, <0, 3, 0>,5,5 // Right Image
    area_light <-2.6, 0, -1.5>, <0, 3, 0>, 5,5 // Left Image
        adaptive 1
    }
```

```
// X-Ray Plates
//Left Image Plate
box {
    <-75,-41,-20>
    <275,391,-21>
    pigment {color < 1,1,1>}
    }
//Right Image Plate
box {
    <570,-41,-20>
    <920,391,-21>
    pigment {color < 1,1,1>}
    }
//Phantom Model
// (#3169) Right Rod (Object1)
#declare Object1 = object {
    #include "A1.inc"
}
object { Object1 material { CoCr }no_image}
// (#3172) Left Rod (Object2)
#declare Object2 = object {
    #include "A2.inc"
}
object { Object2 material { CoCr }no_image}
// (#3160) T4 Vertebrae (Object3)
#declare Object3 = object {
    #include "A3.inc"
}
object { Object3 material { Bone }no_image}
// (#3250) 5.00x30 Monoaxial Screw (Object4)
#declare Object4 = object {
    #include "A4.inc"
}
object { Object4 material { Ti }no_image}
// (#3253) 5.00x30-Monoaxial-Screw-SET (Object5)
#declare Object5 = object {
    #include "A5.inc"
}
object { Object5 material { Ti }no_image}
```

```
// (#3250) 5.00x30 Monoaxial Screw (Object6)
#declare Object6 = object {
    #include "A6.inc"
}
object { Object6 material { Ti }no_image}
// (#3253) 5.00x30-Monoaxial-Screw-SET (Object7)
#declare Object7 = object {
    #include "A7.inc"
}
object { Object7 material { Ti }no_image}
// (#3247) Tantalum Bead (Object8)
#declare Object8 = object {
    #include "A8.inc"
}
object { Object8 material { Tant }no_image}
// (#3247) Tantalum Bead (Object9)
#declare Object9 = object {
    #include "A9.inc"
}
object { Object9 material { Tant }no_image}
// (#3247) Tantalum Bead (Object10)
#declare Object10 = object {
    #include "A10.inc"
}
object { Object10 material { Tant }no_image}
// (#3247) Tantalum Bead (Object11)
#declare Object11 = object {
    #include "A11.inc"
}
object { Object11 material { Tant }no_image}
// (#3247) Tantalum Bead (Object12)
#declare Object12 = object {
    #include "A12.inc"
}
object { Object12 material { Tant }no_image}
// (#3247) Tantalum Bead (Object13)
#declare Object13 = object {
    #include "A13.inc"
}
object { Object13 material { Tant }no_image}
```

```
// (#3247) Tantalum Bead (Object14)
#declare Object14 = object {
    #include "A14.inc"
}
object { Object14 material { Tant }no_image}
// (#3265) T8 Vertebrae (Object15)
#declare Object15 = object {
    #include "A15.inc"
}
object { Object15 material { Bone }no_image}
// (#3241) 5.00x35 Monoaxial Screw (Object16)
#declare Object16 = object {
    #include "A16.inc"
}
object { Object16 material { Ti }no_image}
// (#3244) 5.00x35-Monoaxial-Screw-SET (Object17)
#declare Object17 = object {
    #include "A17.inc"
}
object { Object17 material { Ti }no_image}
// (#3241) 5.00x35 Monoaxial Screw (Object18)
#declare Object18 = object {
    #include "A18.inc"
}
object { Object18 material { Ti }no_image}
// (#3244) 5.00x35-Monoaxial-Screw-SET (Object19)
#declare Object19 = object {
    #include "A19.inc"
}
object { Object19 material { Ti }no_image}
// (#3247) Tantalum Bead (Object20)
#declare Object20 = object {
    #include "A20.inc"
}
object { Object20 material { Tant }no_image}
```

```
// (#3247) Tantalum Bead (Object21)
#declare Object21 = object {
    #include "A21.inc"
}
object { Object21 material { Tant }no_image}
// (#3247) Tantalum Bead (Object22)
#declare Object22 = object {
    #include "A22.inc"
}
object { Object22 material { Tant }no_image}
// (#3247) Tantalum Bead (Object23)
#declare Object23 = object {
    #include "A23.inc"
}
object { Object23 material { Tant }no_image}
// (#3247) Tantalum Bead (Object24)
#declare Object24 = object {
    #include "A24.inc"
}
object { Object24 material { Tant }no_image}
// (#3247) Tantalum Bead (Object25)
#declare Object25 = object {
    #include "A25.inc"
}
object { Object25 material { Tant }no_image}
// (#3247) Tantalum Bead (Object26)
#declare Object26 = object {
    #include "A26.inc"
}
object { Object26 material { Tant }no_image}
// (#3268) L1 Vertebrae (Object27)
#declare Object27 = object {
    #include "A27.inc"
}
object { Object27 material { Bone }no_image}
// (#3256) 6.00x40 Monoaxial Screw (Object28)
#declare Object28 = object {
```

```
    #include "A28.inc"
}
object { Object28 material { Ti }no_image}
// (#3259) 6.00x40-Monoaxial-Screw-SET (Object29)
#declare Object29 = object {
    #include "A29.inc"
}
object { Object29 material { Ti }no_image}
// (#3256) 6.00x40 Monoaxial Screw (Object30)
#declare Object30 = object {
    #include "A30.inc"
}
object { Object30 material { Ti }no_image}
// (#3259) 6.00x40-Monoaxial-Screw-SET (Object31)
#declare Object31 = object {
    #include "A31.inc"
}
object { Object31 material { Ti }no_image}
// (#3247) Tantalum Bead (Object32)
#declare Object32 = object {
    #include "A32.inc"
}
object { Object32 material { Tant }no_image}
// (#3247) Tantalum Bead (Object33)
#declare Object33 = object {
    #include "A33.inc"
}
object { Object33 material { Tant }no_image}
// (#3247) Tantalum Bead (Object34)
#declare Object34 = object {
    #include "A34.inc"
}
object { Object34 material { Tant }no_image}
// (#3247) Tantalum Bead (Object35)
#declare Object35 = object {
    #include "A35.inc"
}
object { Object35 material { Tant }no_image}
// (#3247) Tantalum Bead (Object36)
```

```
#declare Object36 = object {
    #include "A36.inc"
}
object { Object36 material { Tant }no_image}
// (#3247) Tantalum Bead (Object37)
#declare Object37 = object {
    #include "A37.inc"
}
object { Object37 material { Tant }no_image}
// (#3247) Tantalum Bead (Object38)
#declare Object38 = object {
    #include "A38.inc"
}
object { Object38 material { Tant }no_image}
//END
```


## D.1.2 Material Attenuation Properties

The material attenuation values shown here were developed as "best match" conditions based on real x-rays taken of a phantom model. As it was beyond the scope of this project to create real world attenuation conditions, future work is required to refine the material attenuation properties to produce photo-real image contrast.

```
// #### RSA Material Attenuation ####
#version 3.6;
//Bone
#declare Bone=material{
    texture { pigment { color rgbt < 0, 0, 0,.97>} }
    interior { fade_distance 100
            fade_power 2 }
}
// Tantalum
#declare Tant=material{
    texture { pigment { color rgbt < 0, 0, 0, 1>} }
    interior { fade_distance . 21
                fade_power 2 }
}
//Titanium
#declare Ti=material{
    texture { pigment { color rgbt < 0, 0, 0,.9>} }
    interior { fade_distance 4.2
                fade_power 2 }
}
//Cobalt Chrome
#declare CoCr=material{
    texture { pigment { color rgbt < 0, 0, 0,.75>} }
    interior { fade_distance 2.7
                fade_power 2 }
}
//END
```


## D. 2 MatLab Code

## D.2.1 RSA Calculations - Global Reference Frame

## D.2.1.1 Translational

This code uses the matrix calculations in Section \#\#\# to report the migrations of the T8 vertebra. This example utilized the inferior image pair of an inferior fusion failure of 5 mm in the X direction. At the end of the program the results are given as well as the error between this method and the MB-RSA calculated results.

```
clc
clear
%% Global Coord Sys
Xg = [1,0,0];
Yg = [0,1,0];
Zg = [0,0,1];
%% Raw Marker Data
%MB-RSA Calculated Values
MBRSA = [5.0297 -0.0009 0.0055 -0.0064 0.0536 -0.0378];
%L1 at Time 0
```



```
    421.117 78.7006 504.620
    450.592 101.353 516.513
    413.967 85.9599 519.021
    426.023 88.136 519.045
    422.252 101.941 567.842];
CentL1o = sum(L1o)./6;
%L1 at Time 1
L1i = [lllll}\begin{array}{ll}{385.616 89.727 516.525}
    421.118 78.7006 504.620
    450.592 101.353 516.513
    413.967 85.9598 519.020
    426.024 88.1359 519.044
    422.200 101.960 567.887];
CentL1i = sum(L1i)./6;
%T8 at Time 0
T80 = [379.040 257.003 509.614
    407.032 239.469 503.434
    435.009 256.787 509.662
    4 0 1 . 0 4 6 ~ 2 4 9 . 7 2 6 ~ 5 1 0 . 6 3 7 )
    412.546 249.730 510.581
    406.956 249.585 554.651
```

```
    409.744 250.621 551.856];
CentT8o = sum(T80)./7;
%T8 at Time 1
T8i = [384.024 257.016 509.592
        412.043 239.477 503.432
        440.027 256.758 509.626
        406.037 249.724 510.638
        417.548 249.732 510.577
        411.959 249.581 554.652
        414.788 250.640 551.874];
CentT8i = sum(T8i)./7;
%% Pose Matrix Calculations
%L1 at Time 0
xL1o = [L1०(3,:) -L1o(1,:)];
ztempL1o = [L1o(6,:)-L1०(1,:)];
yL1o = cross(xL1o,ztempL1o);
zL1o = cross(yL1o,xL1o);
XL1o = xL1o/norm(xL1o);
YL1o = yL1o/norm(yL1o);
ZL1o = zL1o/norm(zL1o);
PL1o = [dot(XL1o,Xg) dot(YL1O,Xg) dot(ZL1O,Xg)
    dot(XL1o,Yg) dot(YL1o,Yg) dot(ZL1O,Yg)
    dot(XL1O,Zg) dot(YL1O,Zg) dot(ZL1O,Zg)];
%L1 at Time 1
xL1i = [L1i(3,:)-L1i(1,:)];
ztempL1i = [L1i(6,:)-L1i(1,:)];
yL1i = cross(xL1i,ztempL1i);
zL1i = cross(yL1i,xL1i);
XL1i = xL1i/norm(xL1i);
YL1i = yL1i/norm(yL1i);
ZL1i = zL1i/norm(zL1i);
PL1i = [dot(XL1i,Xg) dot(YL1i,Xg) dot(ZL1i,Xg)
    dot(XL1i,Yg) dot(YL1i,Yg) dot(ZL1i,Yg)
    dot(XL1i,Zg) dot(YL1i,Zg) dot(ZL1i,Zg)];
%T8 at Time 0
xT8o = [T80(3,:)-T80(1,:)];
ztempT8o = [T8O(6,:)-T8O(1,:)];
yT8o = cross(xT80,ztempT8o);
zT8o = cross(yT8o,xT8o);
XT8o = xT8o/norm(xT8o);
YT8o = yT8o/norm(yT80);
ZT8o = zT8o/norm(zT8o);
PT80 = [dot(XT80,Xg) dot(YT80,Xg) dot(ZT80,Xg)
    dot(XT8o,Yg) dot(YT8o,Yg) dot(ZT80,Yg)
    dot(XT80,Zg) dot(YT8o,Zg) dot(ZT8o,Zg)];
%T8 at Time 1
xT8i = [T8i(3,:)-T8i(1,:)];
ztempT8i = [T8i(6,:)-T8i(1,:)];
yT8i = cross(xT8i,ztempT8i);
```

```
zT8i = cross(yT8i,xT8i);
XT8i = xT8i/norm(xT8i);
YT8i = yT8i/norm(yT8i);
ZT8i = zT8i/norm(zT8i);
PT8i = [dot(XT8i,Xg) dot(YT8i,Xg) dot(ZT8i,Xg)
    dot(XT8i,Yg) dot(YT8i,Yg) dot(ZT8i,Yg)
    dot(XT8i,Zg) dot(YT8i,Zg) dot(ZT8i,Zg)];
%% RSA Calculations
%Step 1
TL1 = PL1i*PL1O';
%Step 2
T8icor = [[TL1*[T8i(1,:)]']'
    [TL1*[T8i(2,:)]']'
    [TL1*[T8i(3,:)]']
    [TL1*[T8i(4,:)]']
    [TL1*[T8i(5,:)]']'
    [TL1*[T8i(6,:)]']
    [TL1*[T8i(7,:)]']'];
%Step 3
T8oshift = [T8o(1,:)-CentT8o
                T80(2,:) -CentT8o
        T80(3,:) -CentT8o
        T80(4,:) -CentT8o
        T80(5,:) -CentT8o
        T80(6,:) -CentT8o
        T80(7,:) -CentT8o];
T8icorshift = [T8icor(1,:)-CentT8o
                T8icor(2,:)-CentT8o
                T8icor(3,:) -CentT8o
                T8icor(4,:)-CentT8o
                T8icor(5,:)-CentT8o
                T8icor(6,:)-CentT8o
                T8icor(7,:)-CentT8o];
%Step 4
%T8oshift
xT8oshift = [T8oshift(3,:)-T8oshift(1,:)];
ztempT8oshift = [T8oshift(6,:)-T8oshift(1,:)];
yT8oshift = cross(xT8oshift,ztempT8oshift);
zT8oshift = cross(yT8oshift,xT8oshift);
XT8oshift = xT8oshift/norm(xT8oshift);
YT8oshift = yT8oshift/norm(yT8oshift);
ZT8oshift = zT8oshift/norm(zT8oshift);
CentT8oshift = sum(T8oshift)./7;
PT8oshift = [dot(XT8oshift,Xg) dot(YT8oshift,Xg) dot(ZT8oshift,Xg)
    dot(XT8oshift,Yg) dot(YT8oshift,Yg) dot(ZT8oshift,Yg)
    dot(XT8oshift,Zg) dot(YT8oshift,Zg) dot(ZT8oshift,Zg)];
%T8icorshift
xT8icorshift = [T8icorshift(3,:)-T8icorshift(1,:)];
ztempT8icorshift = [T8icorshift(6,:)-T8icorshift(1,:)];
yT8icorshift = cross(xT8icorshift,ztempT8icorshift);
```

```
zT8icorshift = cross(yT8icorshift,xT8icorshift);
XT8icorshift = xT8icorshift/norm(xT8icorshift);
YT8icorshift = yT8icorshift/norm(yT8icorshift);
ZT8icorshift = zT8icorshift/norm(zT8icorshift);
CentT8icorshift = sum(T8icorshift)./7;
PT8icorshift=[dot(XT8icorshift,Xg) dot(YT8icorshift,Xg) dot(ZT8icorshift,Xg)
    dot(XT8icorshift,Yg) dot(YT8icorshift,Yg) dot(ZT8icorshift,Yg)
    dot(XT8icorshift,Zg) dot(YT8icorshift,Zg) dot(ZT8icorshift,Zg)];
TT8io = PT8icorshift*PT8oshift';
%% Results
TransMig = CentT8icorshift-CentT8oshift;
beta = asin(TT8io(3,1));
alpha = asin(((TT8io(3,2))/(cos(beta))));
gamma = asin(((TT8io(2,1))/(cos(beta))));
Rotation = [alpha*(180/pi),beta*(180/pi),gamma*(180/pi)];
Results = [TransMig,Rotation]
%Error from MB-RSA Calculated
Error = Results-MBRSA
```


## Results:

|  | $\mathrm{X}(\mathrm{mm})$ | $\mathrm{Y}(\mathrm{mm})$ | $\mathrm{Z}(\mathrm{mm})$ | $\mathrm{Rx}(\mathrm{deg})$ | $\mathrm{Ry}(\mathrm{deg})$ | $\mathrm{Rz}(\mathrm{deg})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Results | 4.9669 | 0.2280 | -0.0832 | -0.0358 | -0.0099 | -0.0428 |
| Error | -0.0628 | 0.2289 | -0.0887 | -0.0294 | -0.0635 | -0.0050 |

## D.2.1.2 Rotational

The code in this section uses the matrix calculations in Section \#\#\# to report the migrations of the T8 vertebra. This example utilized the inferior image pair assessing the results of a rotational fusion failure of $6^{\circ}$ about the X axis. At the end of the program the results are given as well as the error between this method and the MB-RSA calculated results.

```
clc
clear
%% Global Coord Sys
Xg = [1,0,0];
Yg = [0,1,0];
Zg = [0,0,1];
%% Raw Marker Data
%MB-RSA Calculated Values
MBRSA = [0.0206 -0.0208 0.0288 6.0296 0.0222 -0.0297];
%L1 at Time 0
L1o = [l385.616 89.727 516.525
    421.117 78.7006 504.620
    450.592 101.353 516.513
    413.967 85.9599 519.021
    426.023 88.136 519.045
    422.252 101.941 567.842];
CentL1o = sum(L1O)./6;
%L1 at Time 1
L1i = [385.611 89.7258 516.535
        421.113 78.6992 504.628
        450.588 101.352 516.519
        413.962 85.9585 519.03
        426.019 88.1346 519.053
        422.208 101.96 567.873];
CentL1i = sum(L1i)./6;
%T8 at Time 0
T80 = [379.040 257.003 509.614
        407.032 239.469 503.434
        435.009 256.787 509.662
        401.046 249.726 510.637
        412.546 249.730 510.581
        406.956 249.585 554.651
        409.744 250.621 551.856];
CentT8o = sum(T80)./7;
%T8 at Time 1
T8i = [378.993 258.186 510.289
```

```
    407.05 241.41 502.402
    435.022 257.927 510.343
    401.039 250.885 510.639
    412.536 250.888 510.593
    406.946 246.09 554.428
    409.781 247.393 551.688];
CentT8i = sum(T8i)./7;
%% Pose Matrix Calculations
%L1 at Time 0
xL1o = [L1O(3,:)-L1०(1,:)];
ztempL1o = [L1o(6,:)-L1o(1,:)];
yL1o = cross(xL1o,ztempL1o);
zL1o = cross(yL1o,xL10);
XL1o = xL1o/norm(xL1o);
YL1o = yL1o/norm(yL1o);
ZL1o = zL1o/norm(zL1o);
PL1o = [dot(XL1o,Xg) dot(YL1o,Xg) dot(ZL1o,Xg)
    dot(XL10,Yg) dot(YL1o,Yg) dot(ZL10,Yg)
    dot(XL1O,Zg) dot(YL1O,Zg) dot(ZL1O,Zg)];
%L1 at Time 1
xL1i = [L1i(3,:)-L1i(1,:)];
ztempL1i = [L1i(6,:)-L1i(1,:)];
yL1i = cross(xL1i,ztempL1i);
zL1i = cross(yL1i,xL1i);
XL1i = xL1i/norm(xL1i);
YL1i = yL1i/norm(yL1i);
ZL1i = zL1i/norm(zL1i);
PL1i = [dot(XL1i,Xg) dot(YL1i,Xg) dot(ZL1i,Xg)
    dot(XL1i,Yg) dot(YL1i,Yg) dot(ZL1i,Yg)
    dot(XL1i,Zg) dot(YL1i,Zg) dot(ZL1i,Zg)];
%T8 at Time 0
xT8o = [T80(3,:)-T8o(1,:)];
ztempT8o = [T8०(6,:)-T8०(1,:)];
yT8o = cross(xT80,ztempT8o);
zT8o = cross(yT8o,xT8o);
XT8o = xT8o/norm(xT8o);
YT8o = yT8o/norm(yT8o);
ZT8o = zT8o/norm(zT8o);
PT8o = [dot(XT8o,Xg) dot(YT8o,Xg) dot(ZT80,Xg)
    dot(XT80,Yg) dot(YT80,Yg) dot(ZT80,Yg)
    dot(XT8o,Zg) dot(YT8o,Zg) dot(ZT8o,Zg)];
%T8 at Time 1
xT8i = [T8i(3,:)-T8i(1,:)];
ztempT8i = [T8i(6,:)-T8i(1,:)];
yT8i = cross(xT8i,ztempT8i);
zT8i = cross(yT8i,xT8i);
XT8i = xT8i/norm(xT8i);
YT8i = yT8i/norm(yT8i);
ZT8i = zT8i/norm(zT8i);
```

```
PT8i = [dot(XT8i,Xg) dot(YT8i,Xg) dot(ZT8i,Xg)
    dot(XT8i,Yg) dot(YT8i,Yg) dot(ZT8i,Yg)
    dot(XT8i,Zg) dot(YT8i,Zg) dot(ZT8i,Zg)];
```

```
%% RSA Calculations
% Step 1
TL1 = PL1i*PL1O';
%Step 2
T8icor = [[TL1*[T8i(1,:)]']'
    [TL1*[T8i (2,:) ]']'
    [TL1*[T8i(3,:)]']'
    [TL1*[T8i(4,:)]']'
    [TL1*[T8i(5,:)]']'
    [TL1*[T8i(6,:)]']'
    [TL1*[T8i(7,:)]']'];
```

\%Step 3
T8oshift $=$ [T8o(1,:)-CentT8o
T8o (2, : ) -CentT8o
T8o (3, :) - CentT8o
T8o (4,:) -CentT8o
T8o (5,:) -CentT8o
T80 (6, :) -CentT8o
T80 (7, :) -CentT8o];
T8icorshift $=$ [T8icor $(1,:)$-CentT8o
T8icor (2,:) -CentT8o
T8icor $(3,:)$-CentT8o
T8icor (4, :) -CentT8o
T8icor (5,:) -CentT8o
T8icor (6,:)-CentT8o
T8icor (7,:) -CentT8o];
\%Step 4
\%T8oshift
xT8oshift $=[T 8 o s h i f t(3,:)-T 8 o s h i f t(1,:)] ;$
ztempT8oshift $=[T 80 s h i f t(6,:)-T 8 o s h i f t(1,:)] ;$
yT8oshift $=$ cross (xT8oshift, ztempT8oshift);
zT8oshift $\quad=\operatorname{cross}(y T 80 s h i f t, x T 8 o s h i f t) ;$
XT8oshift $=x T 8 o s h i f t / n o r m(x T 8 o s h i f t) ;$
YT8oshift $=y T 8 o s h i f t / n o r m(y T 8 o s h i f t) ;$
ZT8oshift $=$ zT8oshift/norm(zT8oshift);
CentT8oshift $=$ sum(T8oshift)./7;
PT8oshift $=$ [dot(XT8oshift, Xg) $\operatorname{dot(YT8oshift,Xg)~dot(ZT8oshift,~Xg)~}$
dot(XT8oshift, Yg) dot(YT8oshift, Yg) dot(ZT8oshift, Yg)
dot(XT8oshift,Zg) dot(YT8oshift,Zg) dot(ZT8oshift,Zg)];
\%T8icorshift
xT8icorshift $=[T 8 i c o r s h i f t(3,:)-T 8 i c o r s h i f t(1,:)] ;$
ztempT8icorshift $=[$ T8icorshift $(6,:)-T 8 i \operatorname{corshift(1,:)];~}$
yT8icorshift $\quad=\quad$ cross (xT8icorshift, ztempT8icorshift);
zT8icorshift $=$ cross (yT8icorshift,xT8icorshift);
XT8icorshift = xT8icorshift/norm(xT8icorshift);
YT8icorshift = yT8icorshift/norm(yT8icorshift);
ZT8icorshift = zT8icorshift/norm(zT8icorshift);

```
CentT8icorshift = sum(T8icorshift)./7;
PT8icorshift = [dot(XT8icorshift,Xg) dot(YT8icorshift,Xg) dot(ZT8icorshift,Xg)
                                    dot(XT8icorshift,Yg) dot(YT8icorshift,Yg) dot(ZT8icorshift,Yg)
                                    dot(XT8icorshift,Zg) dot(YT8icorshift,Zg) dot(ZT8icorshift,Zg)];
TT8io = PT8icorshift*PT8oshift';
%% Results
TransMig = CentT8icorshift-CentT8oshift;
beta = asin(TT8io(3,1));
alpha = asin(((TT8io(3,2))/(\operatorname{cos(beta))));}
gamma = asin(((TT8io(2,1))/(cos(beta))));
Rotation = [alpha*(180/pi),beta*(180/pi),gamma*(180/pi)];
Results = [TransMig,Rotation]
%Error from MB-RSA Calculated
Error = Results-MBRSA
```


## Results:

|  | $\mathrm{X}(\mathrm{mm})$ | $\mathrm{Y}(\mathrm{mm})$ | $\mathrm{Z}(\mathrm{mm})$ | $\mathrm{Rx}(\mathrm{deg})$ | $\mathrm{Ry}(\mathrm{deg})$ | $\mathrm{Rz}(\mathrm{deg})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Results | -0.0127 | 0.2246 | -0.1160 | 5.9265 | 0.0306 | -0.0398 |
| Error | -0.0333 | 0.2454 | -0.1448 | -0.1031 | 0.0084 | -0.0101 |

## D.2.2 Apex Rotation Calculation

The following code was used to calculate the rotational displacements in the apex origin style. Section 0 was adapted from a similar program written by E. Laende to utilize the marker cluster locations specific to the Apex rotational migration calculations. The LocalMigration Function was written by E. Laende and published here with permission.

```
% Apex Rotation Calculations
clc;
clear;
%Genaral Input
button = 'Yes';
%% Top
%Input
load TopRotation;
T_pop1 = [1, 0, 0, 407.355
            0, 1, 0, 119.403
            0, 0, 1, 521.471
            0, 0, 0, 1 ];
%Top Calcs
Origin0 = O0;
Mig0 = M0;
TopMigrations = [0,0,0,0,0,0,0];
for count=1:24;
    eval(['MigOrigin = O' num2str(count) ';'])
    eval(['MigMig = M' num2str(count) ';'])
    [MigrLocal_matrix, RedoZYX, localMTPM, pm, tpm, Pros_local0, Pros_local1] =
LocalMigration(Origin0,MigOrigin,Mig0,MigMig,T_pop1,button);
    TopMigrations(count,:)
    =
[MigrLocal matrix(1,1),MigrLocal matrix(1, 2) ,MigrLocal matrix(1, 3) ,RedoZYX(1,1),
RedoZYX(1, 2),RedoZYX (1, 3), localMTPM];
end
% Corrections for Missing Origin Markers (for Top only)
% 14th Exam
[MigrLocal_matrix,RedoZYX, localMTPM, pm, tpm, Pros_local0, Pros_local1] =
LocalMigration(O0(1:6,:),O14(1:6,:),Mig0,M14,T_pop1,button) ;
TopMigrations(14,:)
[MigrLocal matrix(1,1),MigrLocal matrix(1, 2) ,MigrLocal_matrix(1, 3),RedoZYX(1,1),
RedoZYX(1, 2),RedoZYX (1,3), localMTPM] ;
% 22nd Exam
[MigrLocal_matrix,RedoZYX, localMTPM, pm, tpm, Pros_local0, Pros_local1] =
LocalMigration(O0(1:6,:),O22(1:6,:),Mig0,M19,T_pop1,button) ;
```

```
TopMigrations(22,:)
[MigrLocal_matrix(1,1),MigrLocal_matrix(1,2),MigrLocal_matrix(1,3),RedoZYX(1,1),
RedoZYX (1, 2), RedoZYX (1,3),localMTPM];
% 23rd Exam
O0StarB = [00(1:2,:);00(4:7,:)];
023Star = [023(1:2,:);023(4:7,:)];
[MigrLocal matrix,RedoZYX, localMTPM, pm, tpm, Pros_local0, Pros_local1] =
LocalMigration(O0StarB,023Star,Mig0,M23,T_pop1,button);
TopMigrations(23,:)
    =
[MigrLocal_matrix(1,1),MigrLocal_matrix(1,2),MigrLocal_matrix(1,3),RedoZYX(1,1),
RedoZYX (1, 
%% Bottom
%Input
load BotRotation;
T_pop2 = [1, 0, 0, 407.339
    0, 1, 0, 250.417
    0, 0, 1, 521.491
    0, 0, 0, 1 ];
%Bottom Calcs
BotOrigin0 = BO0;
BotMig0 = BM0;
BotMigrations = [0,0,0,0,0,0,0];
for count=1:24;
    eval(['BotMigOrigin = BO' num2str(count) ';'])
    eval(['BotMigMig = BM' num2str(count) ';'])
    [MigrLocal_matrix,RedoZYX, localMTPM, pm, tpm, Pros_local0, Pros_local1] =
LocalMigration(BotOrigin0,BotMigOrigin,BotMig0,BotMigMig,T T pop2,button);
    BotMigrations(count,:)
[MigrLocal_matrix(1,1),MigrLocal_matrix(1,2),MigrLocal_matrix(1,3),RedoZYX(1,1),
RedoZYX (1, 2),RedoZYX (1,3),localMTPM];
end
% Corrections for Missing Origin Markers (for Bot only)
% 10th Exam
[MigrLocal_matrix,RedozYX, localMTPM, pm, tpm, Pros_local0, Pros_local1] =
LocalMigrātion(BOO(1:6,:),BO10(1:6,:),BotMig0,BM10,T pop}2,button)
BotMigrations(10,:)
[MigrLocal_matrix(1,1),MigrLocal_matrix(1,2),MigrLocal_matrix(1,3),RedoZYX(1,1),
RedoZYX (1, 2) ,RedoZYX (1,3),localMTPM];
% 14th Exam
[MigrLocal_matrix,RedoZYX, localMTPM, pm, tpm, Pros_local0, Pros_locall] =
LocalMigration(BO0(2:6,:),BO14(2:6,:),BotMig0,BM10,T_pop2,button);
BotMigrations(14,:)
[MigrLocal_matrix(1,1),MigrLocal_matrix(1,2),MigrLocal_matrix(1,3),RedoZYX(1,1),
RedoZYX (1, 2) ,RedoZYX (1, 3),localMTPM];
% 15, 16 Exams
for count=15:16;
    eval(['BotMigOrigin = BO' num2str(count) '(1:6,:);'])
```

```
    eval(['BotMigMig = BM' num2str(count) ';'])
    [MigrLocal matrix,RedoZYX, localMTPM, pm, tpm, Pros local0, Pros local1] =
LocalMigration(BotOrigin0(1:6,:),BotMigOrigin,BotMig0,BotMigMig,T_pop2,button);
    BotMigrations(count,:) =
[MigrLocal matrix(1,1),MigrLocal_matrix(1, 2) ,MigrLocal_matrix(1, 3), RedoZYX(1,1),
RedoZYX(1,2),RedoZYX(1,3),localMTPM];
end
% 21,22 Exams
for count=21:22;
    eval(['BotMigOrigin = BO' num2str(count) '(1:6,:);'])
    eval(['BotMigMig = BM' num2str(count) ';'])
    [MigrLocal matrix,RedoZYX, localMTPM, pm, tpm, Pros local0, Pros local1] =
LocalMigration(BotOrigin0(1:6, :) ,BotMigOrigin,BotMig0,BotMigMig,T_pop2,button);
    BotMigrations(count,:)
[MigrLocal matrix(1, 1),MigrLocal_matrix(1, 2) ,MigrLocal_matrix(1, 3) ,RedoZYX(1,1) ,
RedoZYX(1,2),RedoZYX(1,3),localMTPM];
end
% 23th Exam
BOOStar = [BOO(1:2,:); BOO(4:7,:)];
BO23Star = [BO23(1:2,:);BO23(4:7,:)];
[MigrLocal_matrix,RedoZYX, localMTPM, pm, tpm, Pros_local0, Pros_local1] =
LocalMigration(BO0Star,BO23Star, BotMig0,BM23,T pop2,button) ;
BotMigrations(23,:
=
[MigrLocal matrix(1,1),MigrLocal matrix(1,2),MigrLocal matrix(1, 3),RedoZYX(1,1),
RedoZYX (1, 人) ,RedoZYX (1,3),localMT}PM]
```


## D.2.3 LocalMigration Function

The LocalMigration Function was developed by Elise Laende and is reproduced
here with permission.

```
function [MigrLocal matrix,RedoZYX, localMTPM, pm, tpm, Pros_local0,
Pros_local1] = LocalMigration(TibMatrix0,TibMatrix1,ProsMatrix0,
ProsMatrix1,T_pop,button)
%LocalMigration.m
%Version 4 Updated 18 Jul 2007 by E Laende
%Calculates migration results in the local coordinate system.
%Revison History
    %Ver 1. 15 Jun 2005. Created.
    %Ver 2. 19 Apr 2006. Added plot option for single analysis
    %Ver 3. 15 Jul 2006. Corrected pm (now 1-0)
    %Ver 4. 18 Jul 2007. Corrected ZYX - now the axes are correct so ZYX
        %no longer necessary (ZYX is now the same as XYZ so no need to
        %change results matrix)
%Inputs:
    %TibMatrix0: n x 3 matrix of the post-op tibial bead locations in the
            %global coordinate system
        %[x1 yl z1
            %x2 y2 z2
            %...
            %xn yn zn]
    %TibMatrix1: n x 3 matrix of the follow-up exam tibial bead locations in the
                %global coordinate system
    %ProsMatrix0: n x 3 matrix of the post-op prosthesis bead locations in the
                %global coordinate system
    %ProsMatrix1: n x 3 matrix of the follow-up exam prosthesis bead locations
in the
            %global coordinate system
    %T_pop: 4 x 4 transformation matrix from global to local coordinate
                %systems:
                %T-pop=[ x
            % R Y
            llllll
    %button: 'Yes' for batch processing or 'No' single subject analysis
%Outputs:
    %MigrLocal matrix: 1x6 matrix [xtrans ytrans ztrans xrot yrot zrot].
                %Note these results are in the box coordinate system. Corrections
                %for L/R leg & incorrect orientation of ap & ml axes (for biplanar)
                %are made in CorrectForConventionsLM.m before being output to the
                %MasterResults matrix
    %RedoZYX: 1x3 matrix: [xrot yrot zrot]. Recalculates the rotations
                %using the correct order of rotations with ml rot calculated first.
                %Note these results are in the box coordinate system. Corrections
                %for L/R leg & incorrect orientation of ap & ml axes (for biplanar)
                %are made in CorrectForConventionsLM.m before being output to the
                %MasterResults matrix
    %localMTPM: maximum total point motion. Will be the same value as
                %calculated in the conventional method with the stem tip centre
                    %included as an implant marker (independent of coordinate system)
```

```
    %pm: "point motion" n x 3 matrix of migration of each implant marker in
    %3 directions:
    %[x1 x2 ...xn
    % y1 y2 ...yn
    % z1 z2 ...zn]
    %Note: these results are in the box coordinate system.
    %tmp: "total point motion" 1 x n matrix of the vector length of the
    %migration of each implant marker
    %Pros local0: 4 x n matrix of the location of each implant marker in
        %post-op exam. Used by FictiveMigration.m. Note: 4th row is a row of 1s
(place holders for matrix
        %multiplication). Note that one marker is the stem tip centre so the
        %coordinates are [0;0;0]
    %Pros local1: 4 x n matrix of the location of each implant marker in
        %the follow-up exam. Used by FictiveMigration.m. Note: 4th row is a row
of 1s (place holders for matrix
        %multiplication).
%Calls the following functions:
    %RBT rsa.m
    %cardan.m
%Called by:
    %TheGuts.m
%--------------------------------------------------------------------------------
%3 x n matrices
ProsMarkers0=ProsMatrix0';
ProsMarkers1=ProsMatrix1';
%matrices now in form x1 x2 ...xn
% y1 y2 ...yn
% z1 z2 ...zn
%inlcudes stem tip centre as a pros marker
%transformation between reference and follow up exams (aligning exams based
%on tibia beads)
direct_disp_1to0=RBT rsa(TibMatrix0', TibMatrix1');
TibMarkers0=TibMatri\overline{x}0';
TibMarkers1=TibMatrix1';
ntib=size(TibMarkers1,2);
TibMarkers1_corrected_sqr = direct_disp_1to0*[TibMarkers1;ones(1,ntib)];
TibMarkers1_corrected=TibMarkers1_corrected_sqr(1:3,:);
npros=size(ProsMarkers0,2); %number of prosthesis markers
%Apply the global transformation to the prosthesis markers at time 1 to
%correct for positioning within calibration box (i.e. align with time 0)
ProsMarkers1 corrected sqr = direct disp 1to0*[ProsMarkers1;ones(1, npros)];
ProsMarkers1_corrected=ProsMarkers1_corrected_sqr(1:3,:);
%transforming prosthesis beads into local coordinate system
Pros_locall=inv(T_pop)*ProsMarkers1_corrected_sqr;
Pros_local0=inv(T_pop) *[ProsMarkers0;ones(1,npros)];
%point motion of each prosthesis bead
for l=1:npros;
    pm(1:3,1)=Pros_local1(1:3,1)-Pros_local0(1:3,1);
    tpm(1,l)=norm(pm(:,l));
end
localMTPM=max(tpm); %maximum total point motion
MigrLocal=RBT_rsa(Pros_local1(1:3,:),Pros_local0(1:3,:));
%norm(MigrLocal(1:3,4));
```

```
x=MigrLocal (1,4);
y=MigrLocal (2,4);
z=MigrLocal(3,4);
[phi1, phi2, phi3] = cardan(MigrLocal,'body3_123');
angle x = phil*180/pi;
angle_y = phi2*180/pi;
angle_z = phi3*180/pi;
MigrLocal_matrix=[x y z angle_x angle_y angle_z];
%Axes correct (x & z no longer reversed) so ZYX calculation of rotations
%not necessary - now the correct order of rotations is the same as the
%original calculations. Left in so results matrix doesn't need to be
%adjusted.
[check1 check2 check3]= cardan(MigrLocal,'body3_123');
check_x = check1*180/pi;
check_y = check2*180/pi;
check_z = check3*180/pi;
RedoZYX=[check_x check_y check_z];
%
% %Checking for fictive markers:
% NoCentre=[Pros_local0(1:3,1)';Pros_local0(1:3,3)';Pros_local0(1:3,4)']
% PEcentroid=mean(NoCentre) % [x y z]
%Plot to check calculations
% if strcmp(button,'Yes')==1;
% %do not plot
if strcmp(button,'No')==1;
    figure,
    plot3(TibMarkers0(1,:) ,TibMarkers0(2,:),TibMarkers0(3,:),'.r');
    hold on,plot3(TibMarkers1(1,:),TibMarkers1(2,:),TibMarkers1(3,:),'.b');
    hold
on,plot3(TibMarkers1 corrected(1,:),TibMarkers1 corrected(2,:),TibMarkers1 corre
cted(3,:),'ob');
    hold on, plot3(ProsMarkers0(1,:),ProsMarkers0(2,:),ProsMarkers0(3,:),'*C');
    hold
on,plot3(ProsMarkers1_corrected(1, :),ProsMarkers1_corrected (2, : ) , ProsMarkers1_co
rrected(3,:),'om');
    hold on, plot3(Pros_local0(1, :), Pros_local0(2,:),Pros_local0(3,:),'.c');
    hold on,plot3(Pros_local1(1,:), Pros_local1(2,:),Pros_local1(3,:),'.m');
    xlabel('x');
    ylabel('y');
    zlabel('z');
    legend('tib0','tib1','tib1 corrected','pros0','pros1 corrected','pros0
local','pros1 local');
        view(2);
end
```


## Appendix E-Tabulated Data

## E. 1 Simulation Precision Validation Data

The raw data for the precision exams collected from MB-RSA are displayed in the tables beyond. This raw data was used to calculate the directional precision using the standard deviation multiplied by the $95 \%$ confidence limit. These calculations are found within Section E.2.

## E.1.1 Phantom Model: Translation

-------- Migration Results -------------
Reference Axis: Automatic
$=================================$
Available scenes:
-------------------------------
PhantomX0M0R --- X-number: 0 --- Reference Position
PhantomX11M0R --- X-number: 11 --- +X Translation
PhantomX12M0R --- X-number: 12 --- +Y Translation
PhantomX13M0R --- X-number: 13 --- +Z Translation
PhantomX14M0R --- X-number: 14 --- -X Translation
PhantomX15M0R --- X-number: 15 --- -Y Translation
PhantomX16M0R --- X-number: 16 --- -Z Translation
PhantomX00M0R --- X-number: 00 --- Reference Position 2

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 11 | -0.0959 | 0.0047 | -0.0994 | -0.1921 | 0.1246 | 0.1316 | 4 | 7 | 0.0584 | 0.0246 | 29.8 | 17.0 | 0.2006 |
| 11 | 12 | 0.0919 | -0.0142 | 0.0010 | 0.3134 | 0.0404 | -0.0137 | 4 | 7 | 0.0478 | 0.0368 | 29.9 | 17.0 | 0.1852 |
| 12 | 13 | -0.0495 | -0.0076 | -0.0076 | -0.0389 | -0.1682 | 0.0249 | 5 | 7 | 0.0516 | 0.0358 | 29.6 | 17.1 | 0.1736 |
| 13 | 14 | -0.1073 | -0.0069 | 0.0233 | -0.0371 | -0.1174 | 0.0025 | 5 | 7 | 0.0437 | 0.0306 | 29.6 | 17.0 | 0.1819 |
| 14 | 15 | 0.2001 | 0.0039 | 0.0940 | -0.2776 | 0.2825 | -0.1079 | 5 | 7 | 0.1116 | 0.0472 | 29.5 | 17.1 | 0.3738 |
| 15 | 16 | 0.0013 | 0.0078 | -0.1109 | 0.2959 | -0.1338 | 0.0222 | 5 | 7 | 0.0797 | 0.0407 | 29.5 | 16.9 | 0.1822 |
| 16 | 00 | -0.1103 | 0.0059 | -0.0207 | -0.0881 | 0.3406 | 0.0932 | 5 | 7 | 0.0718 | 0.0269 | 29.7 | 17.0 | 0.1970 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 11 | -0.0695 | -0.0016 | -0.0228 | -0.0753 | -0.1150 | 0.1038 | 5 | 7 | 0.0342 | 0.0246 | 27.0 | 17.0 | 0.1520 |
| 11 | 12 | 0.0464 | 0.0119 | -0.0657 | -0.0821 | 0.2288 | -0.0056 | 5 | 7 | 0.0575 | 0.0368 | 27.3 | 17.0 | 0.1725 |
| 12 | 13 | -0.0430 | -0.0473 | -0.0229 | -0.2250 | -0.1479 | 0.0923 | 5 | 7 | 0.0541 | 0.0358 | 27.0 | 17.1 | 0.2254 |
| 13 | 14 | -0.0489 | 0.0145 | 0.0097 | 0.1422 | 0.1446 | 0.0334 | 5 | 7 | 0.0352 | 0.0306 | 26.9 | 17.0 | 0.1160 |
| 14 | 15 | 0.1131 | 0.0259 | 0.1476 | 0.2422 | -0.1413 | -0.1126 | 5 | 7 | 0.0233 | 0.0472 | 26.8 | 17.1 | 0.3018 |
| 15 | 16 | -0.0076 | -0.0246 | -0.1430 | -0.1811 | -0.0316 | 0.0382 | 5 | 7 | 0.0504 | 0.0407 | 27.1 | 16.9 | 0.2149 |
| 16 | 00 | -0.0557 | 0.0306 | 0.0422 | 0.1102 | 0.0293 | -0.0472 | 5 | 7 | 0.0362 | 0.0269 | 27.2 | 17.0 | 0.1257 |

## E.1.2 Phantom Model: Rotation

-------- Migration Results ------------

Reference Axis: Automatic
===================================
Available scenes:
---------------------------
PhantomX0M0R --- X-number: 0 --- Reference Position
PhantomX21M0R --- X-number: 21 --- +X Rotation
PhantomX22M0R --- X-number: 22 -- +Y Rotation
PhantomX23M0R --- X-number: 23 --- +Z Rotation
PhantomX24M0R --- X-number: 24 --- -X Rotation
PhantomX25M0R --- X-number: 25 --- -Y Rotation
PhantomX26M0R --- X-number: 26 --- -Z Rotation
PhantomX00M0R --- X-number: 00 --- Reference Position 2

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 21 | -0.0419 | 0.0028 | -0.1568 | -0.1478 | 0.1946 | 0.1006 | 5 | 6 | 0.0491 | 0.0504 | 29.6 | 19.0 | 0.2931 |
| 21 | 22 | -0.0352 | -0.0654 | 0.2452 | 0.1499 | -0.4426 | -0.0420 | 4 | 6 | 0.0811 | 0.0370 | 54.4 | 19.2 | 0.4663 |
| 22 | 23 | 0.0005 | 0.0471 | -0.1789 | -0.1704 | 0.1772 | 0.0060 | 4 | 6 | 0.0348 | 0.0389 | 50.6 | 19.1 | 0.2746 |
| 23 | 24 | -0.0040 | -0.0475 | -0.0031 | 0.1193 | 0.1932 | 0.0321 | 5 | 7 | 0.0680 | 0.0280 | 30.1 | 16.6 | 0.1274 |
| 24 | 25 | -0.0860 | 0.0311 | 0.0661 | 0.2073 | -0.1507 | -0.0379 | 5 | 7 | 0.0505 | 0.0259 | 29.7 | 16.7 | 0.2212 |
| 25 | 26 | 0.1784 | -0.0045 | -0.0509 | -0.2825 | 0.4578 | 0.0068 | 5 | 7 | 0.1256 | 0.0452 | 31.0 | 16.5 | 0.4829 |
| 26 | 00 | -0.0869 | 0.0295 | 0.0104 | -0.0407 | -0.1112 | 0.0405 | 5 | 7 | 0.0278 | 0.0519 | 28.9 | 17.5 | 0.1375 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 21 | -0.0504 | 0.0131 | -0.1080 | -0.2124 | 0.0444 | 0.1574 | 4 | 6 | 0.0193 | 0.0504 | 42.2 | 19.0 | 0.1837 |
| 21 | 22 | -0.0061 | -0.0181 | 0.0786 | -0.0067 | 0.0873 | -0.0080 | 5 | 6 | 0.0748 | 0.0370 | 30.8 | 19.2 | 0.1618 |
| 22 | 23 | -0.0034 | -0.0116 | -0.0963 | 0.0346 | -0.0111 | -0.0624 | 5 | 6 | 0.0386 | 0.0389 | 31.8 | 19.1 | 0.1532 |
| 23 | 24 | 0.0157 | -0.0092 | 0.0138 | 0.1171 | 0.0511 | 0.0489 | 4 | 7 | 0.0261 | 0.0280 | 41.7 | 16.6 | 0.1109 |
| 24 | 25 | -0.0210 | 0.0566 | 0.0884 | 0.2524 | 0.2801 | -0.0152 | 5 | 7 | 0.0725 | 0.0259 | 26.8 | 16.7 | 0.3024 |
| 25 | 26 | 0.0630 | -0.0265 | -0.0135 | 0.0103 | -0.1812 | -0.0237 | 5 | 7 | 0.0442 | 0.0452 | 28.7 | 16.5 | 0.1545 |
| 26 | 00 | -0.0498 | 0.0223 | 0.0139 | 0.1267 | -0.1597 | -0.0596 | 5 | 7 | 0.0257 | 0.0519 | 26.6 | 17.5 | 0.1328 |

## E.1.3 Phantom Model: Combination Rotations



# E.1.4 Simulated Model: Translation 

-------- Migration Results ------------
Reference Axis: Automatic
$=================================$
Available scenes:
-------------------------------
SimulationX0M0R -- X-number: 0 --- Reference Position
SimulationX11M0R --- X-number: 11 --- +X Translation
SimulationX12M0R --- X-number: 12 --- +Y Translation
SimulationX13M0R --- X-number: 13 --- +Z Translation
SimulationX14M0R --- X-number: 14 --- -X Translation
SimulationX15M0R --- X-number: 15 --- -Y Translation
SimulationX16M0R --- X-number: 16 --- -Z Translation

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body <br> Error | Rigid Body Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 11 | -0.0491 | 0.0117 | 0.0952 | 0.0319 | -0.0367 | -0.0132 | 5 | 7 | 0.0150 | 0.0725 | 30.1 | 16.9 | 0.1632 |
| 11 | 12 | 0.1124 | 0.0100 | -0.0357 | -0.0360 | 0.1129 | -0.0397 | 5 | 7 | 0.0374 | 0.0496 | 30.3 | 16.9 | 0.1559 |
| 12 | 13 | 0.0416 | -0.0301 | -0.0456 | -0.1366 | -0.0891 | -0.0127 | 5 | 7 | 0.0252 | 0.0545 | 30.1 | 17.0 | 0.1416 |
| 13 | 14 | -0.0352 | 0.0011 | -0.0052 | 0.0740 | -0.0480 | -0.0574 | 5 | 7 | 0.0405 | 0.0735 | 30.0 | 17.0 | 0.0791 |
| 14 | 15 | -0.0426 | 0.0200 | -0.0054 | 0.1657 | 0.1601 | 0.0634 | 5 | 7 | 0.0500 | 0.0847 | 30.0 | 17.0 | 0.1311 |
| 15 | 16 | -0.1226 | -0.0042 | 0.0529 | -0.1410 | 0.0619 | 0.0542 | 5 | 7 | 0.0829 | 0.0257 | 30.2 | 16.9 | 0.2870 |
| 16 | 0 | 0.0951 | -0.0087 | -0.0562 | 0.0414 | -0.1606 | 0.0059 | 5 | 7 | 0.0991 | 0.0453 | 30.2 | 16.9 | 0.2725 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 11 | -0.0416 | 0.0089 | 0.0003 | -0.4128 | -0.1114 | 0.0448 | 5 | 7 | 0.0669 | 0.0725 | 27.3 | 16.9 | 0.1974 |
| 11 | 12 | 0.0934 | 0.0136 | -0.0076 | 0.0331 | 0.0934 | -0.0362 | 5 | 7 | 0.0249 | 0.0496 | 27.5 | 16.9 | 0.1515 |
| 12 | 13 | 0.0227 | -0.0329 | -0.0266 | 0.1283 | 0.0137 | -0.0417 | 5 | 7 | 0.0196 | 0.0545 | 27.3 | 17.0 | 0.0631 |
| 13 | 14 | -0.0156 | -0.0012 | 0.0344 | 0.4323 | 0.1770 | 0.0576 | 5 | 7 | 0.0492 | 0.0735 | 27.1 | 17.0 | 0.2425 |
| 14 | 15 | -0.0428 | 0.0118 | -0.0046 | -0.0775 | -0.1656 | 0.0320 | 5 | 7 | 0.0425 | 0.0847 | 27.1 | 17.0 | 0.1294 |
| 15 | 16 | -0.0648 | 0.0139 | -0.0003 | -0.2766 | -0.0367 | -0.0377 | 5 | 7 | 0.0515 | 0.0257 | 27.4 | 16.9 | 0.1415 |
| 16 | 0 | 0.0485 | -0.0142 | 0.0044 | 0.1747 | 0.0293 | -0.0216 | 5 | 7 | 0.0270 | 0.0453 | 27.5 | 16.9 | 0.0806 |

## E.1.5 Simulated Model: Rotation

```
-------- Migration Results ------------
```

Reference Axis: Automatic

Available scenes:
SimulationX0M0R --- X-number: 0 --- Reference Position
SimulationX21M0R --- X-number: 21 --- +X Rotation
SimulationX22M0R --- X-number: 22 --- +YRotation
SimulationX23M0R --- X-number: 23 --- +Z Rotation
SimulationX24M0R --- X-number: 24 --- -X Rotation
SimulationX25M0R --- X-number: 25 --- -Y Rotation
SimulationX26M0R --- X-number: 26 --- -Z Rotation

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 21 | 0.1201 | -0.0150 | 0.1350 | -0.0919 | -0.0106 | -0.0556 | 5 | 6 | 0.1261 | 0.0539 | 30.1 | 18.9 | 0.3653 |
| 21 | 22 | 0.1125 | 0.0300 | -0.0653 | -0.1740 | -0.2689 | -0.1185 | 4 | 6 | 0.1139 | 0.0762 | 55.0 | 19.1 | 0.3169 |
| 22 | 23 | -0.0672 | -0.0195 | 0.0950 | 0.1321 | 0.2484 | -0.0282 | 4 | 7 | 0.0614 | 0.0963 | 51.0 | 17.4 | 0.2090 |
| 23 | 24 | -0.0782 | -0.0149 | -0.1537 | 0.1273 | 0.0612 | 0.0497 | 5 | 7 | 0.0540 | 0.0753 | 30.6 | 16.5 | 0.2283 |
| 24 | 25 | -0.1012 | 0.0131 | -0.0691 | -0.3526 | -0.1185 | 0.0500 | 5 | 7 | 0.1103 | 0.1274 | 30.1 | 16.6 | 0.2652 |
| 25 | 26 | -0.0722 | 0.0265 | 0.2958 | 0.4590 | 0.1509 | 0.0515 | 5 | 7 | 0.1636 | 0.0880 | 31.5 | 16.5 | 0.5103 |
| 26 | 0 | 0.0472 | -0.0375 | -0.2425 | -0.1615 | -0.0546 | 0.0260 | 5 | 7 | 0.1418 | 0.0644 | 29.6 | 17.3 | 0.4189 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 21 | 0.1022 | -0.0086 | 0.0890 | 0.0180 | -0.1104 | 0.0176 | 4 | 6 | 0.0463 | 0.0539 | 41.8 | 18.9 | 0.1870 |
| 21 | 22 | 0.0885 | 0.0102 | -0.0599 | 0.1529 | 0.4747 | -0.1109 | 4 | 6 | 0.0657 | 0.0762 | 43.2 | 19.1 | 0.3160 |
| 22 | 23 | -0.0431 | 0.0204 | 0.0032 | -0.1576 | -0.2926 | 0.1791 | 4 | 7 | 0.0221 | 0.0963 | 39.5 | 17.4 | 0.1600 |
| 23 | 24 | -0.0741 | 0.0102 | -0.0513 | -0.1450 | -0.1477 | 0.0483 | 4 | 7 | 0.0809 | 0.0753 | 41.3 | 16.5 | 0.1494 |
| 24 | 25 | -0.0529 | -0.0205 | -0.0263 | 0.0041 | 0.3762 | -0.1123 | 4 | 7 | 0.1143 | 0.1274 | 40.6 | 16.6 | 0.1975 |
| 25 | 26 | -0.0446 | 0.0391 | 0.1318 | 0.2022 | -0.1967 | 0.1092 | 4 | 7 | 0.0550 | 0.0880 | 44.1 | 16.5 | 0.2761 |
| 26 | 0 | -0.0106 | -0.0058 | -0.0983 | -0.0298 | -0.1071 | -0.2350 | 5 | 7 | 0.0716 | 0.0644 | 26.9 | 17.3 | 0.2455 |

## E.1.6 Simulated Model: Combination Rotations

-------- Migration Results -------------
Reference Axis: Automatic
=====================================
Available scenes:
---------------------------------
SimulationX0M0R --- X-number: 0 --- Reference Position
SimulationX31M0R --- X-number: 31 --- +Y and +Z Rotation
SimulationX32M0R --- X-number: 32 --- +Y and -Z Rotation
SimulationX33M0R --- X-number: 33 --- -Y and +Z Rotation
SimulationX34M0R --- X-number: 34 --- -Y and -Z Rotation

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition <br> Number <br> Reference Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 31 | -0.0343 | -0.0034 | 0.0682 | -0.3777 | -0.1386 | -0.0654 | 5 | 7 | 0.1161 | 0.0653 | 30.1 | 16.9 | 0.3778 |
| 31 | 32 | 0.0161 | -0.0030 | -0.0272 | 0.0577 | 0.2296 | 0.1782 | 5 | 7 | 0.0731 | 0.0726 | 32.1 | 16.1 | 0.1811 |
| 32 | 33 | 0.1367 | -0.0162 | -0.0049 | -0.1437 | -0.5077 | -0.4008 | 4 | 7 | 0.0697 | 0.0930 | 57.2 | 16.8 | 0.2413 |
| 33 | 34 | 0.2310 | 0.0119 | 0.1454 | 0.0148 | -0.0250 | -0.0206 | 5 | 6 | 0.0506 | 0.0910 | 33.6 | 18.7 | 0.3207 |
| 34 | 0 | -0.3651 | 0.0615 | -0.1895 | -0.2222 | 0.1249 | 0.1269 | 4 | 6 | 0.1069 | 0.0877 | 50.5 | 19.3 | 0.4516 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 31 | 0.0394 | 0.0102 | -0.0304 | -0.0012 | 0.3588 | -0.0091 | 4 | 7 | 0.0636 | 0.0653 | 41.8 | 16.9 | 0.1941 |
| 31 | 32 | -0.0351 | -0.0201 | 0.0395 | 0.0447 | -0.1245 | -0.0117 | 4 | 7 | 0.0427 | 0.0726 | 43.7 | 16.1 | 0.1279 |
| 32 | 33 | 0.1242 | -0.0373 | 0.0166 | 0.0745 | -0.1716 | -0.0457 | 4 | 7 | 0.0319 | 0.0930 | 44.4 | 16.8 | 0.1950 |
| 33 | 34 | 0.1234 | 0.0316 | 0.0725 | 0.0033 | -0.0377 | -0.0835 | 4 | 6 | 0.0427 | 0.0910 | 53.5 | 18.7 | 0.1848 |
| 34 | 0 | -0.2747 | 0.0155 | -0.0709 | -0.3450 | -0.3473 | 0.0496 | 4 | 6 | 0.0418 | 0.0877 | 39.7 | 19.3 | 0.3853 |

## E. 2 Precision Validation Calculations

## E.2.1 Phantom Model Precision

| Superior Precision | X | Y | Z | Rx | Ry | Rz | MTPM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Translation | -0.0959 | 0.0047 | -0.0994 | -0.1921 | 0.1246 | 0.1316 | 0.2006 |
|  | 0.0919 | -0.0142 | 0.0010 | 0.3134 | 0.0404 | -0.0137 | 0.1852 |
|  | -0.0495 | -0.0076 | -0.0076 | -0.0389 | -0.1682 | 0.0249 | 0.1736 |
|  | -0.1073 | -0.0069 | 0.0233 | -0.0371 | -0.1174 | 0.0025 | 0.1819 |
|  | 0.2001 | 0.0039 | 0.0940 | -0.2776 | 0.2825 | -0.1079 | 0.3738 |
|  | 0.0013 | 0.0078 | -0.1109 | 0.2959 | -0.1338 | 0.0222 | 0.1822 |
|  | -0.1103 | 0.0059 | -0.0207 | -0.0881 | 0.3406 | 0.0932 | 0.1970 |
| Rotation | -0.0419 | 0.0028 | -0.1568 | -0.1478 | 0.1946 | 0.1006 | 0.2931 |
|  | -0.0352 | -0.0654 | 0.2452 | 0.1499 | -0.4426 | -0.0420 | 0.4663 |
|  | 0.0005 | 0.0471 | -0.1789 | -0.1704 | 0.1772 | 0.0060 | 0.2746 |
|  | -0.0040 | -0.0475 | -0.0031 | 0.1193 | 0.1932 | 0.0321 | 0.1274 |
|  | -0.0860 | 0.0311 | 0.0661 | 0.2073 | -0.1507 | -0.0379 | 0.2212 |
|  | 0.1784 | -0.0045 | -0.0509 | -0.2825 | 0.4578 | 0.0068 | 0.4829 |
|  | -0.0869 | 0.0295 | 0.0104 | -0.0407 | -0.1112 | 0.0405 | 0.1375 |
| Combination Rotation | -0.1188 | -0.0008 | -0.0603 | 0.0861 | -0.1392 | 0.0232 | 0.1689 |
|  | 0.2238 | 0.0135 | 0.0548 | -0.0012 | 0.0183 | -0.1154 | 0.2986 |
|  | -0.1889 | 0.0318 | 0.0519 | -0.0144 | 0.0025 | 0.0798 | 0.2805 |
|  | 0.0826 | 0.0124 | -0.0156 | 0.1889 | 0.1599 | -0.0452 | 0.1534 |
|  | -0.0869 | 0.0205 | -0.0415 | -0.0164 | -0.0999 | 0.0734 | 0.1633 |
| Standard Deviation | 0.1167 | 0.0265 | 0.0958 | 0.1773 | 0.2179 | 0.0661 | 0.1045 |
| Precision | 0.2438 | 0.0553 | 0.2001 | 0.3706 | 0.4554 | 0.1382 | 0.2185 |


| Inferior Precision | X | Y | Z | Rx | Ry | Rz | MTPM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Translation | -0.0695 | -0.0016 | -0.0228 | -0.0753 | -0.1150 | 0.1038 | 0.1520 |
|  | 0.0464 | 0.0119 | -0.0657 | -0.0821 | 0.2288 | -0.0056 | 0.1725 |
|  | -0.0430 | -0.0473 | -0.0229 | -0.2250 | -0.1479 | 0.0923 | 0.2254 |
|  | -0.0489 | 0.0145 | 0.0097 | 0.1422 | 0.1446 | 0.0334 | 0.1160 |
|  | 0.1131 | 0.0259 | 0.1476 | 0.2422 | -0.1413 | -0.1126 | 0.3018 |
|  | -0.0076 | -0.0246 | -0.1430 | -0.1811 | -0.0316 | 0.0382 | 0.2149 |
|  | -0.0557 | 0.0306 | 0.0422 | 0.1102 | 0.0293 | -0.0472 | 0.1257 |
| Rotation | -0.0504 | 0.0131 | -0.1080 | -0.2124 | 0.0444 | 0.1574 | 0.1837 |
|  | -0.0061 | -0.0181 | 0.0786 | -0.0067 | 0.0873 | -0.0080 | 0.1618 |
|  | -0.0034 | -0.0116 | -0.0963 | 0.0346 | -0.0111 | -0.0624 | 0.1532 |
|  | 0.0157 | -0.0092 | 0.0138 | 0.1171 | 0.0511 | 0.0489 | 0.1109 |
|  | -0.0210 | 0.0566 | 0.0884 | 0.2524 | 0.2801 | -0.0152 | 0.3024 |
|  | 0.0630 | -0.0265 | -0.0135 | 0.0103 | -0.1812 | -0.0237 | 0.1545 |
|  | -0.0498 | 0.0223 | 0.0139 | 0.1267 | -0.1597 | -0.0596 | 0.1328 |
| Combination Rotation | -0.0858 | -0.0031 | -0.0638 | -0.1601 | 0.0049 | 0.2068 | 0.1552 |
|  | 0.1168 | 0.0471 | 0.0189 | -0.0590 | 0.0066 | -0.0850 | 0.1588 |
|  | -0.0833 | 0.0201 | 0.0353 | 0.0000 | -0.0393 | 0.0501 | 0.1353 |
|  | 0.0579 | 0.0028 | -0.0424 | -0.0653 | 0.0991 | -0.0183 | 0.1280 |
|  | -0.0729 | 0.0208 | -0.0008 | 0.0869 | -0.2382 | -0.0767 | 0.1648 |
| Standard Deviation | 0.0631 | 0.0260 | 0.0713 | 0.1429 | 0.1389 | 0.0845 | 0.0549 |
| Precision | 0.1319 | 0.0544 | 0.1490 | 0.2987 | 0.2902 | 0.1766 | 0.1147 |

## E.2.2 Simulation Model Precision

| Superior Precision | X | Y | Z | Rx | Ry | Rz | MTPM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Translation | -0.0491 | 0.0117 | 0.0952 | 0.0319 | -0.0367 | -0.0132 | 0.1632 |
|  | 0.1124 | 0.0100 | -0.0357 | -0.0360 | 0.1129 | -0.0397 | 0.1559 |
|  | 0.0416 | -0.0301 | -0.0456 | -0.1366 | -0.0891 | -0.0127 | 0.1416 |
|  | -0.0352 | 0.0011 | -0.0052 | 0.0740 | -0.0480 | -0.0574 | 0.0791 |
|  | -0.0426 | 0.0200 | -0.0054 | 0.1657 | 0.1601 | 0.0634 | 0.1311 |
|  | -0.1226 | -0.0042 | 0.0529 | -0.1410 | 0.0619 | 0.0542 | 0.2870 |
|  | 0.0951 | -0.0087 | -0.0562 | 0.0414 | -0.1606 | 0.0059 | 0.2725 |
| Rotation | 0.1201 | -0.0150 | 0.1350 | -0.0919 | -0.0106 | -0.0556 | 0.3653 |
|  | 0.1125 | 0.0300 | -0.0653 | -0.1740 | -0.2689 | -0.1185 | 0.3169 |
|  | -0.0672 | -0.0195 | 0.0950 | 0.1321 | 0.2484 | -0.0282 | 0.2090 |
|  | -0.0782 | -0.0149 | -0.1537 | 0.1273 | 0.0612 | 0.0497 | 0.2283 |
|  | -0.1012 | 0.0131 | -0.0691 | -0.3526 | -0.1185 | 0.0500 | 0.2652 |
|  | -0.0722 | 0.0265 | 0.2958 | 0.4590 | 0.1509 | 0.0515 | 0.5103 |
|  | 0.0472 | -0.0375 | -0.2425 | -0.1615 | -0.0546 | 0.0260 | 0.4189 |
| Combination Rotation | -0.0343 | -0.0034 | 0.0682 | -0.3777 | -0.1386 | -0.0654 | 0.3778 |
|  | 0.0161 | -0.0030 | -0.0272 | 0.0577 | 0.2296 | 0.1782 | 0.1811 |
|  | 0.1367 | -0.0162 | -0.0049 | -0.1437 | -0.5077 | -0.4008 | 0.2413 |
|  | 0.2310 | 0.0119 | 0.1454 | 0.0148 | -0.0250 | -0.0206 | 0.3207 |
|  | -0.3651 | 0.0615 | -0.1895 | -0.2222 | 0.1249 | 0.1269 | 0.4516 |
| Standard <br> Deviation | 0.1304 | 0.0233 | 0.1263 | 0.1968 | 0.1823 | 0.1177 | 0.1177 |
| Precision | 0.2725 | 0.0488 | 0.2640 | 0.4112 | 0.3810 | 0.2460 | 0.2461 |


| Inferior Precision | X | Y | Z | Rx | Ry | Rz | MTPM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Translation | -0.0416 | 0.0089 | 0.0003 | -0.4128 | -0.1114 | 0.0448 | 0.1974 |
|  | 0.0934 | 0.0136 | -0.0076 | 0.0331 | 0.0934 | -0.0362 | 0.1515 |
|  | 0.0227 | -0.0329 | -0.0266 | 0.1283 | 0.0137 | -0.0417 | 0.0631 |
|  | -0.0156 | -0.0012 | 0.0344 | 0.4323 | 0.1770 | 0.0576 | 0.2425 |
|  | -0.0428 | 0.0118 | -0.0046 | -0.0775 | -0.1656 | 0.0320 | 0.1294 |
|  | -0.0648 | 0.0139 | -0.0003 | -0.2766 | -0.0367 | -0.0377 | 0.1415 |
|  | 0.0485 | -0.0142 | 0.0044 | 0.1747 | 0.0293 | -0.0216 | 0.0806 |
| Rotation | 0.1022 | -0.0086 | 0.0890 | 0.0180 | -0.1104 | 0.0176 | 0.1870 |
|  | 0.0885 | 0.0102 | -0.0599 | 0.1529 | 0.4747 | -0.1109 | 0.3160 |
|  | -0.0431 | 0.0204 | 0.0032 | -0.1576 | -0.2926 | 0.1791 | 0.1600 |
|  | -0.0741 | 0.0102 | -0.0513 | -0.1450 | -0.1477 | 0.0483 | 0.1494 |
|  | -0.0529 | -0.0205 | -0.0263 | 0.0041 | 0.3762 | -0.1123 | 0.1975 |
|  | -0.0446 | 0.0391 | 0.1318 | 0.2022 | -0.1967 | 0.1092 | 0.2761 |
|  | -0.0106 | -0.0058 | -0.0983 | -0.0298 | -0.1071 | -0.2350 | 0.2455 |
| Combination Rotation | 0.0394 | 0.0102 | -0.0304 | -0.0012 | 0.3588 | -0.0091 | 0.1941 |
|  | -0.0351 | -0.0201 | 0.0395 | 0.0447 | -0.1245 | -0.0117 | 0.1279 |
|  | 0.1242 | -0.0373 | 0.0166 | 0.0745 | -0.1716 | -0.0457 | 0.1950 |
|  | 0.1234 | 0.0316 | 0.0725 | 0.0033 | -0.0377 | -0.0835 | 0.1848 |
|  | -0.2747 | 0.0155 | -0.0709 | -0.3450 | -0.3473 | 0.0496 | 0.3853 |
| Standard <br> Deviation | 0.0939 | 0.0205 | 0.0562 | 0.2006 | 0.2247 | 0.0905 | 0.0780 |
| Precision | 0.1963 | 0.0429 | 0.1175 | 0.4192 | 0.4697 | 0.1892 | 0.1630 |

## E. 3 Accuracy Data

This is the raw output for the accuracy assessment exams as created by MB-RSA an imported into excel. This data was then used to calculate the prediction intervals using Minitab 16. The accuracy was calculated as half the width of the average prediction interval for each direction assessed as shown in Section E.4.

## E.3.1 Caudal Superior: 0.5mm

```
-------- Migration Results
```

Reference Axis: Automatic
Available scenes:

CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative C S 05X1M0R --- X-number: 1 --- Follow-up: Postoperative C S 05X2M0R --- X-number: 2 --- Follow-up: Postoperative C S 05X3M0R --- X-number: 3 --- Follow-up: Postoperative C S 05X4M0R --- X-number: 4 --- Follow-up: Postoperative C S 05X5M0R --- X-number: 5 --- Follow-up: Postoperative C S 05X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition <br> Number <br> Reference Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.4925 | -0.0197 | 0.2016 | 0.0442 | -0.0051 | 0.0182 | 7 | 6 | 0.0268 | 0.0065 | 18.5 | 19.8 | 0.5697 |
| 0 | 2 | -0.0202 | 0.4983 | 0.1618 | 0.0574 | -0.0271 | 0.0256 | 7 | 6 | 0.0221 | 0.0064 | 18.5 | 19.8 | 0.5632 |
| 0 | 3 | -0.0059 | -0.0122 | 0.6843 | 0.0564 | -0.0217 | 0.0319 | 7 | 6 | 0.0300 | 0.0120 | 18.5 | 19.8 | 0.7311 |
| 0 | 4 | -0.5210 | 0.0026 | 0.0480 | 0.0155 | -0.0218 | 0.0281 | 7 | 6 | 0.0268 | 0.0091 | 18.5 | 19.8 | 0.5419 |
| 0 | 5 | -0.0104 | -0.4976 | 0.0704 | 0.0387 | -0.0178 | 0.0278 | 7 | 6 | 0.0208 | 0.0092 | 18.5 | 19.8 | 0.5232 |
| 0 | 6 | -0.0022 | 0.0100 | -0.4760 | 0.0338 | -0.0040 | 0.0258 | 7 | 6 | 0.0357 | 0.0023 | 18.5 | 19.8 | 0.5243 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0105 | 0.0070 | 0.1107 | 0.0624 | -0.0169 | 0.0016 | 7 | 6 | 0.0150 | 0.0065 | 19.7 | 19.8 | 0.1577 |
| 0 | 2 | -0.0137 | 0.0021 | 0.0717 | 0.0252 | -0.0218 | -0.0051 | 7 | 6 | 0.0261 | 0.0064 | 19.7 | 19.8 | 0.0853 |
| 0 | 3 | -0.0010 | -0.0058 | 0.0775 | 0.0224 | 0.0090 | 0.0080 | 7 | 6 | 0.0272 | 0.0120 | 19.7 | 19.8 | 0.0927 |
| 0 | 4 | -0.0110 | 0.0017 | 0.0133 | -0.0001 | -0.0122 | -0.016 | 7 | 6 | 0.0164 | 0.0091 | 19.7 | 19.8 | 0.0284 |
| 0 | 5 | -0.0031 | -0.0007 | 0.0215 | -0.0001 | 0.0021 | 0.0234 | 7 | 6 | 0.0215 | 0.0092 | 19.7 | 19.8 | 0.0329 |
| 0 | 6 | -0.0047 | 0.0036 | -0.0155 | -0.0116 | -0.0108 | 0.0057 | 7 | 6 | 0.0365 | 0.0023 | 19.7 | 19.8 | 0.0831 |

## E.3.2 Caudal Superior: $\mathbf{1 m m}$

-------- Migration Results ------------
Reference Axis: Automatic
Available scenes:

CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative
C S 1X1M0R --- X-number: 1 --- Follow-up: Postoperative
C S 1X2M0R --- X-number: 2 --- Follow-up: Postoperative
C S 1X3M0R --- X-number: 3 --- Follow-up: Postoperative
C S 1X4M0R --- X-number: 4 --- Follow-up: Postoperative
C S 1X5M0R --- X-number: 5 --- Follow-up: Postoperative
C S 1X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.9803 | -0.0005 | 0.1183 | 0.0448 | -0.0086 | 0.0002 | 7 | 6 | 0.0224 | 0.0146 | 18.5 | 19.8 | 1.0094 |
| 0 | 2 | -0.0102 | 1.0062 | 0.0365 | 0.0337 | 0.0029 | 0.0362 | 7 | 6 | 0.0201 | 0.0033 | 18.5 | 19.8 | 1.0461 |
| 0 | 3 | -0.0157 | -0.0092 | 1.1696 | 0.0438 | 0.0015 | 0.0169 | 7 | 6 | 0.0200 | 0.0070 | 18.5 | 19.8 | 1.2056 |
| 0 | 4 | -1.0417 | -0.0144 | 0.2770 | 0.0625 | -0.0467 | 0.0355 | 7 | 6 | 0.0369 | 0.0270 | 18.5 | 19.8 | 1.1384 |
| 0 | 5 | -0.0154 | -0.989 | 0.0827 | 0.0361 | -0.0185 | 0.0275 | 7 | 6 | 0.0188 | 0.0041 | 18.5 | 19.8 | 1.0078 |
| 0 | 6 | -0.013 | 0.0154 | -1.0138 | 0.0158 | -0.0220 | 0.0197 | 7 | 6 | 0.0254 | 0.0039 | 18.5 | 19.8 | 1.0493 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0107 | -0.0005 | 0.0551 | 0.0073 | -0.0020 | -0.0262 | 7 | 6 | 0.0238 | 0.0146 | 19.7 | 19.8 | 0.0706 |
| 0 | 2 | -0.0036 | 0.0040 | 0.0160 | 0.0102 | 0.0053 | -0.0136 | 7 | 6 | 0.0143 | 0.0033 | 19.7 | 19.8 | 0.0414 |
| 0 | 3 | -0.0082 | -0.0044 | 0.0912 | 0.0232 | -0.0004 | -0.0469 | 7 | 6 | 0.0173 | 0.0070 | 19.7 | 19.8 | 0.1028 |
| 0 | 4 | -0.0144 | -0.0136 | 0.1525 | 0.0384 | -0.0075 | 0.0037 | 7 | 6 | 0.0159 | 0.0270 | 19.7 | 19.8 | 0.1747 |
| 0 | 5 | -0.0078 | 0.0002 | 0.0326 | 0.0067 | -0.0068 | 0.0254 | 7 | 6 | 0.0071 | 0.0041 | 19.7 | 19.8 | 0.0385 |
| 0 | 6 | -0.0067 | 0.0085 | -0.0227 | -0.0072 | -0.0047 | 0.0103 | 7 | 6 | 0.0144 | 0.0039 | 19.7 | 19.8 | 0.0474 |

## E.3.3 Caudal Superior: 5mm

## -------- Migration Results -----------

Reference Axis: Automatic
========================================

Available scenes:
CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative
C S 5X1M0R --- X-number: 1 --- Follow-up: Postoperative
C S 5X2M0R --- X-number: 2 --- Follow-up: Postoperative
C S 5X3M0R --- X-number: 3 --- Follow-up: Postoperative
C S 5X4M0R --- X-number: 4 --- Follow-up: Postoperative
C S 5X5M0R --- X-number: 5 --- Follow-up: Postoperative
C S 5X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition <br> Number <br> Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 5.0276 | -0.0056 | 0.0426 | 0.0525 | 0.0798 | 0.0184 | 7 | 6 | 0.1617 | 0.0165 | 18.5 | 19.8 | 5.1832 |
| 0 | 2 | 0.0063 | 4.9920 | 0.1007 | 0.0664 | -0.0207 | 0.0159 | 7 | 6 | 0.0402 | 0.0250 | 18.5 | 19.8 | 5.0161 |
| 0 | 3 | -0.0243 | -0.0283 | 5.3431 | 0.0736 | -0.0115 | 0.0122 | 7 | 6 | 0.0175 | 0.0184 | 18.5 | 19.8 | 5.3606 |
| 0 | 4 | -4.9921 | 0.0025 | 0.0303 | 0.0121 | 0.0061 | -0.0015 | 7 | 6 | 0.0166 | 0.0150 | 18.5 | 19.8 | 4.9996 |
| 0 | 5 | -0.0358 | -5.0194 | 0.3036 | 0.0730 | -0.0277 | 0.0376 | 7 | 6 | 0.0200 | 0.0180 | 18.5 | 19.8 | 5.0698 |
| 0 | 6 | -0.0042 | -0.0036 | -4.8776 | 0.0415 | -0.0300 | 0.0419 | 7 | 6 | 0.0382 | 0.0038 | 18.5 | 19.8 | 4.9215 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0014 | -0.0050 | 0.0392 | 0.0068 | -0.0014 | -0.0171 | 7 | 6 | 0.0202 | 0.0165 | 19.7 | 19.8 | 0.0502 |
| 0 | 2 | 0.0013 | -0.0115 | 0.0365 | 0.0048 | -0.0007 | 0.0256 | 7 | 6 | 0.0163 | 0.0250 | 19.7 | 19.8 | 0.0490 |
| 0 | 3 | -0.0080 | -0.0106 | 0.1861 | 0.0576 | 0.0078 | -0.0068 | 7 | 6 | 0.0247 | 0.0184 | 19.7 | 19.8 | 0.2148 |
| 0 | 4 | 0.0043 | 0.0031 | -0.0046 | -0.0089 | 0.0056 | -0.0299 | 7 | 6 | 0.0407 | 0.0150 | 19.7 | 19.8 | 0.0773 |
| 0 | 5 | -0.0172 | -0.0007 | 0.1652 | 0.0551 | -0.0060 | -0.0045 | 7 | 6 | 0.0202 | 0.0180 | 19.7 | 19.8 | 0.1798 |
| 0 | 6 | 0.0033 | -0.0034 | 0.0604 | 0.0185 | 0.0029 | -0.0053 | 7 | 6 | 0.0190 | 0.0038 | 19.7 | 19.8 | 0.0688 |

## E.3.4 Caudal Superior: 10mm

```
-------- Migration Results -----------
```

Reference Axis: Automatic

Available scenes:
CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative
C S 10X1M0R --- X-number: 1 --- Follow-up: Postoperative
C S 10X2M0R --- X-number: 2 --- Follow-up: Postoperative
C S 10X3M0R --- X-number: 3 --- Follow-up: Postoperative
C S 10X4M0R --- X-number: 4 --- Follow-up: Postoperative
C S 10X5M0R --- X-number: 5 --- Follow-up: Postoperative
C S 10X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 10.0019 | 0.0152 | 0.0845 | 0.0706 | 0.1133 | 0.0109 | 7 | 6 | 0.1525 | 0.0176 | 18.5 | 19.8 | 10.1155 |
| 0 | 2 | -0.0315 | 10.0134 | 0.0164 | 0.0105 | -0.0430 | 0.0418 | 7 | 6 | 0.0216 | 0.0117 | 18.5 | 19.8 | 10.0264 |
| 0 | 3 | -0.0388 | 0.0050 | 10.1872 | 0.0620 | -0.0690 | 0.0445 | 7 | 6 | 0.0605 | 0.0234 | 18.5 | 19.8 | 10.2793 |
| 0 | 4 | -9.9839 | -0.0081 | 0.0990 | 0.0229 | 0.0275 | 0.0059 | 7 | 6 | 0.0348 | 0.0332 | 18.5 | 19.8 | 10.0120 |
| 0 | 5 | -0.0184 | -9.9639 | 0.0143 | 0.0457 | -0.0086 | 0.0028 | 7 | 6 | 0.0226 | 0.0177 | 18.5 | 19.8 | 9.9861 |
| 0 | 6 | 0.0023 | -0.0214 | -9.7871 | 0.0630 | -0.0284 | 0.0555 | 7 | 6 | 0.0256 | 0.0122 | 18.5 | 19.8 | 9.8336 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0112 | -0.0014 | 0.0631 | 0.0177 | 0.0089 | -0.0221 | 7 | 6 | 0.0279 | 0.0176 | 19.7 | 19.8 | 0.1152 |
| 0 | 2 | -0.0147 | 0.0027 | -0.0170 | 0.0208 | -0.0127 | -0.0364 | 7 | 6 | 0.0160 | 0.0117 | 19.7 | 19.8 | 0.0457 |
| 0 | 3 | -0.0242 | 0.0034 | 0.0959 | 0.0185 | -0.0259 | -0.0132 | 7 | 6 | 0.0305 | 0.0234 | 19.7 | 19.8 | 0.1554 |
| 0 | 4 | 0.0032 | -0.0024 | 0.0479 | 0.0333 | -0.0043 | -0.0264 | 7 | 6 | 0.0231 | 0.0332 | 19.7 | 19.8 | 0.0834 |
| 0 | 5 | -0.0068 | 0.0112 | -0.0092 | -0.0004 | -0.0017 | -0.0346 | 7 | 6 | 0.0145 | 0.0177 | 19.7 | 19.8 | 0.0467 |
| 0 | 6 | -0.0026 | -0.0154 | 0.1084 | 0.0395 | -0.0116 | 0.0067 | 7 | 6 | 0.0242 | 0.0122 | 19.7 | 19.8 | 0.1353 |

## E.3.5 Caudal Superior: 20mm

-------- Migration Results -------------
Reference Axis: Automatic
=====================================
Available scenes:
---------------------------------
CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative
C S 20X1M0R --- X-number: 1 --- Follow-up: Postoperative
C S 20X2M0R --- X-number: 2 --- Follow-up: Postoperative
C S 20X3M0R --- X-number: 3 --- Follow-up: Postoperative
C S 20X4M0R --- X-number: 4 --- Follow-up: Postoperative
C S 20X5M0R --- X-number: 5 --- Follow-up: Postoperative
C S 20X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid Body Error | Rigid Body <br> Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 20.0235 | -0.0143 | 0.1165 | 0.0881 | 0.0472 | 0.0225 | 7 | 6 | 0.1471 | 0.0099 | 18.5 | 19.8 | 20.1579 |
| 0 | 2 | -0.0391 | 19.9844 | 0.1162 | 0.0430 | -0.0063 | 0.3203 | 3 | 6 | 0.0148 | 0.0240 | 34.4 | 19.8 | 19.9992 |
| 0 | 3 | -0.0377 | -0.0211 | 20.1803 | 0.0568 | -0.0673 | 0.0413 | 7 | 6 | 0.0501 | 0.0237 | 18.5 | 19.8 | 20.2652 |
| 0 | 4 | -20.0596 | -0.0159 | 0.1554 | 0.0506 | -0.0243 | 0.0323 | 7 | 6 | 0.0318 | 0.0421 | 18.5 | 19.8 | 20.0848 |
| 0 | 5 | -0.0173 | -20.004 | 0.1911 | 0.0621 | -0.0156 | 0.0426 | 7 | 6 | 0.0154 | 0.0078 | 18.5 | 19.8 | 20.0526 |
| 0 | 6 | -0.0098 | 0.0211 | -19.8533 | 0.0608 | -0.0058 | 0.0657 | 7 | 6 | 0.1258 | 0.0313 | 18.5 | 19.8 | 20.0629 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.0010 | -0.0123 | 0.0802 | 0.0231 | 0.0094 | -0.0115 | 6 | 6 | 0.0120 | 0.0099 | 19.8 | 19.8 | 0.0930 |
| 0 | 2 | -0.0144 | -0.0043 | 0.0552 | 0.0143 | -0.0008 | -0.0126 | 7 | 6 | 0.0245 | 0.0240 | 19.7 | 19.8 | 0.0735 |
| 0 | 3 | -0.0100 | -0.0016 | 0.0819 | 0.0279 | 0.0042 | -0.0350 | 7 | 6 | 0.0248 | 0.0237 | 19.7 | 19.8 | 0.1081 |
| 0 | 4 | -0.0290 | -0.0067 | 0.0878 | 0.0272 | -0.0196 | -0.0096 | 7 | 6 | 0.0178 | 0.0421 | 19.7 | 19.8 | 0.1116 |
| 0 | 5 | -0.0042 | -0.0121 | 0.1105 | 0.0210 | 0.0106 | 0.0141 | 7 | 6 | 0.0220 | 0.0078 | 19.7 | 19.8 | 0.1446 |
| 0 | 6 | -0.0083 | -0.0025 | 0.0856 | 0.0193 | 0.0041 | 0.0010 | 7 | 6 | 0.0323 | 0.0313 | 19.7 | 19.8 | 0.1106 |

## E.3.6 Caudal Inferior: $\mathbf{0 . 5 m m}$

## -------- Migration Results ------------

Reference Axis: Automatic


Available scenes:
CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative C I 05X1M0R --- X-number: 1 --- Follow-up: Postoperative C I 05X2M0R --- X-number: 2 --- Follow-up: Postoperative C I 05X3M0R --- X-number: 3 --- Follow-up: Postoperative C I 05X4M0R --- X-number: 4 --- Follow-up: Postoperative C I 05X5M0R --- X-number: 5 --- Follow-up: Postoperative C I 05X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.4814 | -0.0079 | 0.2330 | 0.0426 | -0.0066 | 0.0082 | 7 | 6 | 0.0200 | 0.0132 | 18.5 | 19.8 | 0.5539 |
| 0 | 2 | -0.0241 | 0.4883 | 0.1958 | 0.0630 | -0.0174 | 0.0348 | 7 | 6 | 0.0142 | 0.0072 | 18.5 | 19.8 | 0.5634 |
| 0 | 3 | -0.0112 | -0.0100 | 0.7189 | 0.0601 | -0.0029 | 0.0220 | 7 | 6 | 0.0381 | 0.0138 | 18.5 | 19.8 | 0.7629 |
| 0 | 4 | -0.5233 | -0.0176 | 0.1902 | 0.0446 | -0.0280 | 0.0290 | 7 | 6 | 0.0270 | 0.0441 | 18.5 | 19.8 | 0.5888 |
| 0 | 5 | -0.0223 | -0.4976 | 0.0513 | 0.0264 | -0.0362 | 0.0294 | 7 | 6 | 0.0139 | 0.0092 | 18.5 | 19.8 | 0.5216 |
| 0 | 6 | -0.0121 | 0.0208 | -0.5006 | 0.0290 | 0.0008 | 0.0183 | 7 | 6 | 0.0308 | 0.0070 | 18.5 | 19.8 | 0.5405 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.4884 | 0.0012 | 0.1296 | 0.0334 | 0.0050 | 0.0054 | 7 | 6 | 0.0184 | 0.0132 | 19.7 | 19.8 | 0.5213 |
| 0 | 2 | -0.0081 | 0.4919 | 0.0909 | 0.0212 | 0.0058 | -0.0278 | 7 | 6 | 0.0295 | 0.0072 | 19.7 | 19.8 | 0.5321 |
| 0 | 3 | -0.0069 | -0.0055 | 0.6095 | 0.0352 | 0.0029 | -0.0275 | 7 | 6 | 0.0337 | 0.0138 | 19.7 | 19.8 | 0.6460 |
| 0 | 4 | -0.5005 | -0.0074 | 0.1010 | 0.0165 | 0.0018 | -0.0294 | 7 | 6 | 0.0360 | 0.0441 | 19.7 | 19.8 | 0.5348 |
| 0 | 5 | -0.0055 | -0.5076 | 0.0148 | -0.0119 | 0.0035 | -0.0259 | 7 | 6 | 0.0235 | 0.0092 | 19.7 | 19.8 | 0.5281 |
| 0 | 6 | 0.0018 | 0.0071 | -0.5137 | -0.0061 | 0.0028 | -0.0068 | 7 | 6 | 0.0262 | 0.0070 | 19.7 | 19.8 | 0.5541 |

## E.3.7 Caudal Inferior: 1mm

## -------- Migration Results -----------

Reference Axis: Automatic

Available scenes:
CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative C I 1X1M0R --- X-number: 1 --- Follow-up: Postoperative
C I 1X2M0R --- X-number: 2 --- Follow-up: Postoperative
C I 1X3M0R --- X-number: 3 --- Follow-up: Postoperative
C I 1X4M0R --- X-number: 4 --- Follow-up: Postoperative
C I 1X5M0R --- X-number: 5 --- Follow-up: Postoperative C I 1X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.9771 | 0.0144 | 0.0630 | 0.0435 | -0.0207 | 0.0236 | 7 | 6 | 0.0218 | 0.0308 | 18.5 | 19.8 | 1.0009 |
| 0 | 2 | -0.0168 | 0.9881 | 0.2110 | 0.0649 | -0.0038 | 0.0158 | 7 | 6 | 0.0139 | 0.0077 | 18.5 | 19.8 | 1.0347 |
| 0 | 3 | -0.0370 | -0.0156 | 1.1599 | 0.0483 | -0.0164 | 0.0266 | 7 | 6 | 0.0227 | 0.0037 | 18.5 | 19.8 | 1.2011 |
| 0 | 4 | -1.0577 | -0.0047 | 0.0990 | 0.0203 | -0.0255 | 0.0202 | 7 | 6 | 0.0262 | 0.0497 | 18.5 | 19.8 | 1.0882 |
| 0 | 5 | -0.0040 | -1.0189 | 0.2377 | 0.0637 | 0.0138 | 0.0058 | 7 | 6 | 0.0218 | 0.0079 | 18.5 | 19.8 | 1.0764 |
| 0 | 6 | -0.0158 | -0.0055 | -0.7756 | 0.0590 | -0.0079 | -0.0083 | 7 | 6 | 0.0232 | 0.0217 | 18.5 | 19.8 | 0.8091 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.9909 | 0.0135 | 0.0344 | 0.0126 | -0.0082 | -0.0086 | 7 | 6 | 0.0134 | 0.0308 | 19.7 | 19.8 | 1.0080 |
| 0 | 2 | -0.0063 | 0.9974 | 0.1011 | 0.0337 | 0.0108 | -0.0367 | 7 | 6 | 0.0372 | 0.0077 | 19.7 | 19.8 | 1.0306 |
| 0 | 3 | -0.0131 | -0.0084 | 1.0845 | 0.0289 | 0.0010 | -0.0155 | 7 | 6 | 0.0209 | 0.0037 | 19.7 | 19.8 | 1.1114 |
| 0 | 4 | -1.0206 | -0.0077 | 0.0579 | 0.0192 | -0.0253 | 0.0019 | 7 | 6 | 0.0170 | 0.0497 | 19.7 | 19.8 | 1.0531 |
| 0 | 5 | -0.0031 | -1.0087 | 0.1164 | 0.0411 | 0.0011 | -0.0400 | 7 | 6 | 0.0338 | 0.0079 | 19.7 | 19.8 | 1.0493 |
| 0 | 6 | -0.0048 | 0.0008 | -0.8680 | 0.0479 | -0.0127 | -0.0120 | 7 | 6 | 0.0173 | 0.0217 | 19.7 | 19.8 | 0.8908 |

## E.3.8 Caudal Inferior: 5mm

## -------- Migration Results ------------

Reference Axis: Automatic
======================================1

Available scenes:
CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative C I 5X1M0R --- X-number: 1 --- Follow-up: Postoperative
C I 5X2M0R --- X-number: 2 --- Follow-up: Postoperative
C I 5X3M0R --- X-number: 3 --- Follow-up: Postoperative
C I 5X4M0R --- X-number: 4 --- Follow-up: Postoperative
C I 5X5M0R --- X-number: 5 --- Follow-up: Postoperative
C I 5X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 5.0022 | 0.0105 | 0.1040 | 0.0336 | 0.0081 | 0.0085 | 7 | 6 | 0.0206 | 0.0089 | 18.5 | 19.8 | 5.0281 |
| 0 | 2 | -0.0319 | 4.9978 | 0.2191 | 0.0738 | -0.0509 | 0.0209 | 7 | 6 | 0.0352 | 0.0212 | 18.5 | 19.8 | 5.0346 |
| 0 | 3 | -0.0167 | -0.0604 | 5.3170 | 0.0604 | 0.0065 | 0.0061 | 7 | 6 | 0.0210 | 0.0151 | 18.5 | 19.8 | 5.3362 |
| 0 | 4 | -5.0565 | -0.0076 | 0.2210 | 0.0592 | -0.0378 | 0.0175 | 7 | 6 | 0.0231 | 0.0368 | 18.5 | 19.8 | 5.0780 |
| 0 | 5 | -0.0118 | -4.9983 | 0.0372 | 0.0226 | -0.0235 | 0.0356 | 7 | 6 | 0.0192 | 0.0236 | 18.5 | 19.8 | 5.0164 |
| 0 | 6 | -0.0007 | 0.0501 | -4.9900 | 0.0051 | 0.0125 | 0.0184 | 7 | 6 | 0.0323 | 0.0058 | 18.5 | 19.8 | 5.0359 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 5.0040 | 0.0091 | 0.0647 | 0.0328 | 0.0104 | 0.0009 | 7 | 6 | 0.0213 | 0.0089 | 19.7 | 19.8 | 5.0199 |
| 0 | 2 | -0.0036 | 5.0017 | 0.1111 | 0.0284 | -0.0161 | -0.0061 | 7 | 6 | 0.0238 | 0.0212 | 19.7 | 19.8 | 5.0207 |
| 0 | 3 | -0.0155 | -0.0330 | 5.1620 | 0.0450 | 0.0051 | -0.0089 | 7 | 6 | 0.0347 | 0.0151 | 19.7 | 19.8 | 5.1994 |
| 0 | 4 | -5.0072 | -0.0022 | 0.1256 | 0.0209 | 0.0071 | -0.0139 | 7 | 6 | 0.0371 | 0.0368 | 19.7 | 19.8 | 5.0385 |
| 0 | 5 | 0.0002 | -5.0029 | 0.0106 | -0.0100 | -0.0019 | -0.0232 | 7 | 6 | 0.0194 | 0.0236 | 19.7 | 19.8 | 5.0255 |
| 0 | 6 | 0.0017 | 0.0162 | -4.9889 | 0.0103 | 0.0085 | 0.0028 | 7 | 6 | 0.0255 | 0.0058 | 19.7 | 19.8 | 5.0159 |

## E.3.9 Caudal Inferior: $\mathbf{1 0 m m}$

```
Reference Axis: Automatic
Available scenes:
CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative CI 10X1M0R --- X-number: 1 --- Follow-up: Postoperative C I 10X2M0R --- X-number: 2 --- Follow-up: Postoperative
C I 10X3M0R --- X-number: 3 --- Follow-up: Postoperative
C I 10X4M0R --- X-number: 4 --- Follow-up: Postoperative
C I 10X5M0R --- X-number: 5 --- Follow-up: Postoperative
C I 10X6M0R --- X-number: 6 --- Follow-up: Postoperative
```

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 9.9811 | 0.0148 | -0.0664 | 0.0502 | -0.0069 | 0.0109 | 7 | 6 | 0.0542 | 0.0234 | 18.5 | 19.8 | 10.0070 |
| 0 | 2 | -0.0117 | 9.9884 | 0.1782 | 0.0317 | -0.0132 | 0.0435 | 7 | 6 | 0.0220 | 0.0166 | 18.5 | 19.8 | 10.0200 |
| 0 | 3 | 0.0231 | -0.0118 | 10.0430 | 0.0306 | 0.0170 | -0.0348 | 7 | 6 | 0.0359 | 0.0289 | 18.5 | 19.8 | 10.0820 |
| 0 | 4 | -10.0048 | -0.0076 | 0.0724 | 0.0214 | 0.0029 | -0.0168 | 7 | 6 | 0.0286 | 0.0134 | 18.5 | 19.8 | 10.0303 |
| 0 | 5 | -0.0487 | -9.9917 | 0.2292 | 0.0814 | -0.0293 | 0.0387 | 7 | 6 | 0.0215 | 0.0142 | 18.5 | 19.8 | 10.0415 |
| 0 | 6 | -0.0509 | -0.0089 | -9.7468 | 0.0850 | -0.0470 | 0.0134 | 7 | 6 | 0.0403 | 0.0490 | 18.5 | 19.8 | 9.8065 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 9.9829 | -0.0008 | -0.0227 | -0.0114 | -0.0331 | -0.0259 | 7 | 6 | 0.0243 | 0.0307 | 19.3 | 19.8 | 10.0043 |
| 0 | 2 | -0.0112 | 9.9966 | 0.1082 | 0.0458 | -0.0185 | 0.0156 | 7 | 6 | 0.0277 | 0.0223 | 19.3 | 19.8 | 10.0374 |
| 0 | 3 | 0.0174 | -0.0034 | 10.0013 | 0.0204 | 0.0218 | -0.0273 | 7 | 6 | 0.0297 | 0.0273 | 19.3 | 19.8 | 10.1469 |
| 0 | 4 | -9.9889 | -0.0037 | 0.0368 | 0.0318 | 0.0086 | -0.0005 | 7 | 6 | 0.0412 | 0.0233 | 19.3 | 19.8 | 10.0583 |
| 0 | 5 | -0.0104 | -10.0047 | 0.1427 | 0.0503 | 0.0246 | -0.0314 | 7 | 6 | 0.0164 | 0.0123 | 19.3 | 19.8 | 10.0389 |
| 0 | 6 | -0.0386 | -0.0072 | -9.8783 | 0.0449 | -0.0440 | -0.0131 | 7 | 6 | 0.0231 | 0.0330 | 19.3 | 19.8 | 9.8462 |

## E.3.10 Caudal Inferior: $\mathbf{2 0 m m}$

## -------- Migration Results -----------

Reference Axis: Automatic


Available scenes:
CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative C I 20X1M0R --- X-number: 1 --- Follow-up: Postoperative
C I 20X2M0R --- X-number: 2 --- Follow-up: Postoperative
C I 20X3M0R --- X-number: 3 --- Follow-up: Postoperative
C I 20X4M0R --- X-number: 4 --- Follow-up: Postoperative
C I 20X5M0R --- X-number: 5 --- Follow-up: Postoperative C I 20X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X |
| :---: | :---: | :---: |

Model: T4

| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 1 | 20.0214 | -0.0009 | 0.1092 | 0.0631 | 0.0030 | 0.0371 |
| 0 | 2 | -0.0464 | 19.9808 | 0.1233 | 0.0484 | -0.0075 | 0.3263 |
| 0 | 3 | 0.0099 | 0.0091 | 20.031 | 0.0319 | -0.0381 | 0.0431 |
| 0 | 4 | -20.0957 | 0.0154 | 0.1321 | 0.0353 | -0.0087 | -0.0019 |
| 0 | 5 | -0.0286 | -19.9884 | 0.1451 | 0.0518 | -0.0311 | 0.0436 |
| 0 | 6 | -0.0072 | 0.0024 | -19.7200 | 0.0915 | -0.0251 | 0.0239 |


|  | \#Matched | Rigid | Rigid Body |  | Condition | Maximum |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \#Matched | Reference | Body | Error | Condition | Number | Total |
| Markers | Markers | Error | Reference | Number | Model | Motion |

19.8

| 6 | 0.0912 | 0.0047 | 18.5 | 19.8 | 20.0918 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 6 | 0.0143 | 0.0184 | 34.4 | 19.8 | 19.9986 |
| 6 | 0.0484 | 0.0170 | 18.5 | 19.8 | 20.1022 |
| 6 | 0.0287 | 0.0494 | 18.5 | 19.8 | 20.1244 |
| 6 | 0.0160 | 0.0244 | 18.5 | 19.8 | 20.0325 |
| 6 | 0.0231 | 0.0208 | 18.5 | 19.8 | 19.7498 |

Model: T8

| Reference: CaudalX0M0R | -- L1 |  |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 1 | 20.0094 | -0.0066 | 0.0620 | 0.0122 | 0.0104 | -0.0139 |
| 0 | 2 | -0.0170 | 20.0036 | 0.0807 | 0.0339 | -0.0032 | -0.0246 |
| 0 | 3 | 0.0194 | 0.0004 | 19.999 | 0.0010 | 0.0409 | -0.0352 |
| 0 | 4 | -20.0481 | 0.0030 | 0.0986 | 0.0154 | -0.0140 | 0.0043 |
| 0 | 5 | -0.0024 | -20.001 | 0.0563 | 0.0136 | 0.0061 | -0.0302 |
| 0 | 6 | 0.0099 | 0.0138 | -19.8335 | 0.0682 | -0.0035 | -0.0042 |

0.0347
0.0188
0.0336
0.015
0.0402
0.00
0.00
0.018
0.017
0.049
0.0244
0.0208
$19.8 \quad 20.0442$
19
19
20.0442
20.0377

| 19.8 | 20.0442 |
| :--- | :--- |
| 19.8 | 20.0377 |
| 19.8 | 20.0508 |

0.0402
19.8
20.0675
$19.8 \quad 20.0266$
19.819 .8500

## E.3.11 Caudal Rotation: $\mathbf{1 0}^{\circ}$

## -------- Migration Results ------------

Reference Axis: Automatic

|  |
| :---: |

Available scenes:
CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative C R 1X1M0R --- X-number: 1 --- Follow-up: Postoperative C R 1X2M0R --- X-number: 2 --- Follow-up: Postoperative C R 1X3M0R --- X-number: 3 --- Follow-up: Postoperative C R 1X4M0R --- X-number: 4 --- Follow-up: Postoperative C R 1X5M0R --- X-number: 5 --- Follow-up: Postoperative C R 1X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0333 | 0.0054 | 0.1302 | 0.0396 | -0.0071 | 0.0205 | 7 | 6 | 0.0262 | 0.0268 | 18.5 | 19.8 | 0.1786 |
| 0 | 2 | -0.0411 | -0.0061 | 0.1754 | 0.0424 | -0.0429 | 0.0324 | 7 | 6 | 0.0161 | 0.0313 | 18.5 | 19.8 | 0.2319 |
| 0 | 3 | -0.0329 | -0.0154 | 0.2730 | 0.0650 | -0.0273 | 0.0303 | 7 | 6 | 0.0103 | 0.0173 | 18.5 | 19.8 | 0.3080 |
| 0 | 4 | -0.0275 | -0.0407 | 0.3257 | 0.0743 | -0.0272 | 0.0321 | 7 | 6 | 0.0170 | 0.0124 | 18.5 | 19.8 | 0.3729 |
| 0 | 5 | -0.0047 | 0.0171 | 0.0327 | 0.0168 | 0.0114 | 0.0012 | 7 | 6 | 0.0128 | 0.0184 | 18.5 | 19.8 | 0.0653 |
| 0 | 6 | -0.0124 | -0.0231 | 0.3106 | 0.0694 | -0.0094 | 0.0219 | 7 | 6 | 0.0034 | 0.0231 | 18.5 | 19.8 | 0.3213 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0084 | 0.0007 | 0.0604 | 1.0229 | -0.0059 | -0.0248 | 7 | 6 | 0.0240 | 0.0268 | 19.7 | 19.8 | 0.5853 |
| 0 | 2 | -0.0139 | -0.0103 | 0.1008 | 0.0351 | 0.9896 | 0.0078 | 7 | 6 | 0.0118 | 0.0313 | 19.7 | 19.8 | 0.6349 |
| 0 | 3 | -0.0078 | -0.0127 | 0.1494 | 0.0421 | 0.0050 | 1.0090 | 7 | 6 | 0.0279 | 0.0173 | 19.7 | 19.8 | 0.5534 |
| 0 | 4 | -0.0137 | -0.0158 | 0.1830 | -0.9431 | -0.0151 | -0.0251 | 7 | 6 | 0.0111 | 0.0124 | 19.7 | 19.8 | 0.5612 |
| 0 | 5 | 0.0047 | 0.0133 | 0.0262 | 0.0015 | -0.9950 | 0.0003 | 7 | 6 | 0.0097 | 0.0184 | 19.7 | 19.8 | 0.5758 |
| 0 | 6 | 0.0013 | -0.0103 | 0.1862 | 0.0803 | -0.0042 | -1.0087 | 7 | 6 | 0.0158 | 0.0231 | 19.7 | 19.8 | 0.5673 |

## E.3.12 Caudal Rotation: $3^{\circ}$

## -------- Migration Results ------------

Reference Axis: Automatic


Available scenes:
CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative C R 3X1M0R --- X-number: 1 --- Follow-up: Postoperative C R 3X2M0R --- X-number: 2 --- Follow-up: Postoperative C R 3X3M0R --- X-number: 3 --- Follow-up: Postoperative C R 3X4M0R --- X-number: 4 --- Follow-up: Postoperative C R 3X5M0R --- X-number: 5 --- Follow-up: Postoperative C R 3X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0170 | 0.0150 | 0.0324 | 0.0192 | 0.0026 | -0.0043 | 7 | 6 | 0.0135 | 0.0065 | 18.5 | 19.8 | 0.0644 |
| 0 | 2 | -0.0109 | 0.0037 | 0.2080 | 0.0536 | -0.0066 | 0.0162 | 7 | 6 | 0.0192 | 0.0315 | 18.5 | 19.8 | 0.2497 |
| 0 | 3 | -0.0127 | 0.0634 | 0.1064 | 0.0251 | 0.0115 | 0.0020 | 7 | 6 | 0.0229 | 0.0280 | 18.5 | 19.8 | 0.1617 |
| 0 | 4 | -0.0306 | -0.0138 | 0.3659 | 0.0856 | -0.0325 | 0.0298 | 7 | 6 | 0.0164 | 0.0366 | 18.5 | 19.8 | 0.4135 |
| 0 | 5 | -0.0052 | -0.0211 | 0.4238 | 0.0864 | -0.0084 | 0.0076 | 7 | 6 | 0.0041 | 0.0179 | 18.5 | 19.8 | 0.4394 |
| 0 | 6 | -0.0010 | -0.0459 | 0.5564 | 0.1316 | 0.0213 | 0.0010 | 7 | 6 | 0.0217 | 0.0191 | 18.5 | 19.8 | 0.6234 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0012 | 0.0052 | 0.0213 | 3.0136 | -0.0033 | -0.0098 | 7 | 6 | 0.0098 | 0.0065 | 19.7 | 19.8 | 1.7276 |
| 0 | 2 | 0.0034 | 0.0117 | 0.1301 | 0.0265 | -2.9943 | -0.0112 | 7 | 6 | 0.0290 | 0.0315 | 19.7 | 19.8 | 1.7397 |
| 0 | 3 | 0.0024 | 0.0413 | 0.0698 | 0.0096 | -0.0037 | 2.9892 | 7 | 6 | 0.0218 | 0.0280 | 19.7 | 19.8 | 1.5388 |
| 0 | 4 | -0.0119 | 0.0079 | 0.2308 | -2.9579 | -0.0444 | 0.0022 | 7 | 6 | 0.0338 | 0.0366 | 19.7 | 19.8 | 1.7369 |
| 0 | 5 | 0.0052 | -0.0001 | 0.2573 | 0.0950 | 3.0038 | -0.0226 | 7 | 6 | 0.0306 | 0.0179 | 19.7 | 19.8 | 1.8406 |
| 0 | 6 | 0.0028 | -0.0191 | 0.3198 | 0.1158 | 0.0013 | -3.0443 | 7 | 6 | 0.0186 | 0.0191 | 19.7 | 19.8 | 1.5752 |

## E.3.13 Caudal Rotation: $6^{0}$

```
-------- Migration Results
```

Reference Axis: Automatic
Available scenes:
CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative
C R 6X1M0R --- X-number: 1 --- Follow-up: Postoperative
C R 6X2M0R --- X-number: 2 --- Follow-up: Postoperative
C R 6X3M0R --- X-number: 3 --- Follow-up: Postoperative
C R 6X4M0R --- X-number: 4 --- Follow-up: Postoperative
C R 6X5M0R --- X-number: 5 --- Follow-up: Postoperative
C R 6X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0173 | -0.0099 | 0.2219 | 0.0461 | -0.0113 | 0.0088 | 7 | 6 | 0.0189 | 0.0199 | 18.5 | 19.8 | 0.2562 |
| 0 | 2 | -0.0272 | -0.0030 | 0.0986 | 0.0152 | -0.0002 | -0.0094 | 7 | 6 | 0.0175 | 0.0203 | 18.5 | 19.8 | 0.1232 |
| 0 | 3 | 0.0062 | -0.0166 | 0.3737 | 0.0828 | 0.0265 | -0.0157 | 7 | 6 | 0.0262 | 0.0124 | 18.5 | 19.8 | 0.4445 |
| 0 | 4 | -0.0415 | -0.0226 | 0.2695 | 0.0585 | -0.0319 | 0.0260 | 7 | 6 | 0.0214 | 0.0324 | 18.5 | 19.8 | 0.3135 |
| 0 | 5 | -0.0029 | -0.0360 | 0.4104 | 0.0829 | 0.0107 | 0.0145 | 7 | 6 | 0.0242 | 0.0109 | 18.5 | 19.8 | 0.4616 |
| 0 | 6 | -0.0057 | -0.0342 | 0.3364 | 0.0744 | -0.0214 | 0.0223 | 7 | 6 | 0.0213 | 0.0137 | 18.5 | 19.8 | 0.3716 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.0077 | 0.0040 | 0.1366 | 6.0519 | 0.0311 | -0.0545 | 7 | 6 | 0.0429 | 0.0199 | 19.7 | 19.8 | 3.4800 |
| 0 | 2 | -0.5303 | 0.0179 | 0.1293 | 0.0311 | 6.0738 | -0.0073 | 6 | 6 | 0.0840 | 0.0203 | 22.0 | 19.8 | 3.5713 |
| 0 | 3 | -0.0018 | 0.0010 | 0.2340 | 0.0175 | -0.0308 | 6.0028 | 7 | 6 | 0.0466 | 0.0124 | 19.7 | 19.8 | 3.0556 |
| 0 | 4 | -0.0049 | -0.5317 | 0.1797 | -5.9859 | -0.0011 | -0.0198 | 6 | 6 | 0.0129 | 0.0324 | 22.0 | 19.8 | 3.4607 |
| 0 | 5 | -0.0068 | -0.0067 | 0.2155 | 0.0624 | -6.0375 | -0.0078 | 7 | 6 | 0.0485 | 0.0109 | 19.7 | 19.8 | 3.5246 |
| 0 | 6 | 0.0269 | -0.0156 | 0.1830 | 0.0980 | 0.0055 | -6.0167 | 6 | 6 | 0.0185 | 0.0137 | 23.3 | 19.8 | 3.0761 |

## E.3.14 Caudal Rotation: $\mathbf{1 0}^{\circ}$

## -------- Migration Results ------------

Reference Axis: Automatic


Available scenes:
CaudalX0M0R --- X-number: 0 --- Follow-up: Postoperative C R 10X1M0R --- X-number: 1 --- Follow-up: Postoperative C R 10X2M0R --- X-number: 2 --- Follow-up: Postoperative C R 10X3M0R --- X-number: 3 --- Follow-up: Postoperative C R 10X4M0R --- X-number: 4 --- Follow-up: Postoperative C R 10X5M0R --- X-number: 5 --- Follow-up: Postoperative C R 10X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0299 | 0.0164 | 0.2356 | 0.0623 | -0.0218 | 0.0265 | 7 | 6 | 0.0262 | 0.0205 | 18.5 | 19.8 | 0.2792 |
| 0 | 2 | -0.0377 | -0.0497 | 0.3867 | 0.0861 | -0.0237 | 0.0291 | 7 | 6 | 0.0269 | 0.0249 | 18.5 | 19.8 | 0.4312 |
| 0 | 3 | 0.0029 | -0.0381 | 0.3059 | 0.0713 | 0.0072 | 0.0043 | 7 | 6 | 0.0270 | 0.0174 | 18.5 | 19.8 | 0.3524 |
| 0 | 4 | -0.0206 | -0.0229 | 0.2421 | 0.0467 | -0.0309 | 0.0250 | 7 | 6 | 0.0229 | 0.0265 | 18.5 | 19.8 | 0.2796 |
| 0 | 5 | -0.0444 | 0.0082 | 0.1542 | 0.0350 | -0.0351 | 0.0241 | 7 | 6 | 0.0200 | 0.0306 | 18.5 | 19.8 | 0.2014 |
| 0 | 6 | -0.0154 | -0.0068 | 0.0980 | 0.0253 | -0.0251 | 0.0246 | 7 | 6 | 0.0207 | 0.0206 | 18.5 | 19.8 | 0.1361 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: CaudalX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0047 | -0.0061 | 0.1444 | 10.0662 | 0.0105 | -0.0497 | 7 | 6 | 0.0253 | 0.0205 | 19.7 | 19.8 | 5.7999 |
| 0 | 2 | -0.9632 | -0.0256 | 0.3214 | 0.1559 | 10.0106 | -0.0162 | 6 | 6 | 0.0354 | 0.0249 | 23.3 | 19.8 | 5.6302 |
| 0 | 3 | 0.0123 | -0.0809 | 0.1717 | 0.0512 | 0.0100 | 9.9927 | 6 | 6 | 0.0207 | 0.0174 | 22.0 | 19.8 | 5.0786 |
| 0 | 4 | 0.0013 | -0.9031 | 0.1722 | -10.002 | -0.0207 | -0.0165 | 6 | 6 | 0.0768 | 0.0265 | 22.0 | 19.8 | 5.7419 |
| 0 | 5 | -0.2795 | -0.0051 | -0.7482 | 0.0199 | -10.0263 | 0.0553 | 6 | 6 | 0.0516 | 0.0306 | 24.8 | 19.8 | 5.7560 |
| 0 | 6 | 0.0054 | 0.0008 | 0.0381 | 0.0198 | -0.0037 | -10.0196 | 7 | 6 | 0.0239 | 0.0206 | 19.7 | 19.8 | 5.0775 |

## E.3.15 Apex Superior: 0.5mm

## -------- Migration Results ------------

Reference Axis: Automatic
========================================12

Available scenes:

TopX0M0R --- X-number: 0 --- Follow-up: Postoperative
T S 05X1M0R --- X-number: 1 --- Follow-up: Postoperative
T S 05X2M0R --- X-number: 2 --- Follow-up: Postoperative
T S 05X3M0R --- X-number: 3 --- Follow-up: Postoperative
T S 05X4M0R --- X-number: 4 --- Follow-up: Postoperative
T S 05X5M0R --- X-number: 5 --- Follow-up: Postoperative
T S 05X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.5481 | -0.0050 | -0.0771 | -0.0320 | -0.0002 | 0.0057 | 7 | 7 | 0.0588 | 0.0237 | 19.8 | 20.9 | 0.5893 |
| 0 | 2 | 0.0862 | 0.4826 | -0.0336 | -0.0272 | 0.0001 | -0.0655 | 7 | 7 | 0.0407 | 0.0328 | 19.8 | 20.9 | 0.5290 |
| 0 | 3 | 0.0049 | -0.0168 | 0.3915 | -0.0626 | -0.0130 | 0.0285 | 7 | 7 | 0.0379 | 0.0229 | 19.8 | 20.9 | 0.4318 |
| 0 | 4 | -0.4761 | -0.0031 | -0.0706 | -0.0295 | -0.0070 | 0.0135 | 7 | 7 | 0.0224 | 0.0235 | 19.8 | 20.9 | 0.4901 |
| 0 | 5 | -0.1019 | -0.4914 | -0.0452 | 0.0018 | 0.0006 | 0.0854 | 7 | 7 | 0.0475 | 0.0235 | 19.8 | 20.9 | 0.5586 |
| 0 | 6 | -0.0066 | -0.0014 | -0.5483 | 0.0156 | 0.0250 | -0.0339 | 7 | 7 | 0.0394 | 0.0224 | 19.8 | 20.9 | 0.6097 |

## E.3.16 Apex Superior: 1mm

## -------- Migration Results ------------

Reference Axis: Automatic
=======================================
Available scenes:

TopX0MOR --- X-number: 0 --- Follow-up: Postoperative T S 1X1M0R --- X-number: 1 --- Follow-up: Postoperative TS 1X2M0R --- X-number: 2 --- Follow-up: Postoperative TS 1X3M0R --- X-number: 3 --- Follow-up: Postoperative
T S 1X4M0R --- X-number: 4 --- Follow-up: Postoperative TS 1X5M0R --- X-number: 5 --- Follow-up: Postoperative
T S 1X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number |  | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 1.0937 | -0.0333 | 0.0193 | -0.0025 | -0.0090 | -0.0405 | 7 | 7 | 0.0325 | 0.0248 | 19.8 | 20.9 | 1.1118 |
| 0 | 2 | -0.0619 | 0.9991 | -0.0179 | -0.0107 | -0.0150 | 0.0428 | 7 | 7 | 0.0437 | 0.0245 | 19.8 | 20.9 | 1.0312 |
| 0 | 3 | 0.0371 | -0.0047 | 0.9519 | 0.0236 | -0.0560 | 0.0081 | 7 | 7 | 0.0885 | 0.0235 | 19.8 | 20.9 | 1.1327 |
| 0 | 4 | -0.9808 | -0.0073 | -0.0759 | -0.0267 | -0.0060 | 0.0327 | 7 | 7 | 0.0693 | 0.0235 | 19.8 | 20.9 | 1.0440 |
| 0 | 5 | -0.0495 | -0.9961 | -0.0235 | 0.0082 | -0.0420 | 0.0714 | 7 | 7 | 0.0260 | 0.0253 | 19.8 | 20.9 | 1.0320 |
| 0 | 6 | -0.0946 | -0.0047 | -0.9953 | 0.0274 | -0.0320 | 0.0420 | 7 | 7 | 0.0357 | 0.0393 | 19.8 | 20.9 | 1.0574 |

## E.3.17 Apex Superior: 5mm

## -------- Migration Results -----------

Reference Axis: Automatic


Available scenes:
TopX0MOR --- X-number: 0 --- Follow-up: Postoperative T S 5X1M0R --- X-number: 1 --- Follow-up: Postoperative T S 5X2M0R --- X-number: 2 --- Follow-up: Postoperative TS 5X3M0R --- X-number: 3 --- Follow-up: Postoperative
T S 5X4M0R --- X-number: 4 --- Follow-up: Postoperative T S 5X5M0R --- X-number: 5 --- Follow-up: Postoperative
T S 5X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number |  | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 4.9426 | 0.0165 | -0.0463 | 0.0027 | -0.0210 | 0.0546 | 7 | 7 | 0.0612 | 0.0253 | 19.8 | 20.9 | 5.0044 |
| 0 | 2 | 0.0179 | 4.9853 | -0.0723 | -0.0091 | -0.0140 | 0.0076 | 7 | 7 | 0.0309 | 0.0337 | 19.8 | 20.9 | 5.0063 |
| 0 | 3 | 0.0107 | -0.0029 | 4.9133 | -0.0176 | 0.0240 | 0.0433 | 7 | 7 | 0.0991 | 0.0235 | 19.8 | 20.9 | 5.0106 |
| 0 | 4 | -4.9686 | -0.0139 | -0.0415 | 0.0028 | -0.0170 | -0.0089 | 7 | 7 | 0.0641 | 0.0234 | 19.8 | 20.9 | 4.9935 |
| 0 | 5 | 0.0193 | -5.0086 | -0.0709 | -0.0027 | -0.0001 | 0.0103 | 7 | 7 | 0.0441 | 0.0235 | 19.8 | 20.9 | 5.0396 |
| 0 | 6 | 0.0340 | -0.0212 | -5.0707 | -0.0060 | 0.0146 | 0.0104 | 7 | 7 | 0.0382 | 0.0235 | 19.8 | 20.9 | 5.1207 |

## E.3.18 Apex Superior: 10mm

## -------- Migration Results ------------

Reference Axis: Automatic
======================================

Available scenes:
TopX0MOR --- X-number: 0 --- Follow-up: Postoperative
TS 10X1M0R --- X-number: 1 --- Follow-up: Postoperative
T S 10X2M0R --- X-number: 2 --- Follow-up: Postoperative
TS 10X3M0R --- X-number: 3 --- Follow-up: Postoperative
T S 10X4M0R --- X-number: 4 --- Follow-up: Postoperative
TS 10X5M0R --- X-number: 5 --- Follow-up: Postoperative
T S 10X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number | Condition <br> Reference Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 10.0617 | 0.0005 | -0.0684 | 0.0153 | 0.0029 | 0.0081 | 7 | 7 | 0.0583 | 0.0230 | 19.8 | 20.9 | 10.1266 |
| 0 | 2 | -0.0848 | 9.9959 | 0.0298 | 0.0165 | -0.0338 | 0.0269 | 7 | 7 | 0.0359 | 0.0303 | 19.8 | 20.9 | 10.0322 |
| 0 | 3 | 0.0115 | -0.0074 | 10.0433 | 0.0660 | -0.0409 | 0.0082 | 7 | 7 | 0.0467 | 0.0292 | 19.8 | 20.9 | 10.0945 |
| 0 | 4 | -10.0206 | 0.0100 | -0.0644 | 0.0069 | 0.0032 | 0.0000 | 7 | 7 | 0.0611 | 0.0262 | 19.8 | 20.9 | 10.0452 |
| 0 | 5 | 0.0068 | -10.0049 | -0.0323 | -0.0384 | -0.0214 | 0.0453 | 7 | 7 | 0.0427 | 0.0258 | 19.8 | 20.9 | 10.0491 |
| 0 | 6 | 0.0889 | -0.0069 | -10.053 | -0.0085 | 0.0088 | -0.0230 | 7 | 7 | 0.0654 | 0.0253 | 19.8 | 20.9 | 10.1951 |

## E.3.19 Apex Superior: 20mm

## -------- Migration Results ------------

Reference Axis: Automatic
============================================

Available scenes:

TopX0M0R --- X-number: 0 --- Follow-up: Postoperative
T S 20X1M0R --- X-number: 1 --- Follow-up: Postoperative
T S 20X2M0R --- X-number: 2 --- Follow-up: Postoperative
T S 20X3M0R --- X-number: 3 --- Follow-up: Postoperative
T S 20X4M0R --- X-number: 4 --- Follow-up: Postoperative
T S 20X5M0R --- X-number: 5 --- Follow-up: Postoperative
T S 20X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid Body Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 20.0293 | -0.0089 | -0.0500 | 0.0097 | -0.0540 | 0.0288 | 7 | 7 | 0.0662 | 0.0231 | 19.8 | 20.9 | 20.0898 |
| 0 | 2 | 0.1158 | 20.0047 | -0.0345 | 0.0273 | -0.0440 | 0.0112 | 7 | 7 | 0.0570 | 0.0208 | 19.8 | 20.9 | 20.0852 |
| 0 | 3 | 0.0138 | -0.0031 | 19.9065 | -0.0299 | -0.0110 | 0.0551 | 7 | 7 | 0.0304 | 0.0237 | 19.8 | 20.9 | 19.9668 |
| 0 | 4 | -19.9879 | -0.0111 | -0.1093 | -0.0525 | 0.0150 | 0.0403 | 7 | 7 | 0.0499 | 0.0236 | 19.8 | 20.9 | 20.0480 |
| 0 | 5 | 0.0135 | -20.0114 | -0.0670 | -0.0157 | -0.0080 | -0.0058 | 7 | 7 | 0.0386 | 0.0239 | 19.8 | 20.9 | 20.0417 |
| 0 | 6 | 0.1003 | -0.0246 | -20.0465 | 0.0050 | 0.0104 | -0.0438 | 7 | 7 | 0.0577 | 0.0223 | 19.8 | 20.9 | 20.1187 |

## E.3.20 Apex Inferior: 0.5mm

## -------- Migration Results -----------

Reference Axis: Automatic
=========================================

## Available scenes:

BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B I 05X1M0R --- X-number: 1 --- Follow-up: Postoperative B I 05X2M0R --- X-number: 2 --- Follow-up: Postoperative B I 05X3M0R --- X-number: 3 --- Follow-up: Postoperative B I 05X4M0R --- X-number: 4 --- Follow-up: Postoperative B I 05X5M0R --- X-number: 5 --- Follow-up: Postoperative B I 05X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: BottomX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.3202 | 0.0180 | -0.1410 | 0.0585 | 0.0531 | 0.0593 | 6 | 7 | 0.0046 | 0.0448 | 20.2 | 20.0 | 0.3782 |
| 0 | 2 | -0.0004 | -0.5019 | -0.0072 | -0.0130 | -0.0080 | 0.0016 | 6 | 7 | 0.0100 | 0.0265 | 20.2 | 20.0 | 0.5039 |
| 0 | 3 | 0.0109 | 0.0254 | -0.4686 | -0.0800 | -0.0320 | 0.0105 | 6 | 7 | 0.0108 | 0.0244 | 20.2 | 20.0 | 0.4808 |
| 0 | 4 | 0.4822 | 0.0025 | -0.0258 | -0.0312 | -0.0140 | -0.0014 | 6 | 7 | 0.0186 | 0.0339 | 20.2 | 20.0 | 0.4896 |
| 0 | 5 | 0.0061 | 0.5101 | -0.0817 | -0.0080 | 0.0015 | 0.0033 | 6 | 7 | 0.0069 | 0.0208 | 20.2 | 20.0 | 0.5262 |
| 0 | 6 | -0.2275 | -0.0037 | 0.5599 | -0.0770 | 0.0337 | -0.0841 | 6 | 7 | 0.0160 | 0.0273 | 20.2 | 20.0 | 0.6357 |

## E.3.21 Apex Inferior: 1mm



M0R --- X-number: 6 --- Follow-up: Postoperative

Xref Xmig X Y

## Model: L1

Reference: BottomX0M0R --- T8

| 0 | 1 | -0.9248 | 0.0209 | -0.0165 | -0.0623 | 0.0446 | 0.0241 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 2 | -0.0213 | -0.9931 | -0.0105 | -0.0286 | 0.0228 | -0.0099 |
| 0 | 3 | 0.0422 | 0.0169 | -0.9698 | -0.0751 | 0.0019 | 0.0155 |
| 0 | 4 | 1.0194 | 0.0084 | -0.0237 | -0.0307 | 0.0131 | 0.0099 |
| 0 | 5 | -0.0509 | 0.9951 | 0.1007 | -0.0537 | 0.0225 | -0.0187 |
| 0 | 6 | 0.0250 | 0.0287 | 1.0540 | -0.0867 | -0.0100 | 0.0149 |


|  |  |  | Rigid |  | Condition | Maximum |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | \#Matched | Rigid | Body |  | Number | Total |
| \#Matched | Reference | Body | Error | Condition | Reference | Point |
| Markers | Markers | Error | Reference | Number | Model | Motion |

## E.3.22 Apex Inferior: 5mm

-------- Migration Results -------------
Reference Axis: Automatic
$==================================$
Available scenes:
---------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B I 5X1M0R --- X-number: 1 --- Follow-up: Postoperative
B I 5X2M0R --- X-number: 2 -- Follow-up: Postoperative
B I 5X3M0R --- X-number: 3 -- Follow-up: Postoperative
B I 5X4M0R --- X-number: 4 -- Follow-up: Postoperative
B I 5X5M0R --- X-number: 5 --- Follow-up: Postoperative
B I 5X6M0R --- X-number: 6 --- Follow-up: Postoperative

Condition | Maximum |
| :---: |
| Total |

## E.3.23 Apex Inferior: 10mm

-------- Migration Results -------------
Reference Axis: Automatic
$==================================$
Available scenes:
-------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B I 10X1M0R --- X-number: 1 --- Follow-up: Postoperative
B I 10X2M0R --- X-number: 2 --- Follow-up: Postoperative
B I 10X3M0R --- X-number: 3 --- Follow-up: Postoperative
B I 10X4M0R --- X-number: 4 --- Follow-up: Postoperative
B I 10X5M0R --- X-number: 5 --- Follow-up: Postoperative
B I 10X6M0R --- X-number: 6 --- Follow-up: Postoperative

B I 10X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: BottomX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -10.0948 | 0.0006 | 0.0722 | -0.0745 | 0.0014 | -0.0423 | 6 | 7 | 0.0229 | 0.0339 | 20.2 | 20 | 10.1261 |
| 0 | 2 | 0.1132 | -9.9891 | -0.1226 | -0.0146 | -0.0069 | 0.0346 | 6 | 7 | 0.0082 | 0.0628 | 20.2 | 20 | 10.0158 |
| 0 | 3 | -0.0265 | -0.0023 | -10.0040 | -0.0288 | 0.0013 | -0.0107 | 6 | 7 | 0.0093 | 0.0385 | 20.2 | 20 | 10.0143 |
| 0 | 4 | 10.0113 | 0.0141 | 0.0543 | -0.0522 | -0.0068 | 0.0066 | 6 | 7 | 0.0061 | 0.0494 | 20.2 | 20 | 10.0152 |
| 0 | 5 | -0.0221 | 10.0275 | 0.1554 | -0.1558 | 0.0150 | -0.0089 | 6 | 7 | 0.0254 | 0.0705 | 20.2 | 20 | 10.1611 |
| 0 | 6 | -0.0139 | 0.0019 | 10.0618 | -0.0570 | 0.0020 | -0.0150 | 6 | 7 | 0.0274 | 0.0390 | 20.2 | 20 | 10.1044 |

## E.3.24 Apex Inferior: 20mm

-------- Migration Results ------------
Reference Axis: Automatic
$=====================================$
Available scenes:
--------------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B I 20X1M0R --- X-number: 1 --- Follow-up: Postoperative
B I 20X2M0R --- X-number: 2 --- Follow-up: Postoperative
B I 20X3M0R --- X-number: 3 --- Follow-up: Postoperative
B I 20X4M0R --- X-number: 4 --- Follow-up: Postoperative
B I 20X5M0R --- X-number: 5 --- Follow-up: Postoperative
B I 20X6M0R --- X-number: 6 --- Follow-up: Postoperative
Xref Xmig X Y

## Model: L1

Reference: BottomX0M0R --- T8

|  |  |  |  |  |  |  |  |
| :--- | :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 1 | -19.9985 | 0.0128 | 0.0811 | -0.0851 | 0.0129 | 0.0036 |
| 0 | 2 | 0.1417 | -19.9824 | -0.1734 | -0.0074 | -0.0060 | 0.0475 |
| 0 | 3 | -0.0906 | -0.0011 | -19.9130 | -0.0911 | -0.0260 | -0.0253 |
| 0 | 4 | 20.0738 | 0.0365 | -0.0135 | -0.0536 | -0.0260 | 0.0327 |
| 0 | 5 | -0.0546 | 20.0149 | 0.0965 | -0.0897 | -0.0370 | -0.0126 |
| 0 | 6 | 0.0747 | 0.0079 | 19.9173 | -0.0377 | -0.0060 | 0.0304 |


| \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body <br> Error | Rigid <br> Body <br> Error <br> Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6 | 7 | 0.0110 | 0.0409 | 20.2 | 20.0 | 20.0048 |
| 6 | 7 | 0.0099 | 0.0183 | 20.2 | 20.0 | 20.0136 |
| 6 | 7 | 0.0193 | 0.0520 | 20.2 | 20.0 | 19.9193 |
| 6 | 7 | 0.0208 | 0.0261 | 20.2 | 20.0 | 20.0866 |
| 6 | 7 | 0.0304 | 0.0376 | 20.2 | 20.0 | 20.0990 |
| 6 | 7 | 0.0131 | 0.0351 | 20.2 | 20.0 | 19.9267 |

## E.3.25 Apex Rotation Superior: $\mathbf{1 0}^{0}$

## -------- Migration Results ------------

Reference Axis: Automatic
======================================12

Available scenes:
TopX0MOR --- X-number: 0 --- Follow-up: Postoperative T R 1X1M0R --- X-number: 1 --- Follow-up: Postoperative T R 1X2M0R --- X-number: 2 --- Follow-up: Postoperative T R 1X3M0R --- X-number: 3 --- Follow-up: Postoperative TR 1X4M0R --- X-number: 4 --- Follow-up: Postoperative TR 1X5M0R --- X-number: 5 --- Follow-up: Postoperative T R 1X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error |  | Condition Number |  | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.0388 | -0.0191 | 0.0102 | -1.0193 | -0.0330 | 0.0462 | 7 | 7 | 0.0280 | 0.0319 | 19.8 | 20.9 | 2.2510 |
| 0 | 2 | 0.0875 | -0.0300 | 0.0116 | -0.0396 | -0.9830 | -0.0257 | 7 | 7 | 0.0395 | 0.0281 | 19.8 | 20.9 | 0.7542 |
| 0 | 3 | -0.0593 | -0.0092 | 0.0237 | -0.0201 | -0.0130 | -1.0203 | 7 | 7 | 0.0404 | 0.0365 | 19.8 | 20.9 | 2.1602 |
| 0 | 4 | 0.0126 | -0.0212 | 0.0451 | 0.9722 | 0.0149 | 0.0318 | 7 | 7 | 0.0524 | 0.0334 | 19.8 | 20.9 | 2.1546 |
| 0 | 5 | 0.0058 | -0.0105 | -0.0094 | -0.0561 | 1.0357 | -0.0394 | 7 | 7 | 0.0617 | 0.0276 | 19.8 | 20.9 | 1.0446 |
| 0 | 6 | 0.0413 | -0.0302 | 0.0172 | -0.0396 | -0.0110 | 1.0229 | 7 | 7 | 0.0586 | 0.0307 | 19.8 | 20.9 | 2.1884 |

## E.3.26 Apex Rotation Inferior: $\mathbf{1 0}^{0}$

-------- Migration Results -------------
Reference Axis: Automatic
======================================
Available scenes:
----------------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B R 1X1M0R --- X-number: 1 --- Follow-up: Postoperative
B R 1X2M0R --- X-number: 2 --- Follow-up: Postoperative
B R 1X3M0R --- X-number: 3 --- Follow-up: Postoperative
B R 1X4M0R --- X-number: 4 --- Follow-up: Postoperative
B R 1X5M0R --- X-number: 5 --- Follow-up: Postoperative
B R 1X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition Number Reference Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: BottomX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0177 | 0.0181 | -0.2616 | -1.1569 | -0.0400 | -0.0139 | 6 | 7 | 0.0083 | 0.0484 | 20.2 | 20.0 | 3.2114 |
| 0 | 2 | 0.0095 | 0.0226 | -0.1444 | -0.0775 | -1.0010 | -0.0186 | 6 | 7 | 0.0294 | 0.0338 | 20.2 | 20.0 | 0.8872 |
| 0 | 3 | -0.0092 | 0.0196 | -0.1545 | -0.0781 | -0.0150 | -0.9408 | 6 | 7 | 0.0041 | 0.0378 | 20.2 | 20.0 | 2.8346 |
| 0 | 4 | -0.0198 | 0.0165 | -0.1682 | 0.9366 | -0.0190 | 0.0604 | 6 | 7 | 0.0213 | 0.0324 | 20.2 | 20.0 | 3.0091 |
| 0 | 5 | -0.0154 | 0.0120 | -0.2521 | -0.0830 | 0.9893 | -0.0083 | 6 | 7 | 0.0083 | 0.0445 | 20.2 | 20.0 | 0.8182 |
| 0 | 6 | -0.0173 | 0.0084 | -0.2283 | -0.0683 | -0.0380 | 0.9608 | 6 | 7 | 0.0240 | 0.0400 | 20.2 | 20.0 | 2.8788 |

## E.3.27 Apex Rotation Superior: $\mathbf{3 o}^{\text {o }}$

-------- Migration Results ------------

## Reference Axis: Automatic

Available scenes
TopX0M0R --- X-number: 0 --- Follow-up: Postoperative T R 3X1M0R --- X-number: 1 --- Follow-up: Postoperative T R 3X2M0R --- X-number: 2 --- Follow-up: Postoperative T R 3X3M0R --- X-number: 3 --- Follow-up: Postoperative TR 3X4MOR --- X-number: 4 --- Follow-up: Postoperative TR 3X5M0R --- X-number: 5 --- Follow-up: Postoperative T R 3X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body <br> Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.0154 | -0.0380 | 0.0171 | -3.0643 | -0.0040 | 0.0044 | 7 | 7 | 0.0627 | 0.0456 | 19.8 | 20.9 | 6.6797 |
| 0 | 2 | 0.0061 | -0.0130 | -0.0171 | -0.0068 | 2.9733 | 0.0548 | 7 | 7 | 0.0481 | 0.0513 | 19.8 | 20.9 | 2.6209 |
| 0 | 3 | 0.0653 | -0.0320 | 0.0076 | -0.0448 | -0.0250 | -2.9504 | 7 | 7 | 0.0443 | 0.0363 | 19.8 | 20.9 | 6.4816 |
| 0 | 4 | -0.0105 | -0.0289 | 0.0261 | 2.9739 | 0.0054 | -0.0407 | 7 | 7 | 0.0251 | 0.0376 | 19.8 | 20.9 | 6.4884 |
| 0 | 5 | 0.0426 | -0.0231 | 0.0249 | -0.0410 | -2.9910 | -0.0218 | 7 | 7 | 0.0604 | 0.0231 | 19.8 | 20.9 | 2.6280 |
| 0 | 6 | 0.1222 | -0.0327 | 0.0253 | -0.0358 | 0.0092 | 2.9887 | 7 | 7 | 0.0584 | 0.0401 | 19.8 | 20.9 | 6.4027 |

## E.3.28 Apex Rotation Inferior: $3^{\circ}$

-------- Migration Results -------------
Reference Axis: Automatic
======================================
Available scenes:
-----------------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B R 3X1M0R --- X-number: 1 --- Follow-up: Postoperative
B R 3X2M0R --- X-number: 2 --- Follow-up: Postoperative
B R 3X3M0R --- X-number: 3 --- Follow-up: Postoperative
B R 3X4M0R --- X-number: 4 --- Follow-up: Postoperative
B R 3X5M0R --- X-number: 5 --- Follow-up: Postoperative
B R 3X6M0R --- X-number: 6 --- Follow-up: Postoperative
B
Xref Xmig X

Model: L1
Reference: BottomX0M0R --- T8

| 0 | 1 | -0.0140 | 0.0042 | -0.1597 | -3.0925 | -0.0620 | -0.0550 | 6 | 7 | 0.0086 | 0.0504 | 20.2 | 20.0 | 9.1602 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 2 | -0.0190 | 0.0157 | -0.1812 | -0.0439 | 2.9917 | 0.0278 | 6 | 7 | 0.0079 | 0.0373 | 20.2 | 20.0 | 2.6207 |
| 0 | 3 | -0.0378 | 0.0324 | -0.2780 | -0.1095 | -0.0500 | -2.8801 | 6 | 7 | 0.0474 | 0.0394 | 20.2 | 20.0 | 8.6847 |
| 0 | 4 | -0.0243 | 0.0371 | -0.0946 | 2.9513 | -0.1500 | 0.1371 | 6 | 6 | 0.0112 | 0.0765 | 20.2 | 21.9 | 8.9658 |
| 0 | 5 | -0.0319 | 0.0047 | -0.0505 | -0.0238 | -3.0960 | 0.0039 | 6 | 7 | 0.0625 | 0.0587 | 20.2 | 20.0 | 2.7038 |
| 0 | 6 | -0.0100 | 0.0006 | -0.2443 | -0.1084 | -0.0220 | 2.8758 | 6 | 7 | 0.0046 | 0.0545 | 20.2 | 20.0 | 8.6373 |

## E.3.29 Apex Rotation Superior: $6^{0}$

## -------- Migration Results -----------

Reference Axis: Automatic
==========================================

## Available scenes:

TopX0M0R --- X-number: 0 --- Follow-up: Postoperative T R 6X1M0R --- X-number: 1 --- Follow-up: Postoperative T R 6X2M0R --- X-number: 2 --- Follow-up: Postoperative T R 6X3M0R --- X-number: 3 --- Follow-up: Postoperative T R 6X4M0R --- X-number: 4 --- Follow-up: Postoperative T R 6X5M0R --- X-number: 5 --- Follow-up: Postoperative T R 6X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid Body Error | Rigid <br> Body <br> Error <br> Reference | Condition Number | Condition <br> Number <br> Reference Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0221 | 0.0027 | -0.0030 | -5.9829 | 0.0052 | 0.0427 | 7 | 7 | 0.0613 | 0.0284 | 19.8 | 20.9 | 12.9746 |
| 0 | 2 | 0.0396 | -0.0113 | -0.0572 | -0.0397 | -5.9900 | -0.0615 | 7 | 6 | 0.0373 | 0.0654 | 19.8 | 22.7 | 5.2681 |
| 0 | 3 | -0.0222 | -0.0022 | -0.0460 | -0.0016 | -0.0020 | -6.0215 | 7 | 7 | 0.0264 | 0.0448 | 19.8 | 20.9 | 13.0851 |
| 0 | 4 | 0.0144 | -0.0211 | 0.0044 | 5.9843 | 0.0223 | -0.0038 | 7 | 7 | 0.0482 | 0.0441 | 19.8 | 20.9 | 13.0334 |
| 0 | 5 | -0.0205 | -0.0153 | -0.0690 | -0.0469 | 6.1091 | -0.0567 | 7 | 7 | 0.0675 | 0.1407 | 19.8 | 20.9 | 5.6837 |
| 0 | 6 | -0.0119 | -0.0264 | 0.0216 | -0.0330 | 0.0288 | 5.9829 | 7 | 7 | 0.0292 | 0.0272 | 19.8 | 20.9 | 13.0119 |

## E.3.30 Apex Rotation Inferior: $6^{0}$

-------- Migration Results ------------
Reference Axis: Automatic
======================================
Available scenes:
-----------------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B R 6X1M0R --- X-number: 1 --- Follow-up: Postoperative
B R 6X2M0R --- X-number: 2 --- Follow-up: Postoperative
B R 6X3M0R --- X-number: 3 --- Follow-up: Postoperative
B R 6X4M0R --- X-number: 4 --- Follow-up: Postoperative
B R 6X5M0R --- X-number: 5 --- Follow-up: Postoperative
B R 6X6M0R --- X-number: 6 --- Follow-up: Postoperative
R----- Xor

| Xref | Xmig | $X$ | $Y$ | $Z$ | $R x$ |
| :--- | :--- | :--- | :--- | :--- | :--- |

## Model: L1

Reference: BottomX0M0R --- T8

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 1 | -0.0216 | 0.0175 | -0.0315 | -6.0302 | -0.0250 | 0.0268 | 6 | 7 | 0.0159 | 0.0502 | 20.2 | 20.0 |
| 0 | 2 | -0.0008 | 0.0085 | -0.1033 | -0.0045 | -6.1180 | 0.1308 | 6 | 5 | 0.0246 | 0.0710 | 20.2 | 26.2 |
| 0 | 3 | -0.0086 | 0.0304 | -0.1855 | -0.0340 | 0.0001 | -5.9309 | 6 | 6 | 0.0229 | 0.0620 | 20.2 | 21.9 |
| 0 | 4 | -0.0518 | 0.0713 | -0.2443 | 5.9096 | -0.0960 | 0.0675 | 17.8341 |  |  |  |  |  |
| 0 | 5 | -0.0572 | 0.0277 | -0.2980 | -0.1361 | 5.9683 | 0.0064 | 6 | 6 | 0.0378 | 0.0427 | 20.2 | 21.9 |
| 0 | 6 | -0.0127 | 0.0119 | -0.1676 | -0.0989 | -0.0300 | 5.9876 | 6 | 7 | 0.0396 | 0.0791 | 20.2 | 20.0 |
| 4 | 4.9872 |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 7 | 0.0158 | 0.0658 | 20.2 | 20.0 | 17.9886 |  |

## E.3.31 Apex Rotation Superior: $\mathbf{1 0}^{\circ}$

## -------- Migration Results -----------

Reference Axis: Automatic
=======================================

Available scenes:
TopX0M0R --- X-number: 0 --- Follow-up: Postoperative
T R 10X1M0R --- X-number: 1 --- Follow-up: Postoperative T R 10X2M0R --- X-number: 2 --- Follow-up: Postoperative T R 10X3M0R --- X-number: 3 --- Follow-up: Postoperative T R 10X4M0R --- X-number: 4 --- Follow-up: Postoperative T R 10X5M0R --- X-number: 5 --- Follow-up: Postoperative
T R 10X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid Body Error | Rigid Body Error Reference | Condition Number | Condition Number Reference Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.0088 | 0.0172 | 0.0087 | -9.9811 | 0.0362 | 0.0188 | 7 | 7 | 0.1044 | 0.0481 | 19.8 | 20.9 | 21.6566 |
| 0 | 2 | 0.0216 | -0.0066 | -0.0295 | 0.0113 | -9.9799 | 0.0359 | 7 | 7 | 0.0429 | 0.1031 | 19.8 | 20.9 | 9.1124 |
| 0 | 3 | -0.0007 | -0.0273 | 0.0051 | -0.0293 | -0.0252 | -10.022 | 7 | 7 | 0.0427 | 0.0609 | 19.8 | 20.9 | 21.7636 |
| 0 | 4 | -0.0119 | 0.0087 | -0.0133 | 9.9711 | 0.0020 | 0.0742 | 7 | 6 | 0.0731 | 0.0513 | 19.8 | 22.7 | 21.6711 |
| 0 | 5 | -0.0318 | 0.0178 | 0.0033 | -0.0322 | 10.1029 | 0.0111 | 7 | 6 | 0.0479 | 0.0601 | 19.8 | 28.2 | 9.1217 |
| 0 | 6 | 0.0052 | -0.0217 | 0.0179 | -0.0340 | 0.0404 | 9.9879 | 7 | 7 | 0.0628 | 0.0358 | 19.8 | 20.9 | 21.7007 |

## E.3.32 Apex Rotation Inferior: $\mathbf{1 0}^{\circ}$

-------- Migration Results ------------
Reference Axis: Automatic
$=====================================$
Available scenes:
-----------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B R 10X1M0R --- X-number: 1 --- Follow-up: Postoperative
B R 10X2M0R --- X-number: 2 --- Follow-up: Postoperative
B R 10X3M0R --- X-number: 3 --- Follow-up: Postoperative
B R 10X4M0R --- X-number: 4 --- Follow-up: Postoperative
B R 10X5M0R --- X-number: 5 --- Follow-up: Postoperative
B R 10X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid Body Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition Number Reference Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: BottomX0M0R --- T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0190 | -0.0108 | -0.1963 | -10.1030 | -0.0200 | 0.0175 | 6 | 7 | 0.0052 | 0.0398 | 20.2 | 20.0 | 30.1799 |
| 0 | 2 | -0.0016 | 0.04671 | -0.1588 | -0.1147 | -10.0090 | 0.0444 | 6 | 7 | 0.0300 | 0.1471 | 20.2 | 20.0 | 8.4601 |
| 0 | 3 | -0.0067 | 0.04429 | -0.2915 | -0.1065 | 0.0112 | -9.8970 | 6 | 6 | 0.0395 | 0.0488 | 20.2 | 21.9 | 29.7324 |
| 0 | 4 | -0.0599 | 0.07876 | -0.2741 | 9.8710 | -0.1694 | 0.0399 | 6 | 6 | 0.0052 | 0.2043 | 20.2 | 21.9 | 29.9482 |
| 0 | 5 | -0.0413 | 0.02217 | -0.1459 | -0.1470 | 10.1016 | 0.1315 | 6 | 6 | 0.0057 | 0.1637 | 20.2 | 26.0 | 8.7817 |
| 0 | 6 | -0.0083 | 0.03130 | -0.3592 | -0.1693 | -0.0475 | 10.0333 | 6 | 7 | 0.0444 | 0.0528 | 20.2 | 20.0 | 30.1305 |

## E.3.33 Dual Superior: 0.5mm

## -------- Migration Results ------------

Reference Axis: Automatic
=======================================

## Available scenes:

TopX0M0R --- X-number: 0 --- Follow-up: Postoperative
T S 05X1M0R --- X-number: 1 --- Follow-up: Postoperative T S 05X2M0R --- X-number: 2 --- Follow-up: Postoperative T S 05X3M0R --- X-number: 3 --- Follow-up: Postoperative T S 05X4M0R --- X-number: 4 --- Follow-up: Postoperative T S 05X5M0R --- X-number: 5 --- Follow-up: Postoperative
T S 05X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid Body Error | Rigid <br> Body <br> Error <br> Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.5594 | 0.0175 | 0.0138 | 0.0320 | 0.0002 | -0.0057 | 7 | 7 | 0.0237 | 0.0588 | 20.9 | 19.8 | 0.5834 |
| 0 | 2 | 0.0440 | -0.4908 | -0.0204 | 0.0272 | -0.0001 | 0.0655 | 7 | 7 | 0.0328 | 0.0407 | 20.9 | 19.8 | 0.5316 |
| 0 | 3 | -0.0657 | 0.0463 | -0.5120 | 0.0626 | 0.0124 | -0.0286 | 7 | 7 | 0.0229 | 0.0379 | 20.9 | 19.8 | 0.5372 |
| 0 | 4 | 0.4470 | 0.0166 | 0.0141 | 0.0295 | 0.0072 | -0.0135 | 7 | 7 | 0.0235 | 0.0224 | 20.9 | 19.8 | 0.4750 |
| 0 | 5 | -0.0662 | 0.5135 | 0.0486 | -0.0018 | -0.0006 | -0.0854 | 7 | 7 | 0.0235 | 0.0475 | 20.9 | 19.8 | 0.5740 |
| 0 | 6 | 0.0819 | -0.0128 | 0.5724 | -0.0155 | -0.0250 | 0.0338 | 7 | 7 | 0.0224 | 0.0394 | 20.9 | 19.8 | 0.6109 |

## E.3.34 Dual Superior: 1mm

## -------- Migration Results -----------

Reference Axis: Automatic


Available scenes:
TopXOMOR --- X-number: 0 --- Follow-up: Postoperative
T S 1X1M0R --- X-number: 1 --- Follow-up: Postoperative
TS 1X2M0R --- X-number: 2 --- Follow-up: Postoperative
TS 1X3M0R --- X-number: 3 --- Follow-up: Postoperative
TS 1X4M0R --- X-number: 4 --- Follow-up: Postoperative
TS 1X5M0R --- X-number: 5 --- Follow-up: Postoperative
T S 1X6M0R --- X-number: 6 --- Follow-up: Postoperative

Condition | Maximum |
| :---: |
| Total |

## E.3.35 Dual Superior: 5mm

## -------- Migration Results -----------

Reference Axis: Automatic
=======================================
Available scenes:

TopXOMOR --- X-number: 0 --- Follow-up: Postoperative
T S 5X1M0R --- X-number: 1 --- Follow-up: Postoperative
T S 5X2M0R --- X-number: 2 --- Follow-up: Postoperative
TS 5X3M0R --- X-number: 3 --- Follow-up: Postoperative
TS 5X4M0R --- X-number: 4 --- Follow-up: Postoperative
T S 5X5M0R --- X-number: 5 --- Follow-up: Postoperative
T S 5X6M0R --- X-number: 6 --- Follow-up: Postoperative
(

## E.3.36 Dual Superior: 10mm

## -------- Migration Results ------------

Reference Axis: Automatic
=======================================

Available scenes:
TopX0MOR --- X-number: 0 --- Follow-up: Postoperative
T S 10X1M0R --- X-number: 1 --- Follow-up: Postoperative TS 10X2M0R --- X-number: 2 --- Follow-up: Postoperative TS 10X3M0R --- X-number: 3 --- Follow-up: Postoperative T S 10X4M0R --- X-number: 4 --- Follow-up: Postoperative TS 10X5M0R --- X-number: 5 --- Follow-up: Postoperative
TS 10X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid <br> Body <br> Error <br> Reference | Condition Number | Condition Number Reference Model | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -10.0768 | -0.0022 | 0.0973 | -0.0153 | -0.0029 | -0.0081 | 7 | 7 | 0.0230 | 0.0583 | 20.9 | 19.8 | 10.0963 |
| 0 | 2 | 0.0153 | -9.9944 | 0.0146 | -0.0165 | 0.0338 | -0.0269 | 7 | 7 | 0.0303 | 0.0359 | 20.9 | 19.8 | 10.0297 |
| 0 | 3 | -0.0488 | -0.0244 | -9.9018 | -0.0660 | 0.0409 | -0.0081 | 7 | 7 | 0.0292 | 0.0467 | 20.9 | 19.8 | 9.9498 |
| 0 | 4 | 10.0215 | -0.0123 | 0.0777 | -0.0069 | -0.0032 | 0.0000 | 7 | 7 | 0.0262 | 0.0611 | 20.9 | 19.8 | 10.0444 |
| 0 | 5 | -0.0958 | 10.0301 | -0.0313 | 0.0384 | 0.0214 | -0.0453 | 7 | 7 | 0.0258 | 0.0427 | 20.9 | 19.8 | 10.0866 |
| 0 | 6 | -0.0419 | 0.0022 | 10.0338 | 0.0085 | -0.0088 | 0.0230 | 7 | 7 | 0.0253 | 0.0654 | 20.9 | 19.8 | 10.0646 |

## E.3.37 Dual Superior: 20mm

## -------- Migration Results -----------

Reference Axis: Automatic
=======================================

Available scenes:

TopX0M0R --- X-number: 0 --- Follow-up: Postoperative
T S 20X1M0R --- X-number: 1 --- Follow-up: Postoperative
T S 20X2M0R --- X-number: 2 --- Follow-up: Postoperative
T S 20X3M0R --- X-number: 3 --- Follow-up: Postoperative
T S 20X4M0R --- X-number: 4 --- Follow-up: Postoperative
T S 20X5M0R --- X-number: 5 --- Follow-up: Postoperative
T S 20X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -20.1047 | 0.0234 | 0.1025 | -0.0097 | 0.0539 | -0.0288 | 7 | 7 | 0.0231 | 0.0662 | 20.9 | 19.8 | 20.1378 |
| 0 | 2 | -0.1566 | -20.0110 | 0.1097 | -0.0273 | 0.0435 | -0.0112 | 7 | 7 | 0.0208 | 0.0570 | 20.9 | 19.8 | 20.0361 |
| 0 | 3 | -0.1302 | 0.0385 | -19.9628 | 0.0299 | 0.0106 | -0.0551 | 7 | 7 | 0.0237 | 0.0304 | 20.9 | 19.8 | 19.9787 |
| 0 | 4 | 19.9133 | 0.0257 | 0.0066 | 0.0525 | -0.0150 | -0.0403 | 7 | 7 | 0.0236 | 0.0499 | 20.9 | 19.8 | 19.9452 |
| 0 | 5 | -0.0069 | 20.0152 | 0.0436 | 0.0157 | 0.0083 | 0.0058 | 7 | 7 | 0.0239 | 0.0386 | 20.9 | 19.8 | 20.0542 |
| 0 | 6 | -0.0138 | 0.0129 | 20.0536 | -0.0050 | -0.0100 | 0.0438 | 7 | 7 | 0.0223 | 0.0577 | 20.9 | 19.8 | 20.0950 |

## E.3.38 Dual Inferior: 0.5mm

## -------- Migration Results ------------

Reference Axis: Automatic

## Available scenes:

BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B I 05X1M0R --- X-number: 1 --- Follow-up: Postoperative B I 05X2M0R --- X-number: 2 --- Follow-up: Postoperative B I 05X3M0R --- X-number: 3 --- Follow-up: Postoperative B I 05X4M0R --- X-number: 4 --- Follow-up: Postoperative B I 05X5M0R --- X-number: 5 --- Follow-up: Postoperative B I 05X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid Body Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: BottomX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.4876 | -0.0078 | -0.0331 | -0.0586 | -0.0530 | -0.0594 | 7 | 6 | 0.0448 | 0.0046 | 20.0 | 20.2 | 0.5126 |
| 0 | 2 | 0.0047 | 0.5029 | 0.0452 | 0.0130 | 0.0080 | -0.0016 | 7 | 6 | 0.0265 | 0.0100 | 20.0 | 20.2 | 0.5236 |
| 0 | 3 | 0.0175 | -0.0205 | 0.6983 | 0.0801 | 0.0315 | -0.0106 | 7 | 6 | 0.0244 | 0.0108 | 20.0 | 20.2 | 0.7179 |
| 0 | 4 | -0.4867 | -0.0015 | 0.1157 | 0.0312 | 0.0140 | 0.0014 | 7 | 6 | 0.0339 | 0.0186 | 20.0 | 20.2 | 0.5378 |
| 0 | 5 | 0.0032 | -0.5090 | 0.1036 | 0.0080 | -0.0020 | -0.0033 | 7 | 6 | 0.0208 | 0.0069 | 20.0 | 20.2 | 0.5302 |
| 0 | 6 | -0.0049 | -0.0107 | -0.3528 | 0.0771 | -0.0340 | 0.0841 | 7 | 6 | 0.0273 | 0.0160 | 20.0 | 20.2 | 0.3879 |

## E.3.39 Dual Inferior: 1mm

-------- Migration Results -------------
Reference Axis: Automatic
$=====================================$
Available scenes:
----------------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B I 1X1M0R --- X-number: 1 --- Follow-up: Postoperative
B I 1X2M0R --- X-number: 2 --- Follow-up: Postoperative
B I 1X3M0R --- X-number: 3 --- Follow-up: Postoperative
B I 1X4M0R --- X-number: 4 --- Follow-up: Postoperative
B I 1X5M0R --- X-number: 5 --- Follow-up: Postoperative
B I 1X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body <br> Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: BottomX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.9937 | -0.0135 | 0.1807 | 0.0622 | -0.0450 | -0.0241 | 7 | 6 | 0.0551 | 0.0092 | 20.0 | 20.2 | 1.0353 |
| 0 | 2 | -0.0055 | 0.9921 | 0.0856 | 0.0286 | -0.0230 | 0.0099 | 7 | 6 | 0.0331 | 0.0192 | 20.0 | 20.2 | 1.0115 |
| 0 | 3 | 0.0009 | -0.0117 | 1.1783 | 0.0751 | -0.0020 | -0.0155 | 7 | 6 | 0.0243 | 0.0144 | 20.0 | 20.2 | 1.1997 |
| 0 | 4 | -0.9913 | -0.0047 | 0.1060 | 0.0307 | -0.0130 | -0.0099 | 7 | 6 | 0.0318 | 0.0065 | 20.0 | 20.2 | 1.0169 |
| 0 | 5 | 0.0002 | -0.9969 | 0.0430 | 0.0538 | -0.0230 | 0.0187 | 7 | 6 | 0.0288 | 0.0048 | 20.0 | 20.2 | 1.0533 |
| 0 | 6 | 0.0159 | -0.0204 | -0.8105 | 0.0867 | 0.0097 | -0.0149 | 7 | 6 | 0.0428 | 0.0107 | 20.0 | 20.2 | 0.8592 |

## E.3.40 Dual Inferior: 5mm

-------- Migration Results ------------
Reference Axis: Automatic
$==================================$
Available scenes:
---------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B I 5X1M0R --- X-number: 1 --- Follow-up: Postoperative
B I 5X2M0R --- X-number: 2 -- Follow-up: Postoperative
B I 5X3M0R --- X-number: 3 -- Follow-up: Postoperative
B I 5X4M0R --- X-number: 4 -- Follow-up: Postoperative
B I 5X5M0R --- X-number: 5 --- Follow-up: Postoperative
B I 5X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: BottomX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 5.0297 | -0.0009 | 0.0055 | -0.0064 | 0.0536 | -0.0378 | 7 | 6 | 0.0407 | 0.0270 | 20.0 | 20.2 | 5.0821 |
| 0 | 2 | 0.0094 | 4.9836 | 0.1544 | 0.0712 | 0.0159 | 0.0209 | 7 | 6 | 0.0297 | 0.0092 | 20.0 | 20.2 | 5.0239 |
| 0 | 3 | 0.0069 | -0.0171 | 5.0653 | 0.0338 | -0.031 | -0.0415 | 7 | 6 | 0.0449 | 0.0064 | 20.0 | 20.2 | 5.1142 |
| 0 | 4 | -4.9842 | -0.0059 | 0.2107 | 0.0497 | 0.0209 | -0.0012 | 7 | 6 | 0.0299 | 0.0149 | 20.0 | 20.2 | 5.0032 |
| 0 | 5 | 0.0211 | -5.0005 | 0.0896 | 0.0268 | 0.0072 | -0.0067 | 7 | 6 | 0.0439 | 0.0247 | 20.0 | 20.2 | 5.0267 |
| 0 | 6 | 0.0122 | -0.0104 | -4.8238 | 0.0836 | 0.0071 | 0.0305 | 7 | 6 | 0.0424 | 0.0138 | 20.0 | 20.2 | 4.8683 |

## E.3.41 Dual Inferior: 10mm

-------- Migration Results -------------
Reference Axis: Automatic
=-=================================
Available scenes:
-------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B I 10X1M0R --- X-number: 1 --- Follow-up: Postoperative
B I 10X2M0R --- X-number: 2 --- Follow-up: Postoperative
B I 10X3M0R --- X-number: 3 --- Follow-up: Postoperative
B I 10X4M0R --- X-number: 4 --- Follow-up: Postoperative
B I 10X5M0R --- X-number: 5 --- Follow-up: Postoperative
B I 10X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid <br> Body <br> Error <br> Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: BottomX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 9.9771 | 0.0007 | 0.1351 | 0.0745 | -0.0014 | 0.0423 | 7 | 6 | 0.0339 | 0.0229 | 20 | 20.2 | 9.9963 |
| 0 | 2 | -0.0112 | 9.9973 | 0.1672 | 0.0146 | 0.0069 | -0.0346 | 7 | 6 | 0.0628 | 0.0082 | 20 | 20.2 | 10.0355 |
| 0 | 3 | -0.0035 | -0.0039 | 10.0836 | 0.0288 | -0.0013 | 0.0107 | 7 | 6 | 0.0385 | 0.0093 | 20 | 20.2 | 10.1468 |
| 0 | 4 | -9.9933 | -0.0093 | 0.0936 | 0.0522 | 0.0068 | -0.0066 | 7 | 6 | 0.0494 | 0.0061 | 20 | 20.2 | 10.0155 |
| 0 | 5 | -0.0006 | -10.0230 | 0.2476 | 0.1558 | -0.0150 | 0.0090 | 7 | 6 | 0.0705 | 0.0254 | 20 | 20.2 | 10.1048 |
| 0 | 6 | -0.0275 | 0.0072 | -9.9036 | 0.0570 | -0.0020 | 0.0150 | 7 | 6 | 0.0390 | 0.0274 | 20 | 20.2 | 9.9447 |

## E.3.42 Dual Inferior: 20mm

-------- Migration Results -------------
Reference Axis: Automatic
$=====================================$
Available scenes:
-----------------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B I 20X1M0R --- X-number: 1 --- Follow-up: Postoperative
B I 20X2M0R --- X-number: 2 --- Follow-up: Postoperative
B I 20X3M0R --- X-number: 3 --- Follow-up: Postoperative
B I 20X4M0R --- X-number: 4 --- Follow-up: Postoperative
B I 20X5M0R --- X-number: 5 --- Follow-up: Postoperative
B I 20X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |
| Reference: BottomX0M0R --- L1 |  |  |  |  |  |
| 0 | 1 | 20.0089 | -0.0097 | 0.1574 | 0.0851 |
| 0 | 2 | 0.0067 | 19.9932 | 0.1978 | 0.0074 |
| 0 | 3 | 0.0282 | -0.0324 | 20.1722 | 0.0911 |
| 0 | 4 | -19.9838 | -0.0157 | 0.1771 | 0.0536 |
| 0 | 5 | 0.0225 | -20.0138 | 0.1297 | 0.0897 |
| 0 | 6 | 0.0075 | 0.0134 | -19.8111 | 0.0377 |

$\mathrm{Ry} \quad \mathrm{Rz}$

| Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -0.0035 | 7 | 6 | 0.0409 | 0.0110 | 20.0 | 20.2 | 20.0304 |
| -0.0475 | 7 | 6 | 0.0183 | 0.0099 | 20.0 | 20.2 | 20.0199 |
| 0.0253 | 7 | 6 | 0.0520 | 0.0193 | 20.0 | 20.2 | 20.2207 |
| -0.0327 | 7 | 6 | 0.0261 | 0.0208 | 20.0 | 20.2 | 19.9999 |
| 0.0125 | 7 | 6 | 0.0376 | 0.0304 | 20.0 | 20.2 | 20.0849 |
| -0.0304 | 7 | 6 | 0.0351 | 0.0131 | 20.0 | 20.2 | 19.8528 |

## E.3.43 Dual Rotation Superior: $1^{0}$

## -------- Migration Results -----------

Reference Axis: Automatic
===========================================

Available scenes:
TopX0M0R --- X-number: 0 --- Follow-up: Postoperative T R 1X1M0R --- X-number: 1 --- Follow-up: Postoperative T R 1X2M0R --- X-number: 2 --- Follow-up: Postoperative T R 1X3M0R --- X-number: 3 --- Follow-up: Postoperative T R 1X4M0R --- X-number: 4 --- Follow-up: Postoperative T R 1X5M0R --- X-number: 5 --- Follow-up: Postoperative T R 1X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0405 | 0.0195 | -0.0102 | 1.0196 | 0.0330 | -0.0475 | 7 | 7 | 0.0319 | 0.0280 | 20.9 | 19.8 | 0.5608 |
| 0 | 2 | -0.0875 | 0.0298 | -0.0101 | 0.0384 | 0.9828 | 0.0249 | 7 | 7 | 0.0281 | 0.0395 | 20.9 | 19.8 | 0.5632 |
| 0 | 3 | 0.0578 | 0.0103 | -0.0227 | 0.0188 | 0.0138 | 1.0198 | 7 | 7 | 0.0365 | 0.0404 | 20.9 | 19.8 | 0.5273 |
| 0 | 4 | -0.0136 | 0.0207 | -0.0456 | -0.9725 | -0.0140 | -0.0319 | 7 | 7 | 0.0334 | 0.0524 | 20.9 | 19.8 | 0.5864 |
| 0 | 5 | -0.0060 | 0.0107 | 0.0092 | 0.0557 | -1.0360 | 0.0399 | 7 | 7 | 0.0276 | 0.0617 | 20.9 | 19.8 | 0.6094 |
| 0 | 6 | -0.0421 | 0.0313 | -0.0184 | 0.0397 | 0.0106 | -1.0246 | 7 | 7 | 0.0307 | 0.0586 | 20.9 | 19.8 | 0.5697 |

## E.3.44 Dual Rotation Inferior: $\mathbf{1}^{\circ}$

-------- Migration Results ------------
Reference Axis: Automatic
======================================
Available scenes:
-----------------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B R 1X1M0R --- X-number: 1 --- Follow-up: Postoperative
B R 1X2M0R --- X-number: 2 --- Follow-up: Postoperative
B R 1X3M0R --- X-number: 3 --- Follow-up: Postoperative
B R 1X4M0R --- X-number: 4 --- Follow-up: Postoperative
B R 1X5M0R --- X-number: 5 --- Follow-up: Postoperative
B R 1X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body <br> Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: BottomX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.0180 | -0.0231 | 0.2596 | 1.1562 | 0.0400 | 0.0120 | 7 | 6 | 0.0484 | 0.0083 | 20.0 | 20.2 | 0.7163 |
| 0 | 2 | -0.0066 | -0.0227 | 0.1431 | 0.0767 | 1.0017 | 0.0171 | 7 | 6 | 0.0338 | 0.0294 | 20.0 | 20.2 | 0.6706 |
| 0 | 3 | 0.0094 | -0.0196 | 0.1545 | 0.0777 | 0.0167 | 0.9409 | 7 | 6 | 0.0378 | 0.0041 | 20.0 | 20.2 | 0.5143 |
| 0 | 4 | 0.0195 | -0.0139 | 0.1677 | -0.9374 | 0.0199 | -0.0600 | 7 | 6 | 0.0324 | 0.0213 | 20.0 | 20.2 | 0.5666 |
| 0 | 5 | 0.0105 | -0.0124 | 0.2530 | 0.0834 | -0.9900 | 0.0094 | 7 | 6 | 0.0445 | 0.0083 | 20.0 | 20.2 | 0.7747 |
| 0 | 6 | 0.0177 | -0.0088 | 0.2267 | 0.0682 | 0.0373 | -0.9620 | 7 | 6 | 0.0400 | 0.0240 | 20.0 | 20.2 | 0.5648 |

## E.3.45 Dual Rotation Superior: $3^{\circ}$

-------- Migration Results -----------
Reference Axis: Automatic
========================================

Available scenes:
TopX0M0R --- X-number: 0 --- Follow-up: Postoperative T R 3X1M0R --- X-number: 1 --- Follow-up: Postoperative T R 3X2M0R --- X-number: 2 --- Follow-up: Postoperative T R 3X3M0R --- X-number: 3 --- Follow-up: Postoperative T R 3X4M0R --- X-number: 4 --- Follow-up: Postoperative T R 3X5M0R --- X-number: 5 --- Follow-up: Postoperative
T R 3X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0161 | 0.0388 | -0.0146 | 3.0637 | 0.0046 | -0.0044 | 7 | 7 | 0.0456 | 0.0627 | 20.9 | 19.8 | 1.7399 |
| 0 | 2 | -0.0066 | 0.0128 | 0.0170 | 0.0025 | -2.9730 | -0.0549 | 7 | 7 | 0.0513 | 0.0481 | 20.9 | 19.8 | 1.7577 |
| 0 | 3 | -0.0690 | 0.0290 | -0.0083 | 0.0437 | 0.0281 | 2.9486 | 7 | 7 | 0.0363 | 0.0443 | 20.9 | 19.8 | 1.5312 |
| 0 | 4 | 0.0095 | 0.0281 | -0.0277 | -2.9744 | -0.0070 | 0.0398 | 7 | 7 | 0.0376 | 0.0251 | 20.9 | 19.8 | 1.7383 |
| 0 | 5 | -0.0463 | 0.0232 | -0.0220 | 0.0394 | 2.9911 | 0.0175 | 7 | 7 | 0.0231 | 0.0604 | 20.9 | 19.8 | 1.6954 |
| 0 | 6 | -0.1213 | 0.0392 | -0.0254 | 0.0346 | -0.0110 | -2.9899 | 7 | 7 | 0.0401 | 0.0584 | 20.9 | 19.8 | 1.5427 |

## E.3.46 Dual Rotation Inferior: $3^{\circ}$

-------- Migration Results -------------
Reference Axis: Automatic
$======================================$
Available scenes:
----------------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B R 3X1M0R --- X-number: 1 --- Follow-up: Postoperative
B R 3X2M0R --- X-number: 2 --- Follow-up: Postoperative
B R 3X3M0R --- X-number: 3 --- Follow-up: Postoperative
B R 3X4M0R --- X-number: 4 --- Follow-up: Postoperative
B R 3X5M0R --- X-number: 5 --- Follow-up: Postoperative
B R 3X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: BottomX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.0130 | -0.0126 | 0.1575 | 3.0910 | 0.0651 | 0.0514 | 7 | 6 | 0.0504 | 0.0086 | 20.0 | 20.2 | 1.7855 |
| 0 | 2 | 0.0090 | -0.0157 | 0.1814 | 0.0418 | -2.9910 | -0.0256 | 7 | 6 | 0.0373 | 0.0079 | 20.0 | 20.2 | 1.7379 |
| 0 | 3 | 0.0382 | -0.0311 | 0.2768 | 0.1061 | 0.0560 | 2.8804 | 7 | 6 | 0.0394 | 0.0474 | 20.0 | 20.2 | 1.5180 |
| 0 | 4 | 0.0097 | -0.2917 | 0.1053 | -2.9510 | 0.1573 | -0.1291 | 6 | 6 | 0.0765 | 0.0112 | 21.9 | 20.2 | 1.6665 |
| 0 | 5 | 0.0340 | -0.0047 | 0.0483 | 0.0241 | 3.0967 | -0.0053 | 7 | 6 | 0.0587 | 0.0625 | 20.0 | 20.2 | 1.8136 |
| 0 | 6 | 0.0102 | -0.0014 | 0.2438 | 0.1089 | 0.0162 | -2.8766 | 7 | 6 | 0.0545 | 0.0046 | 20.0 | 20.2 | 1.5319 |

## E.3.47 Dual Rotation Superior: $6^{0}$

## -------- Migration Results -----------

Reference Axis: Automatic
=======================================

## Available scenes:

TopX0M0R --- X-number: 0 --- Follow-up: Postoperative T R 6X1M0R --- X-number: 1 --- Follow-up: Postoperative T R 6X2M0R --- X-number: 2 --- Follow-up: Postoperative T R 6X3M0R --- X-number: 3 --- Follow-up: Postoperative T R 6X4M0R --- X-number: 4 --- Follow-up: Postoperative T R 6X5M0R --- X-number: 5 --- Follow-up: Postoperative T R 6X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid Body Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.0197 | -0.0025 | 0.0024 | 5.9828 | -0.0090 | -0.0436 | 7 | 7 | 0.0284 | 0.0613 | 20.9 | 19.8 | 3.4706 |
| 0 | 2 | -0.5618 | 0.0140 | 0.1314 | 0.0327 | 5.9908 | 0.0555 | 6 | 7 | 0.0654 | 0.0373 | 22.7 | 19.8 | 3.4597 |
| 0 | 3 | 0.0205 | 0.0047 | 0.0458 | 0.0010 | 0.0023 | 6.0203 | 7 | 7 | 0.0448 | 0.0264 | 20.9 | 19.8 | 3.0084 |
| 0 | 4 | -0.0154 | 0.0209 | -0.0066 | -5.9846 | -0.0220 | 0.0012 | 7 | 7 | 0.0441 | 0.0482 | 20.9 | 19.8 | 3.4867 |
| 0 | 5 | 0.0117 | 0.0153 | 0.0706 | 0.0528 | -6.1090 | 0.0609 | 7 | 7 | 0.1407 | 0.0675 | 20.9 | 19.8 | 3.4527 |
| 0 | 6 | 0.0139 | 0.0252 | -0.0205 | 0.0290 | -0.0320 | -5.9840 | 7 | 7 | 0.0272 | 0.0292 | 20.9 | 19.8 | 3.0723 |

## E.3.48 Dual Rotation Inferior: $\mathbf{6}^{0}$

-------- Migration Results ------------
Reference Axis: Automatic
$=================================$
Available scenes:
---------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B R 6X1M0R --- X-number: 1 --- Follow-up: Postoperative
B R 6X2M0R --- X-number: 2 --- Follow-up: Postoperative
B R 6X3M0R --- X-number: 3 --- Follow-up: Postoperative
B R 6X4M0R --- X-number: 4 -- Follow-up: Postoperative
B R 6X5M0R --- X-number: 5 --- Follow-up: Postoperative
B R 6X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid <br> Body <br> Error <br> Reference | Condition Number |  | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: 78 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: BottomX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.0206 | -0.0208 | 0.0288 | 6.0296 | 0.0222 | -0.0297 | 7 | 6 | 0.0502 | 0.0159 | 20.0 | 20.2 | 3.5100 |
| 0 | 2 | -0.3929 | -0.0176 | -0.5471 | -0.0215 | 6.1390 | -0.1384 | 5 | 6 | 0.0710 | 0.0246 | 26.2 | 20.2 | 3.5593 |
| 0 | 3 | 0.0166 | -0.0678 | 0.1852 | 0.0341 | 0.0033 | 5.9310 | 6 | 6 | 0.0620 | 0.0229 | 21.9 | 20.2 | 3.0675 |
| 0 | 4 | 0.0431 | -0.5663 | 0.2822 | -5.9088 | 0.1027 | -0.0581 | 6 | 6 | 0.0427 | 0.0378 | 21.9 | 20.2 | 3.3841 |
| 0 | 5 | 0.0251 | -0.0285 | 0.3027 | 0.1365 | -5.9690 | 0.0070 | 7 | 6 | 0.0791 | 0.0396 | 20.0 | 20.2 | 3.5124 |
| 0 | 6 | 0.0110 | -0.0133 | 0.1649 | 0.1011 | 0.0195 | -5.9877 | 7 | 6 | 0.0658 | 0.0158 | 20.0 | 20.2 | 3.0478 |

## E.3.49 Dual Rotation Superior: $\mathbf{1 0}^{\circ}$

## -------- Migration Results -----------

Reference Axis: Automatic
======================================

Available scenes:
TopX0M0R --- X-number: 0 --- Follow-up: Postoperative
T R 10X1M0R --- X-number: 1 --- Follow-up: Postoperative TR 10X2M0R --- X-number: 2 --- Follow-up: Postoperative T R 10X3M0R --- X-number: 3 --- Follow-up: Postoperative T R 10X4M0R --- X-number: 4 --- Follow-up: Postoperative T R 10X5M0R --- X-number: 5 --- Follow-up: Postoperative
T R 10X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid Body Error Reference | Condition Number |  | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: TopX0M0R --- T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0086 | -0.0154 | -0.0111 | 9.9804 | -0.0385 | -0.0127 | 7 | 7 | 0.0481 | 0.1044 | 20.9 | 19.8 | 5.7744 |
| 0 | 2 | -0.0166 | 0.0068 | 0.0327 | -0.0055 | 9.9796 | -0.0348 | 7 | 7 | 0.1031 | 0.0429 | 20.9 | 19.8 | 5.8205 |
| 0 | 3 | -0.0058 | 0.0273 | -0.0055 | 0.0242 | 0.0303 | 10.0201 | 7 | 7 | 0.0609 | 0.0427 | 20.9 | 19.8 | 5.0389 |
| 0 | 4 | 0.0297 | -0.8873 | 0.0740 | -9.9706 | 0.0044 | -0.0529 | 6 | 7 | 0.0513 | 0.0731 | 22.7 | 19.8 | 5.7687 |
| 0 | 5 | -0.2450 | -0.0176 | -0.8381 | 0.0292 | -10.103 | -0.0083 | 6 | 7 | 0.0601 | 0.0479 | 28.2 | 19.8 | 5.8576 |
| 0 | 6 | -0.0019 | 0.0228 | -0.0183 | 0.0259 | -0.0460 | -9.9888 | 7 | 7 | 0.0358 | 0.0628 | 20.9 | 19.8 | 5.1156 |

## E.3.50 Dual Rotation Inferior: $\mathbf{1 0}^{\text {o }}$

-------- Migration Results ------------
Reference Axis: Automatic
$=====================================$
Available scenes:
--------------------------------
BottomX0M0R --- X-number: 0 --- Follow-up: Postoperative
B R 10X1M0R --- X-number: 1 --- Follow-up: Postoperative
B R 10X2M0R --- X-number: 2 --- Follow-up: Postoperative
B R 10X3M0R --- X-number: 3 --- Follow-up: Postoperative
B R 10X4M0R --- X-number: 4 --- Follow-up: Postoperative
B R 10X5M0R --- X-number: 5 --- Follow-up: Postoperative
B R 10X6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid Body Error | Rigid <br> Body <br> Error <br> Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: BottomX0M0R --- L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.0179 | -0.0236 | 0.1934 | 10.1017 | 0.0167 | -0.0212 | 7 | 6 | 0.0398 | 0.0052 | 20.0 | 20.2 | 5.8419 |
| 0 | 2 | 0.0290 | -0.0470 | 0.1545 | 0.1232 | 10.0098 | -0.0658 | 7 | 6 | 0.1471 | 0.0300 | 20.0 | 20.2 | 5.8937 |
| 0 | 3 | 0.0249 | -0.1019 | 0.2897 | 0.1070 | 0.0074 | 9.8961 | 6 | 6 | 0.0488 | 0.0395 | 21.9 | 20.2 | 5.0752 |
| 0 | 4 | 0.0451 | -0.8973 | 0.3655 | -9.8709 | 0.1737 | -0.0102 | 6 | 6 | 0.2043 | 0.0052 | 21.9 | 20.2 | 5.7059 |
| 0 | 5 | -0.2614 | -0.0161 | -0.6923 | 0.1258 | -10.1020 | -0.1078 | 6 | 6 | 0.1637 | 0.0057 | 26.0 | 20.2 | 5.8316 |
| 0 | 6 | 0.0018 | -0.0332 | 0.3589 | 0.1750 | 0.0175 | -10.0340 | 7 | 6 | 0.0528 | 0.0444 | 20.0 | 20.2 | 5.0853 |

## E. 4 Prediction Interval Accuracy Calculations

## E.4.1 Caudal: X

| Failure Examined | Data |  | Prediction Interval |  |  |  | Accuracy <br> Half <br> Width |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Induced Displacement | Measured | Lower Limit | Upper Limit | Width | Average Width |  |
| Superior <br> (T4) | 0.5000 | 0.4925 | 0.4348 | 0.5522 | 0.1174 | 0.0528 | 0.1057 |
|  | -0.5000 | -0.5210 | -0.5667 | -0.4493 | 0.1174 |  |  |
|  | 1.0000 | 0.9803 | 0.9356 | 1.0530 | 0.1174 |  |  |
|  | -1.0000 | -1.0417 | -1.0675 | -0.9501 | 0.1174 |  |  |
|  | 5.0000 | 5.0276 | 4.9412 | 5.0599 | 0.1187 |  |  |
|  | -5.0000 | -4.9921 | -5.0744 | -4.9557 | 0.1187 |  |  |
|  | 10.0000 | 10.0019 | 9.9472 | 10.0696 | 0.1224 |  |  |
|  | -10.0000 | -9.9839 | -10.0841 | -9.9617 | 0.1224 |  |  |
|  | 20.0000 | 20.0235 | 19.9560 | 20.0921 | 0.1362 |  |  |
|  | -20.0000 | -20.0596 | -20.1066 | -19.9705 | 0.1362 |  |  |
| Inferior <br> (T8) | 0.5000 | 0.4814 | 0.4177 | 0.5298 | 0.1121 |  |  |
|  | -0.5000 | -0.5233 | -0.5847 | -0.4726 | 0.1121 |  |  |
|  | 1.0000 | 0.9771 | 0.9189 | 1.0310 | 0.1121 |  |  |
|  | -1.0000 | -1.0577 | -1.0860 | -0.9738 | 0.1121 |  |  |
|  | 5.0000 | 5.0022 | 4.9279 | 5.0412 | 0.1133 |  |  |
|  | -5.0000 | -5.0565 | -5.0961 | -4.9829 | 0.1133 |  |  |
|  | 10.0000 | 9.9811 | 9.9382 | 10.0550 | 0.1168 |  |  |
|  | -10.0000 | -10.0048 | -10.1099 | -9.9931 | 0.1168 |  |  |
|  | 20.0000 | 20.0214 | 19.9556 | 20.0856 | 0.1300 |  |  |
|  | -20.0000 | -20.0957 | -20.1406 | -20.0106 | 0.1300 |  |  |
| Inferior <br> (T8) | 0.5000 | 0.4884 | 0.4542 | 0.5288 | 0.0746 |  |  |
|  | -0.5000 | -0.5005 | -0.5467 | -0.4721 | 0.0746 |  |  |
|  | 1.0000 | 0.9909 | 0.9546 | 1.0292 | 0.0746 |  |  |
|  | -1.0000 | -1.0206 | -1.0472 | -0.9726 | 0.0746 |  |  |
|  | 5.0000 | 5.0040 | 4.9578 | 5.0331 | 0.0754 |  |  |
|  | -5.0000 | -5.0072 | -5.0511 | -4.9757 | 0.0754 |  |  |
|  | 10.0000 | 9.9829 | 9.9610 | 10.0387 | 0.0777 |  |  |
|  | -10.0000 | -9.9889 | -10.0567 | -9.9789 | 0.0777 |  |  |
|  | 20.0000 | 20.0094 | 19.9655 | 20.0519 | 0.0865 |  |  |
|  | -20.0000 | -20.0481 | -20.0699 | -19.9834 | 0.0865 |  |  |

## E.4.2 Caudal: Y

| Failure <br> Examined | Data |  | Prediction Interval |  |  |  | Accuracy <br> Half Width |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Induced Displacement | Measured | Lower <br> Limit | Upper Limit | Width | Average Width |  |
| Superior <br> (T4) | 0.5000 | 0.4983 | 0.4622 | 0.5415 | 0.0793 | 0.0468 | 2 |
|  | -0.5000 | -0.4976 | -0.5374 | -0.4581 | 0.0793 |  |  |
|  | 1.0000 | 1.0062 | 0.9620 | 1.0413 | 0.0793 |  |  |
|  | -1.0000 | -0.9890 | -1.0372 | -0.9579 | 0.0793 |  |  |
|  | 5.0000 | 4.9920 | 4.9600 | 5.0402 | 0.0802 |  |  |
|  | -5.0000 | -5.0194 | -5.0361 | -4.9559 | 0.0802 |  |  |
|  | 10.0000 | 10.0134 | 9.9568 | 10.0395 | 0.0827 |  |  |
|  | -10.0000 | -9.9639 | -10.0354 | -9.9527 | 0.0827 |  |  |
|  | 20.0000 | 19.9844 | 19.9483 | 20.0403 | 0.0920 |  |  |
|  | -20.0000 | -20.0040 | -20.0362 | -19.9442 | 0.0920 |  |  |
| Inferior <br> (T8) | 0.5000 | 0.4883 | 0.4767 | 0.5122 | 0.0354 |  |  |
|  | -0.5000 | -0.4976 | -0.5225 | -0.4870 | 0.0354 |  |  |
|  | 1.0000 | 0.9881 | 0.9763 | 1.0118 | 0.0354 |  |  |
|  | -1.0000 | -1.0189 | -1.0221 | -0.9866 | 0.0354 |  |  |
|  | 5.0000 | 4.9978 | 4.9730 | 5.0088 | 0.0358 |  |  |
|  | -5.0000 | -4.9983 | -5.0191 | -4.9833 | 0.0358 |  |  |
|  | 10.0000 | 9.9884 | 9.9685 | 10.0054 | 0.0369 |  |  |
|  | -10.0000 | -9.9917 | -10.0157 | -9.9788 | 0.0369 |  |  |
|  | 20.0000 | 19.9808 | 19.9585 | 19.9995 | 0.0411 |  |  |
|  | -20.0000 | -19.9884 | -20.0098 | -19.9688 | 0.0411 |  |  |
| Inferior (T8) | 0.5000 | 0.4919 | 0.4868 | 0.5066 | 0.0198 |  |  |
|  | -0.5000 | -0.5076 | -0.5133 | -0.4935 | 0.0198 |  |  |
|  | 1.0000 | 0.9974 | 0.9868 | 1.0067 | 0.0198 |  |  |
|  | -1.0000 | -1.0087 | -1.0134 | -0.9936 | 0.0198 |  |  |
|  | 5.0000 | 5.0017 | 4.9873 | 5.0073 | 0.0200 |  |  |
|  | -5.0000 | -5.0029 | -5.0140 | -4.9940 | 0.0200 |  |  |
|  | 10.0000 | 9.9966 | 9.9876 | 10.0082 | 0.0206 |  |  |
|  | -10.0000 | -10.0047 | -10.0150 | -9.9943 | 0.0206 |  |  |
|  | 20.0000 | 20.0036 | 19.9877 | 20.0107 | 0.0230 |  |  |
|  | -20.0000 | -20.0010 | -20.0174 | -19.9944 | 0.0230 |  |  |

## E.4.3 Caudal: Z

| Failure <br> Examined | Data |  | Prediction Interval |  |  |  | Accuracy <br> Half Width |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Induced Displacement | Measured | Lower Limit | Upper Limit | Width | Average Width |  |
| Superior <br> (T4) | 0.5000 | 0.6843 | 0.4068 | 0.9062 | 0.4994 | 0.4725 | 0.2363 |
|  | -0.5000 | -0.4760 | -0.5949 | -0.0955 | 0.4994 |  |  |
|  | 1.0000 | 1.1696 | 0.9076 | 1.4071 | 0.4995 |  |  |
|  | -1.0000 | -1.0138 | -1.0958 | -0.5963 | 0.4995 |  |  |
|  | 5.0000 | 5.3431 | 4.9118 | 5.4165 | 0.5047 |  |  |
|  | -5.0000 | -4.8776 | -5.1051 | -4.6005 | 0.5047 |  |  |
|  | 10.0000 | 10.1872 | 9.9124 | 10.4328 | 0.5204 |  |  |
|  | -10.0000 | -9.7871 | -10.1215 | -9.6010 | 0.5204 |  |  |
|  | 20.0000 | 20.1803 | 19.8999 | 20.4791 | 0.5792 |  |  |
|  | -20.0000 | -19.8533 | -20.1678 | -19.5886 | 0.5792 |  |  |
| Inferior <br> (T8) | 0.5000 | 0.7189 | 0.3742 | 0.9279 | 0.5537 |  |  |
|  | -0.5000 | -0.5006 | -0.6206 | -0.0668 | 0.5537 |  |  |
|  | 1.0000 | 1.1599 | 0.8715 | 1.4254 | 0.5539 |  |  |
|  | -1.0000 | -0.7756 | -1.1180 | -0.5641 | 0.5539 |  |  |
|  | 5.0000 | 5.3170 | 4.8477 | 5.4074 | 0.5596 |  |  |
|  | -5.0000 | -4.9900 | -5.1000 | -4.5404 | 0.5596 |  |  |
|  | 10.0000 | 10.0430 | 9.8129 | 10.3900 | 0.5771 |  |  |
|  | -10.0000 | -9.7468 | -10.0826 | -9.5055 | 0.5771 |  |  |
|  | 20.0000 | 20.0310 | 19.7280 | 20.3703 | 0.6422 |  |  |
|  | -20.0000 | -19.7200 | -20.0629 | -19.4207 | 0.6422 |  |  |
| Inferior <br> (T8) | 0.5000 | 0.6095 | 0.4223 | 0.7289 | 0.3066 |  |  |
|  | -0.5000 | -0.5137 | -0.5741 | -0.2675 | 0.3066 |  |  |
|  | 1.0000 | 1.0845 | 0.9204 | 1.2272 | 0.3067 |  |  |
|  | -1.0000 | -0.8680 | -1.0724 | -0.7657 | 0.3067 |  |  |
|  | 5.0000 | 5.1620 | 4.9045 | 5.2143 | 0.3099 |  |  |
|  | -5.0000 | -4.9889 | -5.0596 | -4.7497 | 0.3099 |  |  |
|  | 10.0000 | 10.0013 | 9.8816 | 10.2012 | 0.3196 |  |  |
|  | -10.0000 | -9.8783 | -10.0464 | -9.7269 | 0.3196 |  |  |
|  | 20.0000 | 19.9990 | 19.8276 | 20.1833 | 0.3556 |  |  |
|  | -20.0000 | -19.8335 | -20.0285 | -19.6729 | 0.3556 |  |  |

## E.4.4 Caudal: Rx

|  | Data |  | Prediction Interval |  |  |  | Accuracy |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| Failure <br> Examined | Induced <br> Displacement | Measured | Lower <br> Limit | Upper <br> Limit | Width | Width | Half Width |
|  | 1.0000 | 1.0229 | 0.9880 | 1.0838 | 0.0959 |  |  |
|  | -1.0000 | -0.9431 | -1.0174 | -0.9216 | 0.0959 |  |  |
|  | 3.0000 | 3.0136 | 2.9928 | 3.0898 | 0.0970 |  |  |
| Inferior | -3.0000 | -2.9579 | -3.0234 | -2.9264 | 0.0970 | 0.1008 | $\mathbf{0 . 0 5 0 4}$ |
| (T8) | 6.0000 | 6.0519 | 5.9990 | 6.0998 | 0.1008 |  |  |
|  | -6.0000 | -5.9859 | -6.0334 | -5.9326 | 0.1008 |  |  |
|  | 10.0000 | 10.0662 | 10.0056 | 10.1149 | 0.1093 |  |  |
|  | -10.0000 | -10.0020 | -10.0485 | -9.9392 | 0.1093 |  |  |

## E.4.5 Caudal: Ry

| Failure <br> Examined | Data |  | Prediction Interval |  |  |  | Accuracy <br> Half Width |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Induced Displacement | Measured | $\begin{aligned} & \text { Lower } \\ & \text { Limit } \end{aligned}$ | Upper Limit | Width | Average Width |  |
| Inferior (T8) | 1.0000 | 0.9896 | 0.9376 | 1.0756 | 0.1380 | 0.1450 | 0.0725 |
|  | -1.0000 | -0.9950 | -1.0694 | -0.9314 | 0.1380 |  |  |
|  | -3.0000 | 3.0038 | 2.9437 | 3.0834 | 0.1397 |  |  |
|  | 3.0000 | -2.9943 | -3.0772 | -2.9375 | 0.1397 |  |  |
|  | 6.0000 | 6.0738 | 5.9514 | 6.0965 | 0.1451 |  |  |
|  | -6.0000 | -6.0375 | -6.0904 | -5.9452 | 0.1451 |  |  |
|  | 10.0000 | 10.0106 | 9.9592 | 10.1166 | 0.1574 |  |  |
|  | -10.0000 | -10.0263 | -10.1104 | -9.9530 | 0.1574 |  |  |

## E.4.6 Caudal: Rz

| Failure <br> Examined | Data |  | Prediction Interval |  |  |  | Accuracy <br> Half Width |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Induced Displacement | Measured | Lower Limit | Upper Limit | Width | Average Width |  |
| Inferior <br> (T8) | 1.0000 | 1.0090 | 0.9499 | 1.0287 | 0.0788 | 0.0828 | 0.0414 |
|  | -1.0000 | -1.0087 | -1.0526 | -0.9738 | 0.0788 |  |  |
|  | 3.0000 | 2.9892 | 2.9519 | 3.0316 | 0.0797 |  |  |
|  | -3.0000 | -3.0443 | -3.0555 | -2.9758 | 0.0797 |  |  |
|  | 6.0000 | 6.0028 | 5.9540 | 6.0368 | 0.0829 |  |  |
|  | -6.0000 | -6.0167 | -6.0607 | -5.9779 | 0.0829 |  |  |
|  | 10.0000 | 9.9927 | 9.9554 | 10.0452 | 0.0898 |  |  |
|  | -10.0000 | -10.0196 | -10.0691 | -9.9793 | 0.0898 |  |  |

## E.4.7 Apex: X

| Failure <br> Examined | Data |  | Prediction Interval |  |  |  | Accuracy <br> Half Width |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Induced Displacement | Measured | Lower <br> Limit | Upper Limit | Width | Average Width |  |
| Superior <br> (T4) | 0.5000 | 0.5481 | 0.4194 | 0.6296 | 0.2102 | 0.3003 | 0.1501 |
|  | -0.5000 | -0.4761 | -0.5813 | -0.3712 | 0.2102 |  |  |
|  | 1.0000 | 1.0937 | 0.9198 | 1.1300 | 0.2102 |  |  |
|  | -1.0000 | -0.9808 | -1.0817 | -0.8715 | 0.2102 |  |  |
|  | 5.0000 | 4.9426 | 4.9218 | 5.1342 | 0.2124 |  |  |
|  | -5.0000 | -4.9686 | -5.0859 | -4.8735 | 0.2124 |  |  |
|  | 10.0000 | 10.0617 | 9.9223 | 10.1414 | 0.2190 |  |  |
|  | -10.0000 | -10.0206 | -10.0931 | -9.8740 | 0.2190 |  |  |
|  | 20.0000 | 20.0293 | 19.9176 | 20.1614 | 0.2438 |  |  |
|  | -20.0000 | -19.9879 | -20.1131 | -19.8694 | 0.2438 |  |  |
| Inferior (L1) | -0.5000 | -0.3202 | -0.6530 | -0.2871 | 0.3659 |  |  |
|  | 0.5000 | 0.4822 | 0.3488 | 0.7147 | 0.3659 |  |  |
|  | -1.0000 | -0.9248 | -1.1540 | -0.7880 | 0.3660 |  |  |
|  | 1.0000 | 1.0194 | 0.8497 | 1.2157 | 0.3660 |  |  |
|  | -5.0000 | -4.9268 | -5.1632 | -4.7934 | 0.3698 |  |  |
|  | 5.0000 | 4.9868 | 4.8551 | 5.2248 | 0.3698 |  |  |
|  | -10.0000 | -10.0948 | -10.1781 | -9.7968 | 0.3813 |  |  |
|  | 10.0000 | 10.0113 | 9.8584 | 10.2397 | 0.3813 |  |  |
|  | -20.0000 | -19.9985 | -20.2178 | -19.7935 | 0.4243 |  |  |
|  | 20.0000 | 20.0738 | 19.8552 | 20.2795 | 0.4243 |  |  |

## E.4.8 Apex: Y

| Failure <br> Examined | Data |  | Prediction Interval |  |  |  | Accuracy <br> Half Width |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Induced Displacement | Measured | Lower Limit | Upper Limit | Width | Average <br> Width |  |
| Superior <br> (T4) | 0.5000 | 0.4826 | 0.4747 | 0.5166 | 0.0419 | 0.0475 | 0.0238 |
|  | -0.5000 | -0.4914 | -0.5256 | -0.4837 | 0.0419 |  |  |
|  | 1.0000 | 0.9991 | 0.9748 | 1.0167 | 0.0419 |  |  |
|  | -1.0000 | -0.9961 | -1.0257 | -0.9838 | 0.0419 |  |  |
|  | 5.0000 | 4.9853 | 4.9757 | 5.0180 | 0.0423 |  |  |
|  | -5.0000 | -5.0086 | -5.0270 | -4.9847 | 0.0423 |  |  |
|  | 10.0000 | 9.9959 | 9.9764 | 10.0200 | 0.0436 |  |  |
|  | -10.0000 | -10.0049 | -10.0290 | -9.9853 | 0.0436 |  |  |
|  | 20.0000 | 20.0047 | 19.9766 | 20.0252 | 0.0486 |  |  |
|  | -20.0000 | -20.0114 | -20.0341 | -19.9855 | 0.0486 |  |  |
| Inferior <br> (L1) | -0.5000 | -0.5019 | -0.5148 | -0.4655 | 0.0493 |  |  |
|  | 0.5000 | 0.5101 | 0.4853 | 0.5345 | 0.0493 |  |  |
|  | -1.0000 | -0.9931 | -1.0148 | -0.9655 | 0.0493 |  |  |
|  | 1.0000 | 0.9951 | 0.9853 | 1.0346 | 0.0493 |  |  |
|  | -5.0000 | -4.9853 | -5.0152 | -4.9654 | 0.0498 |  |  |
|  | 5.0000 | 5.0031 | 4.9852 | 5.0350 | 0.0498 |  |  |
|  | -10.0000 | -9.9891 | -10.0162 | -9.9649 | 0.0513 |  |  |
|  | 10.0000 | 10.0275 | 9.9847 | 10.0360 | 0.0513 |  |  |
|  | -20.0000 | -19.9824 | -20.0196 | -19.9625 | 0.0571 |  |  |
|  | 20.0000 | 20.0149 | 19.9822 | 20.0394 | 0.0571 |  |  |

## E.4.9 Apex: Z

| Failure <br> Examined | Data <br> Induced <br> Displacement |  | Measured | Lower <br> Limit | Prediction Interval <br> Upper <br> Limit | Width | Average <br> Width |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | 0.5000 | 0.3915 | 0.3320 | 0.5664 | 0.2345 |  | Half Width |
| Superior | -0.5000 | -0.5483 | -0.6679 | -0.4334 | 0.2345 |  |  |
| (T4) | 1.0000 | 0.9519 | 0.8319 | 1.0664 | 0.2345 |  |  |
|  | -1.0000 | -0.9953 | -1.1679 | -0.9333 | 0.2345 |  |  |
|  | 5.0000 | 4.9133 | 4.8301 | 5.0671 | 0.2369 |  |  |
|  | -5.0000 | -5.0707 | -5.1685 | -4.9316 | 0.2369 |  |  |
|  | 10.0000 | 10.0433 | 9.8258 | 10.0701 | 0.2443 |  |  |
|  | -10.0000 | -10.0530 | -10.1716 | -9.9272 | 0.2443 |  |  |
|  | 20.0000 | 19.9065 | 19.8106 | 20.0826 | 0.2719 |  |  |
|  | -20.0000 | -20.0465 | -20.1840 | -19.9121 | 0.2719 | 0.2290 | $\mathbf{0 . 1 1 4 5}$ |
|  | -0.5000 | -0.4686 | -0.5695 | -0.3646 | 0.2049 |  |  |
|  | 0.5000 | 0.5599 | 0.4281 | 0.6330 | 0.2049 |  |  |
|  | -1.0000 | -0.9698 | -1.0683 | -0.8634 | 0.2049 |  |  |
|  | 1.0000 | 1.0540 | 0.9269 | 1.1318 | 0.2049 |  |  |
|  | -5.0000 | -4.9782 | -5.0598 | -4.8527 | 0.2071 |  |  |
|  | 5.0000 | 5.0579 | 4.9163 | 5.1233 | 0.2071 |  |  |
|  | -10.0000 | -10.0037 | -10.0511 | -9.8375 | 0.2135 |  |  |
|  | 10.0000 | 10.0618 | 9.9011 | 10.1146 | 0.2135 |  |  |
|  | -20.0000 | -19.9130 | -20.0392 | -19.8015 | 0.2376 |  |  |
|  | 20.0000 | 19.9173 | 19.8651 | 20.1027 | 0.2376 |  |  |

## E.4.10 Apex: Rx

| Failure <br> Examined | Induced <br> Displacement | Measured | Lower <br> Limit | Prediction Interval <br> Upper <br> Limit | Width | Average <br> Width | Half Width |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | -1.0000 | -1.0193 | -1.0827 | -0.9499 | 0.1327 |  |  |
|  | 1.0000 | 0.9722 | 0.9134 | 1.0462 | 0.1327 |  |  |
| Superior | -3.0000 | -3.0643 | -3.0796 | -2.9452 | 0.1344 |  |  |
| (T4) | 3.0000 | 2.9739 | 2.9087 | 3.0431 | 0.1344 |  |  |
|  | -6.0000 | -5.9829 | -6.0764 | -5.9368 | 0.1396 |  |  |
|  | 6.0000 | 5.9843 | 5.9002 | 6.0398 | 0.1396 |  |  |
|  | -10.0000 | -9.9811 | -10.0745 | -9.9231 | 0.1514 |  |  |
|  | 10.0000 | 9.9711 | 9.8865 | 10.0379 | 0.1514 | 0.1899 | $\mathbf{0 . 0 9 4 9}$ |
|  | -1.0000 | -1.1569 | -1.2021 | -0.9736 | 0.2286 |  |  |
|  | 1.0000 | 0.9366 | 0.7951 | 1.0237 | 0.2286 |  |  |
|  | -3.0000 | -3.0925 | -3.2008 | -2.9695 | 0.2313 |  |  |
|  | 3.0000 | 2.9513 | 2.7910 | 3.0223 | 0.2313 |  |  |
|  | -6.0000 | -6.0302 | -6.2012 | -5.9608 | 0.2404 |  |  |
|  | 6.0000 | 5.9096 | 5.7824 | 6.0228 | 0.2404 |  |  |
|  | -10.0000 | -10.1027 | -10.2059 | -9.9452 | 0.2606 |  |  |

## E.4.11 Apex: Ry

| Failure <br> Examined | Induced <br> Displacement | Measured | Lower <br> Limit | Prediction Interval <br> Upper <br> Limit | Width | Average <br> Width | Half Width |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
|  | -1.0000 | -0.9826 | -1.0741 | -0.8656 | 0.2085 |  |  |
|  | 1.0000 | 1.0357 | 0.9350 | 1.1435 | 0.2085 |  |  |
| Superior | 3.0000 | 2.9733 | 2.9429 | 3.1539 | 0.2111 |  |  |
| (T4) | -3.0000 | -2.9910 | -3.0845 | -2.8735 | 0.2111 |  |  |
|  | -6.0000 | -5.9899 | -6.1024 | -5.8830 | 0.2193 |  |  |
|  | 6.0000 | 6.1091 | 5.9524 | 6.1718 | 0.2193 |  |  |
|  | -10.0000 | -9.9799 | -10.1299 | -9.8921 | 0.2378 |  |  |
|  | 10.0000 | 10.1029 | 9.9615 | 10.1993 | 0.2378 | 0.2631 | $\mathbf{0 . 1 3 1 5}$ |
|  | -1.0000 | -1.0015 | -1.1743 | -0.8822 | 0.2921 |  |  |
|  | 1.0000 | 0.9893 | 0.8386 | 1.1307 | 0.2921 |  |  |
| Inferior | 3.0000 | 2.9917 | 2.8497 | 3.1453 | 0.2956 |  |  |
|  | -3.0000 | -3.0962 | -3.1889 | -2.8934 | 0.2956 |  |  |
|  | -6.0000 | -6.1184 | -6.2141 | -5.9069 | 0.3072 |  |  |
|  | 6.0000 | 5.9683 | 5.8633 | 6.1705 | 0.3072 |  |  |
|  | -10.0000 | -10.0092 | -10.2528 | -9.9198 | 0.3331 |  |  |

## E.4.12 Apex: Rz

| Failure <br> Examined | Data |  | Prediction Interval |  |  |  | Accuracy <br> Half Width |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Induced Displacement | Measured | Lower Limit | Upper Limit | Width | Average Width |  |
| Superior <br> (T4) | -1.0000 | -1.0203 | -1.0774 | -0.9305 | 0.1469 | 0.2771 | 0.1386 |
|  | 1.0000 | 1.0229 | 0.9225 | 1.0694 | 0.1469 |  |  |
|  | -3.0000 | -2.9504 | -3.0782 | -2.9296 | 0.1486 |  |  |
|  | 3.0000 | 2.9887 | 2.9215 | 3.0702 | 0.1486 |  |  |
|  | -6.0000 | -6.0215 | -6.0810 | -5.9265 | 0.1545 |  |  |
|  | 6.0000 | 5.9829 | 5.9185 | 6.0730 | 0.1545 |  |  |
|  | -10.0000 | -10.0222 | -10.0873 | -9.9199 | 0.1675 |  |  |
|  | 10.0000 | 9.9879 | 9.9118 | 10.0793 | 0.1675 |  |  |
| Inferior (L1) | -1.0000 | -0.9408 | -1.1572 | -0.7768 | 0.3804 |  |  |
|  | 1.0000 | 0.9608 | 0.8290 | 1.2094 | 0.3804 |  |  |
|  | -3.0000 | -2.8801 | -3.1457 | -2.7607 | 0.3850 |  |  |
|  | 3.0000 | 2.8758 | 2.8129 | 3.1979 | 0.3850 |  |  |
|  | -6.0000 | -5.9309 | -6.1325 | -5.7324 | 0.4001 |  |  |
|  | 6.0000 | 5.9876 | 5.7846 | 6.1847 | 0.4001 |  |  |
|  | -10.0000 | -9.8970 | -10.1217 | -9.6879 | 0.4338 |  |  |
|  | 10.0000 | 10.0333 | 9.7401 | 10.1739 | 0.4338 |  |  |

## E.4.13 Dual: X

|  | Data |  | Prediction Interval |  |  |  | Accuracy |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Failure <br> Examined | Induced <br> Displacement | Measured | Lower <br> Limit | Upper Limit | Width | Width | Half Width |
|  | -0.5000 | -0.5594 | -0.6461 | -0.4631 | 0.1830 |  |  |
|  | 0.5000 | 0.4470 | 0.3553 | 0.5383 | 0.1830 |  |  |
|  | -1.0000 | -1.0166 | -1.1468 | -0.9638 | 0.1831 |  |  |
| Superior | 1.0000 | 0.9141 | 0.8559 | 1.0390 | 0.1831 |  |  |
| (T8) | -5.0000 | -5.0578 | -5.1534 | -4.9684 | 0.1850 |  |  |
|  | 5.0000 | 4.9803 | 4.8606 | 5.0455 | 0.1850 |  |  |
|  | -10.0000 | -10.0768 | -10.1632 | -9.9725 | 0.1907 |  |  |
|  | 10.0000 | 10.0215 | 9.8647 | 10.0554 | 0.1907 |  |  |
|  | -20.0000 | -20.1047 | -20.1879 | -19.9757 | 0.2123 |  |  |
|  | 20.0000 | 19.9133 | 19.8678 | 20.0801 | 0.2123 | 0.1353 | $\mathbf{0 . 0 6 7 7}$ |
|  | 0.5000 | 0.4876 | 0.46730152 | 0.543858101 | 0.0766 |  |  |
|  | -0.5000 | -0.4867 | -0.5323181 | -0.45576152 | 0.0766 |  |  |
|  | 1.0000 | 0.9937 | 0.96709894 | 1.043680305 | 0.0766 |  |  |
|  | -1.0000 | -0.9913 | -1.0321403 | -0.95555894 | 0.0766 |  |  |
|  | 5.0000 | 5.0297 | 4.96518291 | 5.04255329 | 0.0774 |  |  |
|  | -5.0000 | -4.9842 | -5.0310133 | -4.95364291 | 0.0774 |  |  |
|  | 10.0000 | 9.9771 | 9.96207332 | 10.04185908 | 0.0798 |  |  |
|  | -10.0000 | -9.9933 | -10.030319 | -9.95053332 | 0.0798 |  |  |
|  | 20.0000 | 20.0089 | 19.9537661 | 20.04255874 | 0.0888 |  |  |
|  | -20.0000 | -19.9838 | -20.031019 | -19.9422261 | 0.0888 |  |  |

## E.4.14 Dual: Y

| Failure <br> Examined | Data |  | Prediction Interval |  |  |  | Accuracy <br> Half Width |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Induced Displacement | Measured | Lower Limit | Upper Limit | Width | Average Width |  |
| Superior <br> (T8) | -0.5000 | -0.4908 | -0.5069 | -0.4692 | 0.0378 | 0.0414 | 0.0207 |
|  | 0.5000 | 0.5135 | 0.4938 | 0.5315 | 0.0378 |  |  |
|  | -1.0000 | -0.9840 | -1.0073 | -0.9695 | 0.0378 |  |  |
|  | 1.0000 | 1.0123 | 0.9941 | 1.0319 | 0.0378 |  |  |
|  | -5.0000 | -4.9802 | -5.0103 | -4.9721 | 0.0382 |  |  |
|  | 5.0000 | 5.0123 | 4.9967 | 5.0349 | 0.0382 |  |  |
|  | -10.0000 | -9.9944 | -10.0143 | -9.9750 | 0.0394 |  |  |
|  | 10.0000 | 10.0301 | 9.9996 | 10.0389 | 0.0394 |  |  |
|  | -20.0000 | -20.0110 | -20.0235 | -19.9797 | 0.0438 |  |  |
|  | 20.0000 | 20.0152 | 20.0043 | 20.0481 | 0.0438 |  |  |
| Inferior <br> (T8) | 0.5000 | 0.5029 | 0.47192176 | 0.513503797 | 0.0416 |  |  |
|  | -0.5000 | -0.5090 | -0.5283238 | -0.48674176 | 0.0416 |  |  |
|  | 1.0000 | 0.9921 | 0.97203781 | 1.013633308 | 0.0416 |  |  |
|  | -1.0000 | -0.9969 | -1.0284533 | -0.98685781 | 0.0416 |  |  |
|  | 5.0000 | 4.9836 | 4.97280576 | 5.014829818 | 0.0420 |  |  |
|  | -5.0000 | -5.0005 | -5.0296498 | -4.98762576 | 0.0420 |  |  |
|  | 10.0000 | 9.9973 | 9.97337759 | 10.01671357 | 0.0433 |  |  |
|  | -10.0000 | -10.0230 | -10.031534 | -9.98819759 | 0.0433 |  |  |
|  | 20.0000 | 19.9932 | 19.9733871 | 20.02161522 | 0.0482 |  |  |
|  | -20.0000 | -20.0138 | -20.036435 | -19.9882071 | 0.0482 |  |  |

## E.4.15 Dual: Z

| Failure <br> Examined | Data |  | Prediction Interval |  |  |  | Accuracy <br> Half Width |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Induced Displacement | Measured | Lower Limit | Upper Limit | Width | Average Width |  |
| Superior <br> (T8) | -0.5000 | -0.5120 | -0.5322 | -0.3574 | 0.1748 | 0.2200 | 0.1100 |
|  | 0.5000 | 0.5724 | 0.4676 | 0.6424 | 0.1748 |  |  |
|  | -1.0000 | -0.8903 | -1.0321 | -0.8572 | 0.1749 |  |  |
|  | 1.0000 | 1.0578 | 0.9674 | 1.1423 | 0.1749 |  |  |
|  | -5.0000 | -4.9546 | -5.0319 | -4.8552 | 0.1767 |  |  |
|  | 5.0000 | 5.0550 | 4.9655 | 5.1421 | 0.1767 |  |  |
|  | -10.0000 | -9.9018 | -10.0333 | -9.8512 | 0.1822 |  |  |
|  | 10.0000 | 10.0338 | 9.9614 | 10.1436 | 0.1822 |  |  |
|  | -20.0000 | -19.9628 | -20.0410 | -19.8382 | 0.2027 |  |  |
|  | 20.0000 | 20.0536 | 19.9485 | 20.1512 | 0.2027 |  |  |
| Inferior (T8) | 0.5000 | 0.6983 | 0.5255 | 0.7727 | 0.2472 |  |  |
|  | -0.5000 | -0.3528 | -0.4735 | -0.2263 | 0.2472 |  |  |
|  | 1.0000 | 1.1783 | 1.0250 | 1.2723 | 0.2473 |  |  |
|  | -1.0000 | -0.8105 | -0.9731 | -0.7258 | 0.2473 |  |  |
|  | 5.0000 | 5.0653 | 5.0199 | 5.2698 | 0.2499 |  |  |
|  | -5.0000 | -4.8238 | -4.9706 | -4.7207 | 0.2499 |  |  |
|  | 10.0000 | 10.0836 | 10.0112 | 10.2689 | 0.2577 |  |  |
|  | -10.0000 | -9.9036 | -9.9697 | -9.7121 | 0.2577 |  |  |
|  | 20.0000 | 20.1722 | 19.9872 | 20.2739 | 0.2867 |  |  |
|  | -20.0000 | -19.8111 | -19.9747 | -19.6880 | 0.2867 |  |  |

## E.4.16 Dual: Rx

| Failure Examined | Data |  | Prediction Interval |  |  |  | Accuracy <br> Half <br> Width |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Induced Displacement | Measured | Lower <br> Limit | Upper Limit | Width | Average Width |  |
| Superior <br> (T8) | 1.0000 | 1.0196 | 0.9500 | 1.0822 | 0.1322 | 0.1891 | 0.0945 |
|  | -1.0000 | -0.9725 | -1.0461 | -0.9139 | 0.1322 |  |  |
|  | 3.0000 | 3.0637 | 2.9452 | 3.0790 | 0.1338 |  |  |
|  | -3.0000 | -2.9744 | -3.0429 | -2.9091 | 0.1338 |  |  |
|  | 6.0000 | 5.9828 | 5.9366 | 6.0757 | 0.1390 |  |  |
|  | -6.0000 | -5.9846 | -6.0396 | -5.9005 | 0.1390 |  |  |
|  | 10.0000 | 9.9804 | 9.9228 | 10.0736 | 0.1507 |  |  |
|  | -10.0000 | -9.9706 | -10.0375 | -9.8867 | 0.1507 |  |  |
| Inferior (T8) | 1.0000 | 1.1562 | 0.9735 | 1.2012 | 0.2276 |  |  |
|  | -1.0000 | -0.9374 | -1.0236 | -0.7959 | 0.2276 |  |  |
|  | 3.0000 | 3.0910 | 2.9693 | 3.1996 | 0.2304 |  |  |
|  | -3.0000 | -2.9510 | -3.0220 | -2.7917 | 0.2304 |  |  |
|  | 6.0000 | 6.0296 | 5.9604 | 6.1998 | 0.2394 |  |  |
|  | -6.0000 | -5.9088 | -6.0222 | -5.7828 | 0.2394 |  |  |
|  | 10.0000 | 10.1017 | 9.9445 | 10.2041 | 0.2596 |  |  |
|  | -10.0000 | -9.8709 | -10.0265 | -9.7669 | 0.2596 |  |  |

## E.4.17 Dual: Ry

| Failure <br> Examined | Induced <br> Displacement | Measured | Lower <br> Limit | Prediction Interval <br> Upper <br> Limit | Width | Average <br> Width | Half Width |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | 1.0000 | 0.9828 | 0.8653 | 1.0747 | 0.2094 |  |  |
|  | -1.0000 | -1.0358 | -1.1439 | -0.9345 | 0.2094 |  |  |
| Superior | -3.0000 | -2.9730 | -3.1543 | -2.9424 | 0.2119 |  |  |
| (T8) | 3.0000 | 2.9911 | 2.8732 | 3.0851 | 0.2119 |  |  |
|  | 6.0000 | 5.9908 | 5.8828 | 6.1030 | 0.2202 |  |  |
|  | -6.0000 | -6.1093 | -6.1722 | -5.9519 | 0.2202 |  |  |
|  | 10.0000 | 9.9796 | 9.8918 | 10.1306 | 0.2388 |  |  |
|  | -10.0000 | -10.1029 | -10.1997 | -9.9610 | 0.2388 | 0.2741 | $\mathbf{0 . 1 3 7 1}$ |
|  | 1.0000 | 1.0017 | 0.8753 | 1.1875 | 0.3122 |  |  |
|  | -1.0000 | -0.9895 | -1.1386 | -0.8263 | 0.3122 |  |  |
|  | -3.0000 | -2.9912 | -3.1543 | -2.8383 | 0.3160 |  |  |
|  | 3.0000 | 3.0967 | 2.8872 | 3.2032 | 0.3160 |  |  |
|  | 6.0000 | 6.1390 | 5.9018 | 6.2302 | 0.3284 |  |  |
|  | -6.0000 | -5.9685 | -6.1813 | -5.8529 | 0.3284 |  |  |
|  | 10.0000 | 10.0098 | 9.9156 | 10.2717 | 0.3560 |  |  |

## E.4.18 Dual: Rz

| Failure <br> Examined | Induced <br> Displacement | Measured | Lower <br> Limit | Prediction Interval <br> Upper <br> Limit | Width | Average <br> Width | Accuracy |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | 1.0000 | 1.0198 | 0.9285 | 1.0767 | 0.1482 |  |  |
|  | -1.0000 | -1.0246 | -1.0713 | -0.9231 | 0.1482 |  |  |
| Superior Width |  |  |  |  |  |  |  |
| (T8) | 3.0000 | 2.9486 | 2.9274 | 3.0774 | 0.1500 |  |  |
|  | -3.0000 | -2.9899 | -3.0721 | -2.9220 | 0.1500 |  |  |
|  | 6.0000 | 6.0203 | 5.9242 | 6.0801 | 0.1559 |  |  |
|  | -6.0000 | -5.9840 | -6.0747 | -5.9188 | 0.1559 |  |  |
|  | 10.0000 | 10.0201 | 9.9173 | 10.0863 | 0.1690 |  |  |
|  | -10.0000 | -9.9888 | -10.0810 | -9.9119 | 0.1690 | 0.2770 | $\mathbf{0 . 1 3 8 5}$ |
|  | 1.0000 | 0.9409 | 0.7772 | 1.1560 | 0.3788 |  |  |
|  | -1.0000 | -0.9620 | -1.2090 | -0.8302 | 0.3788 |  |  |
|  | 3.0000 | 2.8804 | 2.7611 | 3.1445 | 0.3834 |  |  |
|  | -3.0000 | -2.8766 | -3.1975 | -2.8141 | 0.3834 |  |  |
|  | 6.0000 | 5.9310 | 5.7329 | 6.1314 | 0.3984 |  |  |
|  | -6.0000 | -5.9877 | -6.1844 | -5.7859 | 0.3984 |  |  |
|  | 10.0000 | 9.8961 | 9.6886 | 10.1206 | 0.4320 |  |  |

## E. 5 Precision Data

The raw data for the precision exams collected from MB-RSA are displayed in the tables beyond. This raw data was used to calculate the directional precision using the standard deviation multiplied by the $95 \%$ confidence limit. These calculations are found within Section E.6.

## E.5.1 Caudal: Translation

```
-------- Migration Results -
```

Reference Axis: Automatic

Available scenes:

CREFXOMOR --- X-number: 0 --- Follow-up: Postoperative C P TX2M0R --- X-number: 2 --- Follow-up: Postoperative C P TX3M0R --- X-number: 3 --- Follow-up: Postoperative C P TX4M0R --- X-number: 4 --- Follow-up: Postoperative C P TX5M0R --- X-number: 5 --- Follow-up: Postoperative C P TX6M0R --- X-number: 6 --- Follow-up: Postoperative C P TX1M0R --- X-number: 1 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0194 | -0.0210 | 0.0611 | 0.0039 | -0.0416 | 0.0627 | 7 | 6 | 0.0523 | 0.0407 | 18.5 | 19.8 | 0.1764 |
| 1 | 2 | -0.0242 | 0.0333 | 0.0745 | 0.0460 | 0.0136 | 0.0111 | 7 | 6 | 0.0406 | 0.0420 | 18.5 | 19.8 | 0.1405 |
| 2 | 3 | 0.0368 | -0.0218 | -0.1871 | -0.0514 | 0.0144 | -0.0081 | 7 | 6 | 0.0492 | 0.0275 | 18.5 | 19.9 | 0.2458 |
| 3 | 4 | 0.0006 | -0.0419 | 0.3005 | 0.0668 | -0.0133 | -0.0159 | 7 | 6 | 0.0536 | 0.0111 | 18.5 | 19.8 | 0.3797 |
| 4 | 5 | -0.0667 | 0.0939 | -0.3500 | -0.0573 | -0.0515 | 0.0469 | 7 | 5 | 0.0376 | 0.0504 | 18.5 | 21.6 | 0.4062 |
| 5 | 6 | 0.0677 | -0.0832 | 0.1202 | -0.0185 | 0.0366 | -0.0207 | 7 | 5 | 0.0423 | 0.0426 | 18.6 | 21.6 | 0.1953 |
| 6 | 0 | 0.0142 | 0.0417 | -0.0720 | -0.0016 | 0.0411 | -0.0781 | 7 | 6 | 0.0369 | 0.0182 | 18.6 | 19.8 | 0.1190 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.0067 | -0.0082 | 0.0496 | 0.0274 | 0.0125 | -0.0324 | 7 | 6 | 0.0640 | 0.0407 | 19.3 | 19.8 | 0.1758 |
| 1 | 2 | -0.0229 | 0.0287 | 0.0243 | -0.0006 | -0.0054 | 0.0009 | 7 | 6 | 0.0312 | 0.0420 | 19.4 | 19.8 | 0.0701 |
| 2 | 3 | 0.0259 | -0.0131 | -0.0829 | -0.0273 | -0.0113 | 0.0061 | 7 | 6 | 0.0298 | 0.0275 | 19.3 | 19.9 | 0.1321 |
| 3 | 4 | -0.0049 | -0.0123 | 0.1653 | 0.0747 | 0.0061 | 0.0063 | 7 | 6 | 0.0199 | 0.0111 | 19.3 | 19.8 | 0.1992 |
| 4 | 5 | -0.0318 | 0.0189 | -0.2072 | -0.0862 | -0.0303 | -0.0131 | 7 | 5 | 0.0132 | 0.0504 | 19.3 | 21.6 | 0.2374 |
| 5 | 6 | 0.0274 | -0.0350 | 0.0535 | 0.0193 | 0.0216 | 0.0223 | 7 | 5 | 0.0214 | 0.0426 | 19.4 | 21.6 | 0.0951 |
| 6 | 0 | 0.0048 | 0.0186 | -0.0316 | -0.0196 | 0.0060 | 0.0079 | 7 | 6 | 0.0352 | 0.0182 | 19.4 | 19.8 | 0.0798 |

## E.5.2 Caudal: Rotation

-------- Migration Results ------------
Reference Axis: Automatic
$====================================$
Available scenes:
--------------------------------
CREFX0M0R --- X-number: 0 --- Follow-up: Postoperative
C P RX1M0R --- X-number: 1 --- Follow-up: Postoperative
C P RX2M0R --- X-number: 2 --- Follow-up: Postoperative
C P RX3M0R --- X-number: 3 --- Follow-up: Postoperative
C P RX4M0R --- X-number: 4 --- Follow-up: Postoperative
C P RX5M0R --- X-number: 5 --- Follow-up: Postoperative
C P RX6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0872 | -0.0115 | 0.0371 | -0.0104 | 0.0084 | 0.0240 | 7 | 4 | 0.1528 | 0.0207 | 18.5 | 22.0 | 0.2440 |
| 1 | 2 | 0.0516 | 0.0101 | 0.1895 | 0.0860 | 0.0379 | -0.0046 | 7 | 3 | 0.1663 | 0.0218 | 19.5 | 27.8 | 0.4691 |
| 2 | 3 | Not possi | to calcul | migratio | No Refere | Match |  |  |  |  |  |  |  |  |
| 2 | 4 | -0.3837 | -0.0006 | 0.2000 | 0.1342 | 0.0940 | 0.1015 | 7 | 3 | 0.1511 | 0.0370 | 18.9 | 82.3 | 0.5227 |
| 4 | 5 | 0.0929 | -0.0027 | -0.1020 | 0.1486 | 0.1876 | 0.0887 | 5 | 3 | 0.1072 | 0.0422 | 30.1 | 80.7 | 0.2814 |
| 5 | 6 | Not possi | e to calcul | migratio | No Refere | Match |  |  |  |  |  |  |  |  |
| 5 | 0 | 0.1201 | 0.0134 | -0.1213 | -0.2400 | -0.2719 | -0.1589 | 5 | 5 | 0.1262 | 0.0127 | 32.3 | 31.4 | 0.3610 |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0312 | -0.0332 | 0.0452 | 0.2047 | 0.0895 | -0.0525 | 5 | 4 | 0.0495 | 0.0207 | 32.5 | 22.0 | 0.1314 |
| 1 | 2 | 0.0074 | 0.0430 | 0.0778 | -0.0698 | -0.0916 | 0.0319 | 5 | 3 | 0.0306 | 0.0218 | 31.9 | 27.8 | 0.1391 |
| 2 | 3 | Not possi | e to calcul | migratio | No Refere | Match |  |  |  |  |  |  |  |  |
| 2 | 4 | -0.2644 | -0.0371 | 0.1497 | 0.0444 | 0.0602 | 0.0891 | 6 | 3 | 0.0422 | 0.0370 | 22.1 | 82.3 | 0.3512 |
| 4 | 5 | 0.0582 | 0.0129 | -0.1124 | -0.0118 | -0.1644 | 0.0297 | 6 | 3 | 0.0503 | 0.0422 | 21.6 | 80.7 | 0.2603 |
| 5 | 6 | Not possi | e to calcul | migratio | No Refere | Match |  |  |  |  |  |  |  |  |
| 5 | 0 | 0.0581 | 0.0423 | -0.0282 | -0.0225 | 0.0285 | -0.0231 | 6 | 5 | 0.0359 | 0.0127 | 21.4 | 31.4 | 0.1373 |

## E.5.3 Apex Superior Translation

## -------- Migration Results ------------

Reference Axis: Automatic


## Available scenes:

TREFX0M0R --- X-number: 0 --- Follow-up: Postoperative T P TX1M0R --- X-number: 1 --- Follow-up: Postoperative T P TX2M0R --- X-number: 2 --- Follow-up: Postoperative T P TX3M0R --- X-number: 3 --- Follow-up: Postoperative T P TX4M0R --- X-number: 4 --- Follow-up: Postoperative T P TX5M0R --- X-number: 5 --- Follow-up: Postoperative T P TX6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid <br> Body <br> Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.1391 | -0.0085 | -0.0230 | 0.0246 | -0.0069 | -0.0100 | 7 | 7 | 0.0666 | 0.0400 | 19.7 | 20.5 | 0.1949 |
| 1 | 2 | -0.0172 | 0.0124 | -0.0199 | -0.0235 | -0.0339 | -0.0628 | 7 | 7 | 0.0509 | 0.0300 | 19.8 | 20.4 | 0.1165 |
| 2 | 3 | 0.0323 | 0.0176 | -0.0510 | 0.0210 | 0.0456 | 0.0810 | 7 | 7 | 0.0500 | 0.0328 | 19.7 | 20.4 | 0.1366 |
| 3 | 4 | -0.0285 | -0.0203 | 0.1024 | 0.0285 | -0.1130 | 0.0214 | 7 | 7 | 0.1219 | 0.0340 | 19.8 | 20.6 | 0.3567 |
| 4 | 5 | 0.0369 | 0.0014 | -0.0678 | -0.0470 | 0.1122 | -0.0905 | 7 | 7 | 0.1938 | 0.0295 | 19.8 | 20.6 | 0.5254 |
| 5 | 6 | -0.0496 | 0.0038 | 0.0102 | 0.0120 | 0.0292 | 0.0402 | 7 | 7 | 0.0416 | 0.0271 | 19.9 | 20.5 | 0.0986 |
| 6 | 0 | -0.1132 | -0.0067 | 0.0490 | -0.0156 | -0.0329 | 0.0209 | 7 | 7 | 0.0418 | 0.0497 | 19.7 | 20.4 | 0.1612 |

## E.5.4 Apex Inferior Translation

## -------- Migration Results ------------

Reference Axis: Automatic

## Available scenes:

BREFXOMOR --- X-number: 0 --- Follow-up: Postoperative B P TX1M0R --- X-number: 1 --- Follow-up: Postoperative B P TX2M0R --- X-number: 2 --- Follow-up: Postoperative B P TX3M0R --- X-number: 3 --- Follow-up: Postoperative B P TX4M0R --- X-number: 4 --- Follow-up: Postoperative B P TX5M0R --- X-number: 5 --- Follow-up: Postoperative B P TX6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid Body Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0798 | -0.0266 | -0.0202 | 0.0451 | 0.0718 | -0.0444 | 6 | 7 | 0.0328 | 0.0362 | 20.2 | 19.7 | 0.1134 |
| 1 | 2 | 0.1289 | 0.0252 | -0.0096 | -0.0704 | -0.0223 | 0.0418 | 6 | 7 | 0.0538 | 0.0475 | 20.2 | 19.7 | 0.1594 |
| 2 | 3 | -0.1156 | -0.0237 | 0.0962 | -0.0103 | 0.0771 | -0.0296 | 6 | 7 | 0.0468 | 0.0780 | 20.3 | 19.6 | 0.2236 |
| 3 | 4 | -0.069 | -0.0037 | -0.0552 | 0.0645 | 0.0049 | -0.0412 | 6 | 7 | 0.0247 | 0.0332 | 20.2 | 19.8 | 0.1168 |
| 4 | 5 | 0.1943 | 0.0120 | -0.0699 | 0.0456 | -0.0698 | 0.0780 | 6 | 7 | 0.0185 | 0.0907 | 20.3 | 19.8 | 0.2526 |
| 5 | 6 | 0.0594 | 0.01270 | 0.1041 | -0.0707 | -0.0048 | 0.0337 | 6 | 7 | 0.0211 | 0.0365 | 20.2 | 19.8 | 0.1477 |
| 6 | 0 | -0.1185 | 0.0046 | -0.0451 | -0.0036 | -0.0569 | -0.0385 | 6 | 7 | 0.0225 | 0.0771 | 20.2 | 19.7 | 0.1692 |

## E.5.5 Apex Superior Rotation

-------- Migration Results ------------
Reference Axis: Automatic
$=================================$
Available scenes:
---------------------------
TREFX0M0R --- X-number: 0 --- Follow-up: Postoperative
T P RX1M0R --- X-number: 1 --- Follow-up: Postoperative
T P RX2M0R --- X-number: 2 --- Follow-up: Postoperative
T P RX3M0R --- X-number: 3 --- Follow-up: Postoperative
T P RX4M0R --- X-number: 4 --- Follow-up: Postoperative
T P RX5M0R --- X-number: 5 --- Follow-up: Postoperative
T P RX6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid <br> Body <br> Error <br> Reference | Condition Number |  | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.1135 | 0.0183 | 0.1039 | 0.1284 | 0.0796 | -0.0969 | 7 | 7 | 0.1576 | 0.0526 | 19.7 | 20.5 | 0.4692 |
| 1 | 2 | 0.0245 | -0.0481 | 0.0479 | -0.0921 | -0.1164 | -0.1959 | 7 | 7 | 0.1649 | 0.1018 | 18.8 | 19.7 | 0.3967 |
| 2 | 3 | -0.0002 | 0.0036 | -0.0743 | 0.0485 | 0.0630 | 0.1483 | 7 | 7 | 0.1973 | 0.1072 | 20.3 | 21.4 | 0.3911 |
| 3 | 4 | -0.0192 | -0.0331 | 0.1111 | 0.0150 | 0.1493 | -0.0590 | 7 | 6 | 0.0676 | 0.0890 | 20.4 | 26.5 | 0.2830 |
| 4 | 5 | 0.1418 | 0.0201 | -0.1413 | 0.0602 | -0.0645 | -0.0418 | 7 | 6 | 0.1390 | 0.1219 | 20.9 | 28.0 | 0.3398 |
| 5 | 6 | -0.1293 | 0.0010 | -0.0720 | -0.1384 | -0.0733 | 0.1226 | 7 | 6 | 0.1797 | 0.1158 | 19.2 | 23.6 | 0.3914 |
| 6 | 0 | -0.1497 | 0.0145 | 0.0554 | -0.0384 | -0.0524 | 0.0744 | 7 | 7 | 0.0915 | 0.0676 | 19.3 | 20.4 | 0.2283 |

## E.5.6 Apex Inferior Rotation

-------- Migration Results ------------
Reference Axis: Automatic
=-=================================
Available scenes:
--------------------------
BREFX0M0R --- X-number: 0 --- Follow-up: Postoperative
B P RX1M0R --- X-number: 1 --- Follow-up: Postoperative
B P RX2M0R --- X-number: 2 --- Follow-up: Postoperative
B P RX3M0R --- X-number: 3 --- Follow-up: Postoperative
B P RX4M0R --- X-number: 4 --- Follow-up: Postoperative
B P RX5M0R --- X-number: 5 --- Follow-up: Postoperative
B P RX6M0R --- X-number: 6 --- Follow-up: Postoperative

B P RX6M0R --- X-number: 6 --- Follow-up: Postoperative
Xref Xmig X

Model: L1

| Reference: T8 |  |  |  |  |  |  |  |
| :---: | :---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 1 | 0.0415 | 0.0142 | 0.1860 | -0.2147 | 0.0572 | 0.0155 |
| 1 | 2 | -0.0338 | -0.0282 | -0.0588 | 0.1590 | -0.0261 | -0.0586 |
| 2 | 3 | 0.4099 | 0.0607 | -0.1228 | 0.0131 | 0.0365 | 0.1867 |
| 3 | 4 | -0.1614 | -0.0410 | -0.0324 | -0.0128 | 0.1672 | -0.1033 |
| 4 | 5 | 0.2020 | 0.0161 | -0.0222 | -0.0990 | -0.2043 | 0.1294 |
| 5 | 6 | -0.1155 | -0.0232 | 0.0063 | 0.1348 | -0.1539 | -0.0065 |
| 6 | 0 | -0.1844 | -0.0063 | -0.4408 | 0.1873 | 0.2610 | -0.0761 |


| \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition Number Reference Model | Maximum <br> Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 7 | 0.0326 | 0.0822 | 25.1 | 19.7 | 0.2640 |
| 5 | 6 | 0.0322 | 0.0761 | 26.7 | 21.0 | 0.1332 |
| 6 | 6 | 0.1147 | 0.0349 | 20.3 | 22.0 | 0.5392 |
| 7 | 6 | 0.0255 | 0.2001 | 17.0 | 25.1 | 0.2634 |
| 5 | 6 | 0.0203 | 0.1660 | 23.7 | 27.3 | 0.2644 |
| 5 | 4 | 0.0299 | 0.0661 | 28.7 | 42.2 | 0.1824 |
| 5 | 4 | 0.0216 | 0.0584 | 24.1 | 38.1 | 0.6048 |

## E.5.7 Dual Superior Translation

## -------- Migration Results ------------

Reference Axis: Automatic
=======================================

Available scenes:
TREFX0M0R --- X-number: 0 --- Follow-up: Postoperative T P TX1M0R --- X-number: 1 --- Follow-up: Postoperative T P TX2M0R --- X-number: 2 --- Follow-up: Postoperative T P TX3M0R --- X-number: 3 --- Follow-up: Postoperative T P TX4M0R --- X-number: 4 --- Follow-up: Postoperative T P TX5M0R --- X-number: 5 --- Follow-up: Postoperative T P TX6M0R --- X-number: 6 --- Follow-up: Postoperative

| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body Error | Rigid <br> Body <br> Error Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total <br> Point <br> Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.1217 | -0.0026 | 0.0736 | -0.0247 | 0.0069 | 0.0100 | 7 | 7 | 0.0400 | 0.0666 | 20.5 | 19.7 | 0.1880 |
| 1 | 2 | 0.1298 | -0.0211 | -0.0176 | 0.0235 | 0.0340 | 0.0628 | 7 | 7 | 0.0300 | 0.0509 | 20.4 | 19.8 | 0.1519 |
| 2 | 3 | -0.1772 | -0.0030 | 0.0804 | -0.0211 | -0.0455 | -0.0810 | 7 | 7 | 0.0328 | 0.0500 | 20.4 | 19.7 | 0.2535 |
| 3 | 4 | -0.0523 | 0.0163 | -0.0159 | -0.0284 | 0.1130 | -0.0213 | 7 | 7 | 0.0340 | 0.1219 | 20.6 | 19.8 | 0.1230 |
| 4 | 5 | 0.1805 | -0.0095 | -0.0551 | 0.0471 | -0.1121 | 0.0906 | 7 | 7 | 0.0295 | 0.1938 | 20.6 | 19.8 | 0.2437 |
| 5 | 6 | -0.0200 | 0.0028 | 0.0058 | -0.0120 | -0.0292 | -0.0402 | 7 | 7 | 0.0271 | 0.0416 | 20.5 | 19.9 | 0.0678 |
| 6 | 0 | 0.0606 | 0.0176 | -0.0711 | 0.0156 | 0.0329 | -0.0209 | 7 | 7 | 0.0497 | 0.0418 | 20.4 | 19.7 | 0.1970 |

## E.5.8 Dual Inferior Translation

-------- Migration Results -------------
Reference Axis: Automatic
$=====================================$
Available scenes:
----------------------------------
BREFX0M0R --- X-number: 0 --- Follow-up: Postoperative
B P TX1M0R --- X-number: 1 --- Follow-up: Postoperative
B P TX2M0R --- X-number: 2 --- Follow-up: Postoperative
B P TX3M0R --- X-number: 3 --- Follow-up: Postoperative
B P TX4M0R --- X-number: 4 --- Follow-up: Postoperative
B P TX5M0R --- X-number: 5 --- Follow-up: Postoperative
B P TX6M0R --- X-number: 6 --- Follow-up: Postoperative

B P TX6M0R --- X-number: 6 --- Follow-up: Postoperative
Xref Xmig X

Model: T8

| Reference: L1 |  |  |  |  |  |  |  |
| :---: | :---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 1 | -0.0406 | 0.0149 | -0.1209 | -0.0450 | -0.0718 | 0.0444 |
| 1 | 2 | -0.0135 | -0.0131 | 0.2105 | 0.0705 | 0.0222 | -0.0418 |
| 2 | 3 | 0.0367 | 0.0177 | -0.0843 | 0.0103 | -0.0771 | 0.0296 |
| 3 | 4 | -0.0453 | -0.0082 | -0.1254 | -0.0645 | -0.0049 | 0.0411 |
| 4 | 5 | 0.0198 | 0.0033 | -0.0414 | -0.0455 | 0.0699 | -0.0780 |
| 5 | 6 | 0.0342 | -0.0022 | 0.0938 | 0.0707 | 0.0048 | -0.0337 |
| 6 | 0 | 0.0089 | -0.0129 | 0.0674 | 0.0035 | 0.0569 | 0.0385 |

\#Matched

Markers \begin{tabular}{c}
\#Matched <br>
Reference <br>
Markers

 

Rigid <br>
Body <br>
Error

 

Rigid <br>
Body <br>
Error <br>
Reference

 

Condition <br>
Number

 


| Number |
| :---: |
| Reference |
| Model |


 


| Maximum |
| :---: |
| Total |
| Point |
| Motion | <br>

<br>
\end{tabular}

## E.5.9 Dual Superior Rotation



| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched Reference Markers | Rigid <br> Body <br> Error | Rigid <br> Body <br> Error <br> Reference | Condition Number |  | Maximum Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: T4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0.1052 | -0.0878 | 0.1290 | -0.1283 | -0.0798 | 0.0967 | 7 | 7 | 0.0526 | 0.1576 | 20.5 | 19.7 | 0.2415 |
| 1 | 2 | 0.2658 | 0.0590 | -0.1907 | 0.0917 | 0.1167 | 0.1957 | 7 | 7 | 0.1018 | 0.1649 | 19.7 | 18.8 | 0.5557 |
| 2 | 3 | -0.2750 | 0.0304 | 0.1501 | -0.0487 | -0.0629 | -0.1484 | 7 | 7 | 0.1072 | 0.1973 | 21.4 | 20.3 | 0.5034 |
| 3 | 4 | 0.1859 | 0.0287 | -0.0803 | -0.0148 | -0.1493 | 0.0590 | 6 | 7 | 0.0890 | 0.0676 | 26.5 | 20.4 | 0.3612 |
| 4 | 5 | -0.0548 | -0.0323 | 0.2855 | -0.0602 | 0.0644 | 0.0418 | 6 | 7 | 0.1219 | 0.1390 | 28.0 | 20.9 | 0.4198 |
| 5 | 6 | -0.1429 | 0.0859 | -0.1832 | 0.1385 | 0.0730 | -0.1228 | 6 | 7 | 0.1158 | 0.1797 | 23.6 | 19.2 | 0.3896 |
| 6 | 0 | -0.0098 | 0.0437 | -0.0967 | 0.0385 | 0.0524 | -0.0745 | 7 | 7 | 0.0676 | 0.0915 | 20.4 | 19.3 | 0.2513 |

## E.5.10 Dual Inferior Rotation



| Xref | Xmig | X | Y | Z | Rx | Ry | Rz | \#Matched Markers | \#Matched <br> Reference <br> Markers | Rigid Body Error | Rigid <br> Body <br> Error <br> Reference | Condition Number | Condition <br> Number <br> Reference <br> Model | Maximum <br> Total Point Motion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model: T8 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Reference: L1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | -0.0045 | -0.0350 | 0.4075 | 0.2147 | -0.0572 | -0.0153 | 7 | 5 | 0.0822 | 0.0326 | 19.7 | 25.1 | 0.5844 |
| 1 | 2 | -0.1156 | 0.0967 | -0.3768 | -0.1590 | 0.0259 | 0.0586 | 6 | 5 | 0.0761 | 0.0322 | 21.0 | 26.7 | 0.5771 |
| 2 | 3 | 0.1129 | -0.0169 | 0.0773 | -0.0133 | -0.0364 | -0.1868 | 6 | 6 | 0.0349 | 0.1147 | 22.0 | 20.3 | 0.2284 |
| 3 | 4 | -0.0935 | -0.0359 | -0.0602 | 0.0131 | -0.1672 | 0.1033 | 6 | 7 | 0.2001 | 0.0255 | 25.1 | 17.0 | 0.4662 |
| 4 | 5 | 0.0875 | 0.0570 | 0.3588 | 0.0994 | 0.2040 | -0.1298 | 6 | 5 | 0.1660 | 0.0203 | 27.3 | 23.7 | 0.6663 |
| 5 | 6 | 0.0691 | -0.0032 | -0.3382 | -0.1348 | 0.1539 | 0.0068 | 4 | 5 | 0.0661 | 0.0299 | 42.2 | 28.7 | 0.4855 |
| 6 | 0 | 0.0018 | -0.0159 | -0.0403 | -0.1870 | -0.2612 | 0.0759 | 4 | 5 | 0.0584 | 0.0216 | 38.1 | 24.1 | 0.2006 |

## E. 6 Precision Calculations

## E.6.1 Caudal Precision

| Superior <br> Precision | X | Y | Z | Rx | Ry | Rz | MTPM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Translation | -0.0194 | -0.021 | 0.0611 | 0.0039 | -0.0416 | 0.0627 | 0.1764 |
|  | -0.0242 | 0.0333 | 0.0745 | 0.046 | 0.0136 | 0.0111 | 0.1405 |
|  | 0.0368 | -0.0218 | -0.1871 | -0.0514 | 0.0144 | -0.0081 | 0.2458 |
|  | 0.0006 | -0.0419 | 0.3005 | 0.0668 | -0.0133 | -0.0159 | 0.3797 |
|  | -0.0667 | 0.0939 | -0.35 | -0.0573 | -0.0515 | 0.0469 | 0.4062 |
|  | 0.0677 | -0.0832 | 0.1202 | -0.0185 | 0.0366 | -0.0207 | 0.1953 |
|  | 0.0142 | 0.0417 | -0.072 | -0.0016 | 0.0411 | -0.0781 | 0.119 |
| Rotation | -0.0872 | -0.0115 | 0.0371 | -0.0104 | 0.0084 | 0.024 | 0.244 |
|  | 0.0516 | 0.0101 | 0.1895 | 0.086 | 0.0379 | -0.0046 | 0.4691 |
|  | -0.3837 | -0.0006 | 0.2 | 0.1342 | 0.094 | 0.1015 | 0.5227 |
|  | 0.0929 | -0.0027 | -0.102 | 0.1486 | 0.1876 | 0.0887 | 0.2814 |
|  | 0.1201 | 0.0134 | -0.1213 | -0.24 | -0.2719 | -0.1589 | 0.361 |
| Standard Deviation | 0.1310 | 0.0444 | 0.1852 | 0.1032 | 0.1075 | 0.0719 | 0.1315 |
| Precision | 0.2804 | 0.0950 | 0.3963 | 0.2208 | 0.2301 | 0.1539 | 0.2813 |


| Inferior <br> Precision | X | Y | Z | Rx | Ry | Rz | MTPM |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | 0.0067 | -0.0082 | 0.0496 | 0.0274 | 0.0125 | -0.0324 | 0.1758 |
|  | -0.0229 | 0.0287 | 0.0243 | -0.0006 | -0.0054 | 0.0009 | 0.0701 |
| Translation | 0.0259 | -0.0131 | -0.0829 | -0.0273 | -0.0113 | 0.0061 | 0.1321 |
|  | -0.0049 | -0.0123 | 0.1653 | 0.0747 | 0.0061 | 0.0063 | 0.1992 |
|  | -0.0318 | 0.0189 | -0.2072 | -0.0862 | -0.0303 | -0.0131 | 0.2374 |
|  | 0.0274 | -0.035 | 0.0535 | 0.0193 | 0.0216 | 0.0223 | 0.0951 |
|  | 0.0048 | 0.0186 | -0.0316 | -0.0196 | 0.006 | 0.0079 | 0.0798 |
|  | -0.0312 | -0.0332 | 0.0452 | 0.2047 | 0.0895 | -0.0525 | 0.1314 |
|  | 0.0074 | 0.043 | 0.0778 | -0.0698 | -0.0916 | 0.0319 | 0.1391 |
| Rotation | -0.2644 | -0.0371 | 0.1497 | 0.0444 | 0.0602 | 0.0891 | 0.3512 |
|  | 0.0582 | 0.0129 | -0.1124 | -0.0118 | -0.1644 | 0.0297 | 0.2603 |
|  | 0.0581 | 0.0423 | -0.0282 | -0.0225 | 0.0285 | -0.0231 | 0.1373 |
| Standard | 0.0844 | 0.0292 | 0.1075 | 0.0758 | 0.0668 | 0.0364 | 0.0826 |
| Deviation | $\mathbf{0 . 1 8 0 7}$ | $\mathbf{0 . 0 6 2 5}$ | $\mathbf{0 . 2 3 0 0}$ | $\mathbf{0 . 1 6 2 2}$ | $\mathbf{0 . 1 4 3 0}$ | $\mathbf{0 . 0 7 7 8}$ | $\mathbf{0 . 1 7 6 7}$ |

## E.6.2 Apex Precision

| Superior Precision | X | Y | Z | Rx | Ry | Rz | MTPM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Translation | 0.1391 | -0.0085 | -0.023 | 0.0246 | -0.0069 | -0.01 | 0.1949 |
|  | -0.0172 | 0.0124 | -0.0199 | -0.0235 | -0.0339 | -0.0628 | 0.1165 |
|  | 0.0323 | 0.0176 | -0.051 | 0.021 | 0.0456 | 0.081 | 0.1366 |
|  | -0.0285 | -0.0203 | 0.1024 | 0.0285 | -0.113 | 0.0214 | 0.3567 |
|  | 0.0369 | 0.0014 | -0.0678 | -0.047 | 0.1122 | -0.0905 | 0.5254 |
|  | -0.0496 | 0.0038 | 0.0102 | 0.012 | 0.0292 | 0.0402 | 0.0986 |
|  | -0.1132 | -0.0067 | 0.049 | -0.0156 | -0.0329 | 0.0209 | 0.1612 |
| Rotation | 0.1135 | 0.0183 | 0.1039 | 0.1284 | 0.0796 | -0.0969 | 0.4692 |
|  | 0.0245 | -0.0481 | 0.0479 | -0.0921 | -0.1164 | -0.1959 | 0.3967 |
|  | -0.0002 | 0.0036 | -0.0743 | 0.0485 | 0.063 | 0.1483 | 0.3911 |
|  | -0.0192 | -0.0331 | 0.1111 | 0.015 | 0.1493 | -0.059 | 0.283 |
|  | 0.1418 | 0.0201 | -0.1413 | 0.0602 | -0.0645 | -0.0418 | 0.3398 |
|  | -0.1293 | 0.001 | -0.072 | -0.1384 | -0.0733 | 0.1226 | 0.3914 |
|  | -0.1497 | 0.0145 | 0.0554 | -0.0384 | -0.0524 | 0.0744 | 0.2283 |
| Standard Deviation | 0.0925 | 0.0203 | 0.0786 | 0.0661 | 0.0827 | 0.0947 | 0.1376 |
| Precision | 0.1979 | 0.0434 | 0.1681 | 0.1414 | 0.1770 | 0.2028 | 0.2944 |


| Inferior <br> Precision | X | Y | Z | Rx | Ry | Rz | MTPM |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | -0.0798 | -0.0266 | -0.0202 | 0.0451 | 0.0718 | -0.0444 | 0.1134 |
|  | 0.1289 | 0.0252 | -0.0096 | -0.0704 | -0.0223 | 0.0418 | 0.1594 |
|  | -0.1156 | -0.0237 | 0.0962 | -0.0103 | 0.0771 | -0.0296 | 0.2236 |
| Translation | -0.069 | -0.0037 | -0.0552 | 0.0645 | 0.0049 | -0.0412 | 0.1168 |
|  | 0.1943 | 0.012 | -0.0699 | 0.0456 | -0.0698 | 0.078 | 0.2526 |
|  | 0.0594 | 0.0127 | 0.1041 | -0.0707 | -0.0048 | 0.0337 | 0.1477 |
|  | -0.1185 | 0.0046 | -0.0451 | -0.0036 | -0.0569 | -0.0385 | 0.1692 |
|  | 0.0415 | 0.0142 | 0.1860 | -0.2147 | 0.0572 | 0.0155 | 0.2640 |
|  | -0.0338 | -0.0282 | -0.0588 | 0.1590 | -0.0261 | -0.0586 | 0.1332 |
|  | 0.4099 | 0.0607 | -0.1228 | 0.0131 | 0.0365 | 0.1867 | 0.5392 |
| Rotation | -0.1614 | -0.0410 | -0.0324 | -0.0128 | 0.1672 | -0.1033 | 0.2634 |
|  | 0.2020 | 0.0161 | -0.0222 | -0.0990 | -0.2043 | 0.1294 | 0.2644 |
|  | -0.1155 | -0.0232 | 0.0063 | 0.1348 | -0.1539 | -0.0065 | 0.2266 |
|  | -0.1844 | -0.0063 | -0.4408 | 0.1873 | 0.2610 | -0.0767 | 0.6048 |
| Standard | 0.1709 | 0.0269 | 0.1422 | 0.1078 | 0.1194 | 0.0815 | 0.1485 |
| Deviation | $\mathbf{0 . 3 6 5 7}$ | $\mathbf{0 . 0 5 7 7}$ | $\mathbf{0 . 3 0 4 3}$ | $\mathbf{0 . 2 3 0 7}$ | $\mathbf{0 . 2 5 5 4}$ | $\mathbf{0 . 1 7 4 4}$ | $\mathbf{0 . 3 1 7 7}$ |

## E.6.3 Dual Precision

| Superior Precision | X | Y | Z | Rx | Ry | Rz | MTPM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Translation | -0.1217 | -0.0026 | 0.0736 | -0.0247 | 0.0069 | 0.01 | 0.188 |
|  | 0.1298 | -0.0211 | -0.0176 | 0.0235 | 0.034 | 0.0628 | 0.1519 |
|  | -0.1772 | -0.003 | 0.0804 | -0.0211 | -0.0455 | -0.081 | 0.2535 |
|  | -0.0523 | 0.0163 | -0.0159 | -0.0284 | 0.113 | -0.0213 | 0.123 |
|  | 0.1805 | -0.0095 | -0.0551 | 0.0471 | -0.1121 | 0.0906 | 0.2437 |
|  | -0.02 | 0.0028 | 0.0058 | -0.012 | -0.0292 | -0.0402 | 0.0678 |
|  | 0.0606 | 0.0176 | -0.0711 | 0.0156 | 0.0329 | -0.0209 | 0.197 |
| Rotation | 0.1052 | -0.0878 | 0.129 | -0.1283 | -0.0798 | 0.0967 | 0.2415 |
|  | 0.2658 | 0.059 | -0.1907 | 0.0917 | 0.1167 | 0.1957 | 0.5557 |
|  | -0.275 | 0.0304 | 0.1501 | -0.0487 | -0.0629 | -0.1484 | 0.5034 |
|  | 0.1859 | 0.0287 | -0.0803 | -0.0148 | -0.1493 | 0.059 | 0.3612 |
|  | -0.0548 | -0.0323 | 0.2855 | -0.0602 | 0.0644 | 0.0418 | 0.4198 |
|  | -0.1429 | 0.0859 | -0.1832 | 0.1385 | 0.073 | -0.1228 | 0.3896 |
|  | -0.0098 | 0.0437 | -0.0967 | 0.0385 | 0.0524 | -0.0745 | 0.2513 |
| Standard <br> Deviation | 0.1563 | 0.0423 | 0.1321 | 0.0661 | 0.0827 | 0.0947 | 0.1441 |
| Precision | 0.3344 | 0.0905 | 0.2828 | 0.1414 | 0.1771 | 0.2027 | 0.3083 |


| Inferior <br> Precision | X | Y | Z | Rx | Ry | Rz | MTPM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | -0.0406 | 0.0149 | -0.1209 | -0.045 | -0.0718 | 0.0444 | 0.1922 |
|  | -0.0135 | -0.0131 | 0.2105 | 0.0705 | 0.0222 | -0.0418 | 0.2577 |
| Translation | 0.0367 | 0.0177 | -0.0843 | 0.0103 | -0.0771 | 0.0296 | 0.1449 |
|  | -0.0453 | -0.0082 | -0.1254 | -0.0645 | -0.0049 | 0.0411 | 0.1815 |
|  | 0.0198 | 0.0033 | -0.0414 | -0.0455 | 0.0699 | -0.078 | 0.2736 |
|  | 0.0342 | -0.0022 | 0.0938 | 0.0707 | 0.0048 | -0.0337 | 0.1592 |
|  | 0.0089 | -0.0129 | 0.0674 | 0.0035 | 0.0569 | 0.0385 | 0.1308 |
|  | -0.0045 | -0.0350 | 0.4075 | 0.2147 | -0.0572 | -0.0153 | 0.5844 |
|  | -0.1156 | 0.0967 | -0.3768 | -0.1590 | 0.0259 | 0.0586 | 0.5771 |
| Rotation | 0.1129 | -0.0169 | 0.0773 | -0.0133 | -0.0364 | -0.1868 | 0.2284 |
|  | -0.0935 | -0.0359 | -0.0602 | 0.0131 | -0.1672 | 0.1033 | 0.4662 |
|  | 0.0875 | 0.0570 | 0.3588 | 0.0994 | 0.2040 | -0.1298 | 0.6663 |
|  | 0.0691 | -0.0032 | -0.3382 | -0.1348 | 0.1539 | 0.0068 | 0.4855 |
|  | 0.0018 | -0.0159 | -0.0403 | -0.1870 | -0.2612 | 0.0759 | 0.2006 |
| Standard | 0.0644 | 0.0356 | 0.2252 | 0.1078 | 0.1193 | 0.0815 | 0.1883 |
| Deviation | $\mathbf{0 . 1 3 7 8}$ | $\mathbf{0 . 0 7 6 2}$ | $\mathbf{0 . 4 8 1 9}$ | $\mathbf{0 . 2 3 0 7}$ | $\mathbf{0 . 2 5 5 4}$ | $\mathbf{0 . 1 7 4 4}$ | $\mathbf{0 . 4 0 2 9}$ |
| Precision |  |  |  |  |  |  |  |

## Appendix F - Plots

## F. 1 Simulation Validation

## F.1.1 Check for Normalcy

The plots in this section assess the distribution of the precision data sets. P-values less than $\mathbf{0 . 0 5}$ indicate non-parametric datasets.

## F.1.1.1 Phantom - Superior









## F.1.1.2 Phantom - Inferior









## F.1.1.3 Simulation - Superior









## F.1.1.4 Simulation - Inferior









## F.1.2 Variance Comparison

The comparison of the origin style was done using either the F-Test or Levene test. The use of the F-Test was reserved for cases where the data sets for both the phantom and simulated models were normally distributed. If one or both data sets were non-parametrically distributed the Levene test was used. For each of the following plots the utilized test is indicated. P-values above $\mathbf{0 . 0 5}$ indicate no statistically significant differences between the two models.

## F.1.2.1 Superior Assessment






## F.1.2.2 Inferior Assessment






## F. 2 Accuracy Plots

These are Bland-Altman plots comparing the measured values of each origin style to the reference inputted displacement. Each plot shows the mean for the set of data. This is the green horizontal line. For each plot the Limits of Clinical Significance are the maximum and minimum of the ordinate axis. For a measurement technique to agree with the true value the limits of agreement must be within the Limits of Clinical Significance. The Limits of Clinical Significance are the maxima and minima of the ordinate axis of each BA plot. The limits of agreement are shown by the red lines labeled ULA and LLA representing the Upper Limit of Agreement and Lower Limit of Agreement respectively. These limits are located $\pm 1.96 *$ SD from the mean and show $95 \%$ confidence. The black data points are those which fall within the limits of agreement while the red data points are ones which fall outside these limits.

## F.2.1 X Accuracy - Translation along the X Axis



## F.2.2 Y Accuracy - Translation along the Y Axis





## F.2.3 Z Accuracy - Translation along the Z Axis





## F.2.4 Rx Accuracy - Rotation around the X Axis





## F.2.5 Ry Accuracy - Rotation around the Y Axis





## F.2.6 Rz Accuracy - Rotation around the Z Axis





## F.2.7 Translational Accuracy Comparison



## F.2.8 Rotational Accuracy Comparison



## F. 3 Precision Plots

## F.3.1 Check for Normalcy

The plots in this section assess the distribution of the precision data sets. P-values less than $\mathbf{0 . 0 5}$ indicate non-parametric datasets.

## F.3.1.1 Superior - Caudal









## F.3.1.2 Superior - Apex









## F.3.1.3 Superior - Dual









## F.3.1.4 Inferior - Caudal









## F.3.1.5 Inferior - Apex









## F.3.1.6 Inferior - Dual









## F.3.2 Variance Comparison

The comparison of the origin style was done using either a Bartlett or Levene test. The use of the Bartlett test was reserved for cases where the data sets for all three origin styles were normally distributed. If one or more data sets were non-parametrically distributed the Levene test was used. For each of the following plots the utilized test is indicated. P-values above $\mathbf{0 . 0 5}$ indicate no statistically significant differences between the three origin styles.

## F.3.2.1 Superior Assessment







## F.3.2.2 Assessment of Apex Vs. Dual for Statistically Different Superior <br> Precision



## F.3.2.3 Inferior Assessment







## F.3.2.4 Assessment of Apex Vs. Dual for Statistically Different Inferior

 Precision


## Appendix G-Original Thesis Work

This thesis work has been a continuation of the project started with this research group by A. Francis in 2009 [27]. During the course of this project there has been significant advancements made to the simulation process as well as a simulation validation component and an accuracy and precision assessment component. The original work conducted during the course of creating this thesis has been listed here. All of the following changes, improvements and additions had the potential to significantly impact the results of the project.
i. Refining the marker placement protocol to use anatomical measurements available to surgeons during operations. This is a change from the precise (submillimetre) placement dimensions published by Francis (2009) [27]. This refinement affects the marker placement options and thus potentially affects the accuracy and precision of the RSA measurements.
ii. Significant modifications to the simulation process originally developed at this institution by Francis (2009) [27]. The significant modifications include:
a. The use of a linear attenuation factor to produce image contrast. This is a significant improvement over the previous method surface attenuation method. The implementation of this new process greatly effects image spatial resolution and better simulates the physical RSA environment.
b. Created a calibration box native to the simulation environment which eliminated the errors associated with previously used CAD created calibration box. The previous simulated calibration box used the nominal
positions of the calibration markers instead of actual positions defined by HBI and used by the RSA software. This change impacts the accuracy of the RSA measurements.

## iii. Validation of the Simulated RSA Environment

a. Construction and imaging of a new phantom model used to assess the validity of the simulated environment.
b. Construction of and imaging of a new simulated model developed from a CT scan of the physical phantom to match marker placement in both environments.
c. Parallel precision studies of the two models to assess the validity of the simulated RSA environment. This included 35 RSA image pairs: 18 image sets of the physical phantom and 17 image sets of the simulated model. Each study produced 19 data points to assess system precision. Analysis of equal variance and was used to assess simulation validity.
iv. Creation of two novel origin styles, the Apex and Dual Origin Styles, to compensate for the limited imaging area present in the Halifax RSA suite. These origin styles are unique to this thesis alone.
v. Assessment of the Accuracy and Precision of three origin styles (Caudal, Apex and Dual)
a. Changed the methodology from the previous project work of how accuracy and precision was calculated compared to the methods used by the previous project. The new methods used are based on those described in the literature by Madanat et al (2005, 2007), Laende et al (2009),

Bragdon et al (2002), Önsten et al (2001) and Allen et al (2004) [26], [34], [59-61], [63].
b. Creation and analysis of approximately 300 original simulated RSA image sets (approximately 460 data points as the RSA exams are used twice for the Apex and Dual Origin Styles) for the assessment of the accuracy and precision of the Caudal, Apex and Dual Origin Styles.
c. Statistical methods to assess the agreement of the three origin styles not previously used in this project. To compare accuracy measurements Bland-Altman plots were used and analysis of equal variance was used to assess the agreement between precision measurements. The use of these statistics is based on their use by Bland and Altman (1986) and their use in RSA by Laende et al (2009) [4], [61].

Along with the major original material, additional minor improvements were made to the simulation.
i. Complete reconstruction of the vertebral and spinal models to better reflect the recorded measurements published by Panjabi et al (1991, 1992) [67], [68]. The models are now entirely based on the measurements reported in these two papers.
ii. Additional refinements were made to the simulation process:
a. Refined how the simulated images are created using a different file structure method to improve coding and usability.
b. Improved the ease of use of model placement in the CAD RSA environment increasing usability of the simulation process.

## Appendix H-Permission for Publication

This thesis contains work not originally created by this researcher. I would like to thank Elise Laende and Antony Francis for their assistance and their permission to publicise their works.

Images Figure 1.12 and Figure 1.14 located on pages 41 and 44 were originally created by Antony Francis in his Master’s thesis entitled: "Simulation of a Standardized Bead Placement Protocol for Radiostereometric Analysis of Thoracic Spinal Fusion" published in 2009 [27]. These images show the image simulation process and marker placement protocol developed over the course of his project.

The matrix mathematical equations presented in Section 3.2.4.1, starting on page 74, were originally developed by Elise Laende for her Master's thesis entitled: "Radiostereometric Analysis of Migration and Inducible Displacement for the Evaluation of Total Knee Replacement Fixation" published in 2006 [29]. I would also like to thank Elise for the use of her LocalMigration Function for MatLab. The code for this function, with her permission, has been included in Section D.2.3, starting on page 244.

February 22, 2012

## Antony Bou Francis,

Marie Curie Research Fellow / PhD Student
School of Mechanical Engineering
University of Leeds
Leeds, UK
LS2 9JT
I am preparing my M.A.Sc. thesis for submission to the Faculty of Graduate Studies at Dalhousie University, Halifax, Nova Scotia, Canada. I am seeking your permission to include images produced for your thesis entitled:

Simulation of a Standardized Bead Placement Protocol for Radiostereometric Analysis of Thoracic Spinal Fusion

Canadian graduate theses are reproduced by the Library and Archives of Canada (formerly National Library of Canada) through a non-exclusive, world-wide license to reproduce, loan, distribute, or sell theses. I am also seeking your permission for the material described above to be reproduced and distributed by the LAC (NLC). Further details about the LAC (NLC) thesis program are available on the LAC (NLC) website (www.nlc-bnc.ca)

Full Publication details and a copy of this permission letter will be included in the thesis.

Sincerely,

Alan Spurway

Permission is granted for:
a) The inclusion of the material described above in A. Spurway's thesis.
b) For the material described above to be included in the copy of A. Spurway's thesis that is sent to the Library and Archives of Canada (formerly National Library of Canada) for reproduction and distribution.

Name: $\qquad$
Signature: $\qquad$

Title: $\qquad$
Date: $\qquad$

March 08, 2012

## Elise Laende

6068 Cherry St.
Halifax, NS
B3H 2K3
I am preparing my M.A.Sc. thesis for submission to the Faculty of Graduate Studies at Dalhousie University, Halifax, Nova Scotia, Canada. I am seeking your permission to include the mathematical equations published in the Mathematical Steps of Micromotion Calculations for RSA Appendix produced for your thesis entitled:

Radiostereometric Analysis of Migration and Inducible Displacement for the Evaluation of Total Knee Replacement Fixation

I am also seeking your permission to include the coding to your Matlab Program:

## LocalMigration Function

Canadian graduate theses are reproduced by the Library and Archives of Canada (formerly National Library of Canada) through a non-exclusive, world-wide license to reproduce, loan, distribute, or sell theses. I am also seeking your permission for the material described above to be reproduced and distributed by the LAC(NLC). Further details about the LAC(NLC) thesis program are available on the LAC(NLC) website (www.nlc-bnc.ca)

Full Publication details and a copy of this permission letter will be included in the thesis.

Sincerely,

## Alan Spurway

Permission is granted for:
a) The inclusion of the material described above in A. Spurway's thesis.
b) For the material described above to be included in the copy of A. Spurway's thesis that is sent to the Library and Archives of Canada (formerly National Library of Canada) for reproduction and distribution.

Name: $\qquad$
Signature: $\qquad$

Title: $\qquad$
Date: $\qquad$

# PERMISSION LICENSE AGREEMENT 

P3607.JBJSInc.JBJS Am.Lenke.887.Dalhousie University.Spurway

$$
4 / 3 / 2012
$$

Mr, Alan J. Spurway
INVOICE
ATTACHED
Dalhousie University
,

Dear Mr. Spurway,
Thank you for your interest in JBJS [Am] material. Please note: This permission does not apply to any figure or other material that is credited to any source other than JBJS. It is your responsibility to validate that the material is in fact owned by JBJS. If material within JBJS material is credited to another source (in a figure legend, for example) then any permission extended by JBJS is invalid. We encourage you to view the actual material at www.ejbjs org or a library or other source. Information provided by third parties as to credits that may or may not be associated with the material may be unreliable.

We are pleased to grant you non-exclusive, nontransferable permission, limited to the format described below, and provided you meet the criteria below. Such permission is for one-time use and does not include permission for future editions, revisions, additional printings, updates, ancillaries, customized forms, any electronic forms, Braille editions, translations or promotional pieces unless otherwise specified below. We must be contacted for permission each time such use is planned. This permission does not include the right to modify the material. Use of the material must not imply any endorsement by the copyright owner. This permission is not valid for the use of JBJS logos or other collateral material.
Abstracts or collections of abstracts and all translations must be approved by publisher's agent in advance, and in the case of translations, before printing. No financial liability for the project will devolve upon JBJS, Inc. or on Rockwater, Inc., All expenses for translation, validation of translation accuracy, publication costs and reproduction costs are the sole responsibility of the foreign language sponsor. The new work must be reprinted and delivered as a stand-alone piece and may not be integrated or bound with other material. JBJS does not supply photos or artwork; these may be downloaded from the JBJS website, scanned, or (if available) obtained from the author of the article.

## PERMISSION IS VALID FOR THE FOLLOWING MATERIAL ONLY:

## Figure 3

Journal of Bone and Joint Surgery Amercian, , 2001, 83, 8, Adolescent idiopathic scoliosis: a new
classification to determine extent of spinal arthrodesis, Lenke, 1169-1181

## IN THE FOLLOWING WORK ONLY:

electronic and/or print copies of "radiostereometric analysis origin styles: their impact on accuracy and precision in the assessment of spinal fusion success" to be published in English by Dalhousie University, with no commercial use
CREDIT LINE(S) must be published next to any figure, and/or if permission is granted for electronic form, visible at the same time as the content republished with a hyperlink to the publisher's home page.

WITH PAYMENT OF PERMISSIONS FEE. License, once paid, is good for one year from your anticipated publication date unless otherwise specified above. Failure to pay the fee(s) or to follow instructions here upon use of the work as described here, will result in automatic termination of the license or permission granted. All information is required. Payment should be made to Rockwater, Inc. by check or credit card, via mail

Please contact Beth Ann Rocheleau at jbjs@rockwaterinc.com or 1-803-359-4578 with questions.

## WOLTERS KLUWER HEALTH LICENSE TERMS AND CONDITIONS

Apr 13, 2012

This is a License Agreement between Alan J Spurway ("You") and Wolters Kluwer Health ("Wolters Kluwer Health") provided by Copyright Clearance Center ("CCC"). The license consists of your order details, the terms and conditions provided by Wolters Kluwer Health, and the payment terms and conditions.

All payments must be made in full to CCC. For payment instructions, please see information listed at the bottom of this form.

| License Number | 2887080997767 |
| :--- | :--- |
| License date | Apr 13, 2012 |
| Licensed content publisher | Wolters Kluwer Health |
| Licensed content publication | Spine |
| Licensed content title | Thoracic Human Vertebrae Quantitative Three-Dimensional Anatomy |
| Licensed content author | MANOHAR PANJABI, KOICHIRO TAKATA, VIJAY GOEL, et al |
| Licensed content date | Jan 1, 1991 |
| Volume Number | 16 |
| Issue Number | 8 |
| Type of Use | Dissertation/Thesis |
| Requestor type | Individual |
| Title of your thesis / | Radiostereometric Analysis Origin Styles: Their Impact on Accuracy |
| dissertation | and Precision in the Assessment of Spinal Fusion Success |
| Expected completion date | Apr 2012 |
| Estimated size(pages) | 412 |
| Billing Type | Invoice |
| Billing address | School of Biomedical Engineering |


[^0]:    ${ }^{2}$ Panjabi, M, K. Takata, V. Goel, et al "Thoracic Human Vertebrae Quantitative ThreeDimensional Anatomy" Spine, vol. 16, no. 8, pp. 888-901, 1991

